

Structural Design of Mass Timber Framing Systems

Presented by Paul B. Becker, PE

Thornton Tomasetti

Disclaimer: This presentation was developed by a third party and is not funded by WoodWorks or the Softwood Lumber Board.

“The Wood Products Council” is a Registered Provider with The American Institute of Architects Continuing Education Systems (AIA/CES), Provider #G516.

Credit(s) earned on completion of this course will be reported to AIA CES for AIA members. Certificates of Completion for both AIA members and non-AIA members are available upon request.

This course is registered with AIA CES for continuing professional education. As such, it does not include content that may be deemed or construed to be an approval or endorsement by the AIA of any material of construction or any method or manner of handling, using, distributing, or dealing in any material or product.

Questions related to specific materials, methods, and services will be addressed at the conclusion of this presentation.



Course Description

This presentation will provide a detailed look at the structural design processes associated with a variety of mass timber products, including glu-laminated timber (glulam), cross-laminated timber (CLT), and nail laminated timber (NLT). Applications for the use of these products in gravity force-resisting systems under modern building codes will be discussed. Other technical topics will include the use of mass timber panels as two-way spanning slabs, connection options and design considerations, and detailing and construction best practices.

Learning Objectives

1. Provide an overview of available mass timber products, design standards and structural optimization.
2. Review structural design properties and design considerations for CLT floor and roof slabs
3. Review design properties and design considerations for glulam beams and columns
4. Review connection options for CLT and glulam beams

Bath, NY circa 1880



Mass Timber Products



CLT



GLULAM



NLT



DLT



LVL



LSL



PSL



MPP

Albina Yards, Portland, OR circa 2016

Lever Architecture
Four-Story, 16,000 sf



photo: Lever Architecture

Albina Yards, Portland, OR circa 2016



photo: Lever Architecture

T3, Minneapolis, MN circa 2017

Michael Green Architecture/DLR Group
Seven-Story, 220,000 sf



photo: Hines Development

T3, Minneapolis, MN circa 2017

Michael Green Architecture/DLR Group
Seven-Story, 220,000 sf



photo: Hines Development

Candlewood Suites, Huntsville, AL, circa 2015



CLT Bearing Walls /Slabs
3-ply walls, 5-ply slabs
Four-stories 62,700 sf

photo: Lend Lease

Spaced CLT

allows for MEP chase, inlay ceiling



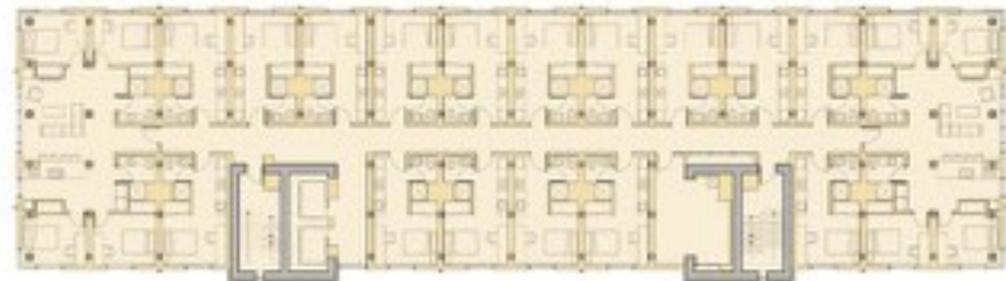
photo: MGA

Brock Commons, Vancouver, BC

18 stories, two-way slabs, no beams



9.33' x 13.0' grid, 18 stories

