

# **Cantilever Wood Diaphragm Webinar Series**

A Design Example of a Wood Cantilever Diaphragm

### Part 2-Shear Wall Design in

**Cantilever Diaphragm Structures** 



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Questions related to specific materials, methods, and services will be addressed at the conclusion of this presentation.



# **Course Description**

Part 2 of this series will introduce an open front diaphragm design example that will be worked through in the remaining webinars. Topics addressed will include seismic force calculation and distribution, and preliminary shear wall design taking into account nominal shear wall stiffness. The impact of factors such as horizontal and torsional irregularities on force distribution to shear walls will be examined, and design of elements contributing to shear wall rotation and overturning will be discussed. The effect of gravity loads on shear walls will also be reviewed.

# **Learning Objectives**

- 1. Discuss evolutions in mid-rise building typology that have led to the need for open-front diaphragm analysis.
- 2. Review diaphragm flexibility provisions in ASCE 7 and the 2015 Special Design Provisions for Wind & Seismic (SDPWS).
- 3. Explore one option for open-front diaphragm analysis under seismic and wind loading in a wood-frame structure.
- 4. Highlight how to calculate story drift, diaphragm deflection and torsional irregularities, and discover their effects on load distribution through a cantilever diaphragm structure.

# **Fasten Your Seatbelts**



**5 out of 5 Calculators** 

WoodWorks Example and Method of Analysis:

- The solutions paper and this webinar were developed independently from the AWC task group for open-front diaphragms. The method of analysis used in this example is based on our engineering judgement, experience, and interpretation of codes and standards as to how they might relate to open-front structures.
- The analysis techniques provided in this presentation are intended to demonstrate one method of analysis, but not the only means of analysis. The techniques and examples shown here are provided as guidance and information for designers and engineers.

### **Cantilever Wood Diaphragm Webinar Series-Content**

#### Webinar Part 1- Code Requirements and Relative Stiffness issues:

- Introduction
- Questions needing resolution
- Horizontal distribution of shear and stiffness issues
- 2015 SDPWS open-front requirements
- Review preliminary design assumptions

#### Webinar Part 2- Shear Wall Design in Cantilever Diaphragm Structures:

- Introduction to open-front example
- Calculation of seismic forces and distribution
- Preliminary shear wall design
- Nominal shear wall stiffness
- Verification of shear wall design

#### Webinar Part 3- Cantilever Diaphragm Design, Flexibility and Drift Checks :

- Diaphragm design
- Maximum diaphragm chord force
- Diaphragm flexibility
- Story drift

#### Webinar Part 4-Torsional Irregularity, Other Design Checks, and Final Comments :

- Amplification of accidental torsion
- Redundancy
- Transverse direction design
- Multi-story shear wall effects

## **Content and Learning Objectives**

# Shear Wall Design:

- Introduction to open-front design example The design example plan layout and goal of the example will be explained.
- Calculation of seismic forces and distribution

The basic seismic forces and distribution to the shear walls will be covered.

### Preliminary shear wall design

The basic shear wall construction will be chosen. Suggestions for improving the preliminary wall design to limit drift and reduce torsion will be discussed.

### Nominal shear wall stiffness

A new approach for determining a single shear wall stiffness will be presented.

### Verification of shear wall design

Verification of the wall capacity will be examined after the redistribution of forces are calculated using the nominal shear wall stiffness.

# **Design Example- Longitudinal Direction**

Example plan selected to provide maximum information on design issues



**Disclaimer:** 

The following information is an open-front diaphragm example which is subject to further revisions and validation. The information provided is project specific, and is for informational purposes only. It is <u>not</u> intended to serve as recommendations or as the only method of analysis available.

Page 4





(Platform framing not shown)

**Typical Exterior Wall Sections** 



**Typical Exterior Wall Elevations at Grid Lines A and B** 





#### **Typical Spreadsheet**



#### Analysis Flow Longitudinal Design



Example Plan



#### Assumptions Made: Page 8

- Diaphragm is rigid or semi-rigid in both directions
- Torsional irregularity Type 1a occurs in longitudinal direction, but not transverse, Ax=1.25.
- Horizontal irregularity Type 1b does not occur in either direction.
- No redundancy in both directions, ρ=1.3



### **Basic Project Information**

- Structure-Occupancy B, Office, Construction Type VB-Light framing:
  - Wall height=10'-Single story
  - L=76', total length
  - W'=40', width/depth
  - L'=35', cantilever length (max.)
  - o 6' corridor width
- Roof DL (seismic)= 35.0 psf including wall/ partitions
- Wall DL = 13.0 psf (in-plane)
- Roof snow load = 25 psf > required roof LL=20 psf
- Roof (lateral)= roof + wall H/2 plus parapet

### Lateral Load Calculations-Seismic

Calculate Seismic Forces -ASCE 7-16 Section 12.8 Equivalent Lateral Force Procedure,  $F_x$ 

- Risk category II
- Importance factor, le = 1.0

Using USGS Seismic Design Map-Tool, 2015 NEHRP, 2016 ASCE 7-16:

- Location-Tacoma, Washington
- Site class D-stiff soil
- Ss = 1.355 g, S1 = 0.468 g
- SDS = 1.084 g, SD1 = 0.571 g
- Seismic Design Category (SDC) = D

ASCE 7-16 Table 12.2-1, Bearing Wall System, A(15) light framed wood walls w/ WSP sheathing. R = 6.5,  $\Omega_0$ =3, Cd=4, Maximum height for shear wall system=65'.

### **Seismic Force Calculation results:**

$$C_s = rac{S_{DS}}{\left(rac{R}{I_e}
ight)} = 0.167$$
 short period controls

**Basic lateral force MSFRS** 

V = C<sub>s</sub>W = 0.167(35)(76)(40) = 17769 lbs. STR 17769(0.7) = 12438 lbs. ASD

**Rigid Diaphragm Analysis-** ρ=1.3, Ax=1.25 Initial wall stiffness will be based on wall length.

The final wall <u>Nominal stiffness's</u> are used for all final analysis checks.

#### **RDA Equations**

T = V(e)(Ax)(
$$\rho$$
) ft. lbs.  

$$F_T = T \frac{kd}{\sum kd_x^2 + kd_y^2}$$

$$F_{sw} = F_V + F_T$$

$$J = \sum kd_x^2 + kd_y^2$$

$$F_V = F_x \frac{k}{\sum k}$$





### **SW Design Checks**

Check aspect ratio, If A.R.>2:1, reduction is required per SDPWS Section 4.3.4.
 A.R. = 1.25:1< 3.5:1. Since the A.R. does not exceed 2:1, no reduction is required.</li>

• Wall shear: 
$$V_{swA, B} = \frac{V_{wall line}}{2}$$
 Lbs. each wall segment,  $v_s = \frac{V_{wall}}{L_{wall}}$  plf

- Select over-turning anchor-capacity > demand.
- Calculate actual anchor slip, slip =  $\frac{\text{Max slip at capacity}(T)}{\text{Strength capacity}}$
- Determine shear wall chord properties:

2x6 DF-L no. 1 framing used throughout. E = 1,700,000 psi, wall studs @ 16" o.c.

EA= 42,075,000 lbs. at grid line A,B = (3)2x6 D.F., KD, studs @16" o.c. boundary elem.

EA= 28,050,000 lbs. at grid line 2,3 = (2)2x6 D.F., KD, studs @16" o.c. boundary elem.

Calculate wall deflection

• Shear Wall Deflection-calculated using:

Traditional 4 term deflection equation



**SDPWS 3 term deflection equation** 



Note:

Calculate wall deflection as:  $\delta_{swA,B} = \frac{F}{k}$ 

after Nominal stiffness has been established



#### **Causes of Wall Rotation**

- Hold downs = pre-manufactured bucket style with screw attachments Same H.D used at all SW locations
  - Manuf. table gives Allowable ASD hold down capacity and displacement at capacity (ESR Reports)
  - **Displacement at hold down** =  $\frac{T(Allow.Displ)}{ASD Capacity}$
  - Min. wood attachment thickness = 3" per table
- Sill plate shrinkage:

Dimensional change = 0.0025 inches per inch of cross-sectional dimension for every 1 percent change in MC.

Shrinkage = (0.0025)(D)(Starting MC - End MC)

Where: D is the dimension of the member in the direction under consideration, in this case the thickness of a wall plate.

#### • Sill plate crushing:

 $F'_{c\perp}$  values in AWC 2018 NDS section 4.2.6 are based on 0.04" deformation/crushing limit for a steel plate bearing on wood.

Adjustment factor = 1.75 for parallel to perpendicular grain wood to wood contact.

Boundary values for bearing perpendicular to grain stresses and crushing-D.F.

$$F_{c\perp 0.02} = 0.73 F_{c\perp}' = 0.73$$
(625) = 456.3 psi $F_{c\perp 0.04} = F_{c\perp}' =$  625 psi

When 
$$f_{c\perp} \leq F_{c\perp 0.02}$$
 "

$$\Delta_{crush} = 0.02 \left( \frac{f_{c\perp}}{F_{c\perp 0.02}} \right)$$

When  $F_{c\perp 0.02}$ "  $\leq f_{c\perp} \leq F_{c\perp 0.04}$ "

$$\Delta_{crush} = \mathbf{0}.\,\mathbf{04} - \mathbf{0}.\,\mathbf{02} \left( \frac{1 - \frac{f_{c\perp}}{F_{c\perp 0.04}}}{0.27} \right)$$

When 
$$f_{c\perp} > F_{c\perp 0.04}$$
"  

$$\Delta_{crush} = 0.04 \left(\frac{f_{c\perp}}{F_{c\perp 0.04}}\right)^{3}$$
If  $f_{c\perp} = \left(\frac{c}{A_{chord}}\right) < 456.3$  psi, Crushing =  $0.02 \left(\frac{f_{c\perp}}{456.3}\right)$ (1)





Load Combinations (ASD):

LC8 = 1.152D +0.7ρQE

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LC9 = 1.114D + 0.525\rho Q_{E} + 0.75S
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LC10 = 0.448D+0.7ρQ<sub>E</sub>

Full dead loads shown, 1.0D

### Adding Gravity Loads to SW's

- Can have a significant impact on horizontal shear wall deflections and stiffness.
- Results in wall stiffness (K = F/δ) relationships which are non-linear with the horizontal loading applied.



Shear Walls Along Grid Lines A and B Design Dimensions



**Design Dimensions** 

#### Based on initial Relative Wall Stiffness's, ASD, ρ=1.3, Ax=1.25 –by wall lengths

| SW<br>Line | Ky<br>k/in | Kx<br>k/in | Dx<br>Ft. | Dy<br>Ft. | Kd  | Kd <sup>2</sup> | Fv<br>Lbs. | Fτ<br>Lbs. | Total<br>Lbs. | Grid<br>& B |
|------------|------------|------------|-----------|-----------|-----|-----------------|------------|------------|---------------|-------------|
| Α          |            | 16         |           | 20        | 320 | 6400            | 0          | 1842.4     | 1842.4        | s at (      |
| В          |            | 16         |           | 20        | 320 | 6400            | 0          | -1842.4    | -1842.4       | Wall        |
| 2          | 30         |            | 3         |           | 90  | 270             | 8084.9     | -518.2     | 7566.7        | dor         |
| 3          | 30         |            | 3         |           | 90  | 270             | 8084.9     | 518.2      | 8603.1        | Corri<br>Va |
|            | ΣKy=60     | ΣKx=32     |           |           |     | J=16169.8       |            |            |               | - •         |

Longitudinal Direction, e=4.75', T = 76806.5 ft. lbs.

Transverse Direction, e=2.5', T = 40424.5 ft. lbs.

| SW<br>Line | Ky<br>k/in | Kx<br>k/in | Dx<br>Ft. | Dy<br>Ft. | Kd  | Kd <sup>2</sup> | Fv<br>Lbs. | FT<br>Lbs. | Total<br>Lbs. | Grid<br>& B |
|------------|------------|------------|-----------|-----------|-----|-----------------|------------|------------|---------------|-------------|
| Α          |            | 16         |           | 20        | 320 | 6400            | 8084.9     | 969.7      | 9054.6        | s at<br>s A |
| В          |            | 16         |           | 20        | 320 | 6400            | 8084.9     | -969.7     | 7115.2        | Wall        |
| 2          | 30         |            | 3         |           | 90  | 270             | 0          | -272.7     | -272.7        | dor         |
| 3          | 30         |            | 3         |           | 90  | 270             | 0          | 272.7      | 272.7         | Corri<br>Va |

**ΣKy=60 ΣKx=32** 

J=16169.8

Page 14

#### Preliminary Shear Wall Design-Distribution based on wall lengths



Shear Walls Along Grid Lines A and B Transverse Loading Shear Walls Along Grid Lines 2 and 3 Longitudinal Loading

#### Calculated results by wall length

Vsw A,B = 565.9 plf

Vsw 2,3 = 286.8 plf

#### **Shear Wall Capacity-Wood Based Panels**

#### Blocked Table 4.3A Nominal Unit Shear Capacities for Wood-Framed Shear Walls

| Wood Based Panels <sup>4</sup> |  |   |  |                     |                                      |                     |                     |       |       |       |       |  |
|--------------------------------|--|---|--|---------------------|--------------------------------------|---------------------|---------------------|-------|-------|-------|-------|--|
|                                |  | Minimum<br>Fastener   | Fastener<br>Type & Size<br>Nail<br>(common o<br>Galvanized<br>box) |                     | ہ<br>Seis                            | B<br>Wind           |                     |       |       |       |       |  |
| Sheathing<br>Material          | Nominal<br>Panel<br>Thickness<br>(in.) | Penetration<br>In Framing<br>Member or<br>Blocking<br>(in.) |  | Panel               | Panel Edge Fastener<br>Spacing (in.) |                     |                     | er    |       |       |       |  |
|                                |  |   |  | 6                   | 4                                    | 3                   | 2                   | 6     | 4     | 3     | 2     |  |
|                                |  |   |  | (plf)<br>(kips/in.) | (plf)<br>(kips/in.)                  | (plf)<br>(kips/in.) | (plf)<br>(kips/in.) | (plf) | (plf) | (plf) | (plf) |  |
| Wood <sup>4,5</sup>            |  |   |  | Vs Ga<br>OSB PLY    | Vs Ga<br>OSB PLY                     | Vs Ga<br>OSB PLY    | Vs Ga<br>OSB PLY    | Vw    | Vw    | Vw    | Vw    |  |
| Structural                     | 15/32                                  | 1-3/8   | 8d   | 520 13 10           | 760 19 13                            | 980 25 15           | 1280 39 20          | 730   | 1065  | 1370  | 1790  |  |
| Panels-                        | 15/32                                  |   |  | 620 22 14           | 920 30 17                            | <b>1200 37</b> 19   | 1540 52 23          | 870   | 1290  | 1680  | 2155  |  |
| Sheathing                      | 19/32                                  | 1-1/2   | 10d  | 680 19 13           | 1020 26 1                            | 1330 33 18          | 1740 48 28          | 950   | 1430  | 1860  | 2435  |  |
|                                |  |   |  |                     |                                      |                     |                     |       |       |       |       |  |

Increasing stiffness to account for drift, torsion, etc. requires engineering judgement.

SWA,B: Use 15/32" OSB w/ 10d@3" o.c., vs= (1200)/2 = 600 plf, Ga=37 SW2,3: Use 15/32" OSB w/ 10d@4" o.c., vs= (920)/2 = 460 plf, Ga=30

Maximum tension force, T= 4570 lbs.- Use HD=4565 lbs. (0.1% under-check later) ASD,  $\Delta a=0.114''$  @ capacity STR,  $\Delta a=0.154''$  @ capacity Page 13

### **Determination of Nominal Wall Stiffness**

Combining Rigid Diaphragm Analysis & shear wall deflection calculations is problematic due to non-linearities, which can effect the distribution of loads to the shear walls and will effect the shear wall deflections. This can lead to a different set of stiffness values that may not be consistent.

Whenever changing:

- Load combinations
- Vertical or lateral loads,
- Direction of loading
- Redundancy, or
- Accidental torsion

Requires an Iterative search for the point of convergence, which is not practical for multistory structures.

Sources of non-linearities:

- Hold-down slip at uplift (e.g. shrinkage gap)
- Hold-down system tension and elongation
- Compression crushing. Non-linear in NDS
- Shrinkage
- 4-term deflection equation

Since deflection is "non-linear".... the stiffness can vary with the loading, even when using 3-term deflection equation.

#### Page 16

#### **LATERAL Load for Shear Wall Deflection & Stiffness Calculations**

- 3-term equation is a linear simplification of the 4-term equation, calibrated to match the applied load at 1.4 ASD.
- This simplification removes the non-linear behavior of en.
- Similar approach can be used to remove non-linear effects of Δa by calculating the wall stiffness at strength level capacity of the wall, not the applied load.



#### Method allows having only one set of nominal stiffness values.

#### **Objective:**

Use a single rational vertical and lateral load combination to calculate deflections and Nominal shear wall stiffness.

#### **Gravity Loads:**

A simplification of gravity loads are applied similar to nonlinear procedures in ASCE 41-13 in ASCE 41-13 Eq. 7-3.

For this Single-Story Example we used 1.0D, using  $\rho = 1.0$  and Ax = 1.0. Vertical seismic loading not included. (Ev=0.2SpsD)

For multi-story buildings, suggest 1.0D+  $\alpha$ L as in ASCE 7-16 Section 16.3.2- Nonlinear analysis

Results in single vertical loading condition to use when calculating shear wall deflections and nominal shear wall stiffnesses.

#### **Proposing:**

- 1. Stiffness calculated using 3-term eq. and LC 1.0D+Qe, with ρ=1.0 and Ax=1.0.
- 2. Use stiffness calculated at 100% Maximum Seismic Design Capacity of the Wall for all Load Combinations and Drift Checks from RDA using 3 term equation.
- 3. Use nominal stiffness for all other analysis checks, calculating wall deflection,  $\delta_{SW} = \frac{F}{\kappa}$
- Maximum wall capacity =max. allow. Shear (nailing) or HD capacity whichever is less. 4.



### Nominal Shear Wall Stiffness's (STR) p=1.0, Ax=1.0

Load Combination: 1.0D + QE



### **Verification of Wall Strength (ASD)**

#### **Based on selected wall construction and Nominal Wall Stiffness**

| Longitudinal Direction, e=4.75', T = 76806.5 ft. lbs. | ρ=1.3, Ax=1.25 |
|---|----------------|
|---|----------------|

|            |            |            |           |           |        |                 |            |            |               | _               |
|------------|------------|------------|-----------|-----------|--------|-----------------|------------|------------|---------------|-----------------|
| SW<br>Line | Ky<br>k/in | Kx<br>k/in | Dx<br>Ft. | Dy<br>Ft. | Kd     | Kd <sup>2</sup> | Fv<br>Lbs. | Fт<br>Lbs. | Total<br>Lbs. | t Grid<br>8 B   |
| А          |            | 25.14      |           | 20        | 502.8  | 10056           | 0          | 1848.1     | 1848.1        | lls af<br>ìes A |
| В          |            | 25.14      |           | 20        | 502.8  | 10056           | 0          | -1848.1    | -1848.1       | lir Va          |
| 2          | 43.54      |            | 3         |           | 130.62 | 391.86          | 8084.9     | -480.1     | 7604.8        | ridor<br>alls   |
| 3          | 43.54      |            | 3         |           | 130.62 | 391.86          | 8084.9     | 480.1      | 8565.0        | C or            |
| 2          | ΣKy=87.08  | ΣKx=50.28  | }         |           |        | J=20895.72      |            |            |               | -               |

Transverse Direction – e=2.5', T = 40424.5 ft. lbs.  $\rho=1.3$ , Ax=1.25

|    |            |            |           |           |        |                 |            |            |               | _                |
|----|------------|------------|-----------|-----------|--------|-----------------|------------|------------|---------------|------------------|
| SW | Ky<br>k/in | Kx<br>k/in | Dx<br>Ft. | Dy<br>Ft. | Kd     | Kd <sup>2</sup> | Fv<br>Lbs. | FT<br>Lbs. | Total<br>Lbs. | at Grid<br>A & B |
| Α  |            | 25.14      |           | 20        | 502.8  | 10056           | 8084.9     | 972.7      | 9057.6        | alls a           |
| В  |            | 25.14      |           | 20        | 502.8  | 10056           | 8084.9     | -972.7     | 7112.2        | l≊ ≔             |
| 2  | 43.54      |            | 3         |           | 130.62 | 391.86          | 0          | 252.7      | 252.7         | ridor<br>alls    |
| 3  | 43.54      |            | 3         |           | 130.62 | 391.86          | 0          | -252.7     | -252.7        | Co<br>Co         |
|    | ΣKy=87.08  | ΣKx=50.2   | 8         |           |        | J=20895.72      |            |            |               | _                |

Nominal stiffness values used

ASD Load Combination: LC10 0.448D + 0.7ρQE ρ=1.3, Ax=1.25



Shear wall Grid A and B

Shear Walls Along Grid Lines A and B Transverse Loading- Nominal Strength

vs =  $\frac{4528.8}{8}$  = 566.1 plf <600 plf allowed ∴ o.k. T= 4579.2 lbs. ≈ 4565 lbs. allowed, 0.3% over ∴ hold down o.k. –check later



Shear Walls Along Grid Lines 2 and 3 Longitudinal Loading- Nominal Strength

vs =  $\frac{2855}{10}$  = 285.5 plf. < 460 plf allowed ∴ o.k. T = 2557.1 lbs. < 4565 lbs. allowed ∴ hold down o.k. **Questions?** 

This concludes Woodworks Presentation on:

Part 2-Shear Wall Design in Cantilever Diaphragm Structures

Your comments and suggestions are valued. They <u>will</u> make a difference.

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#### Thank You

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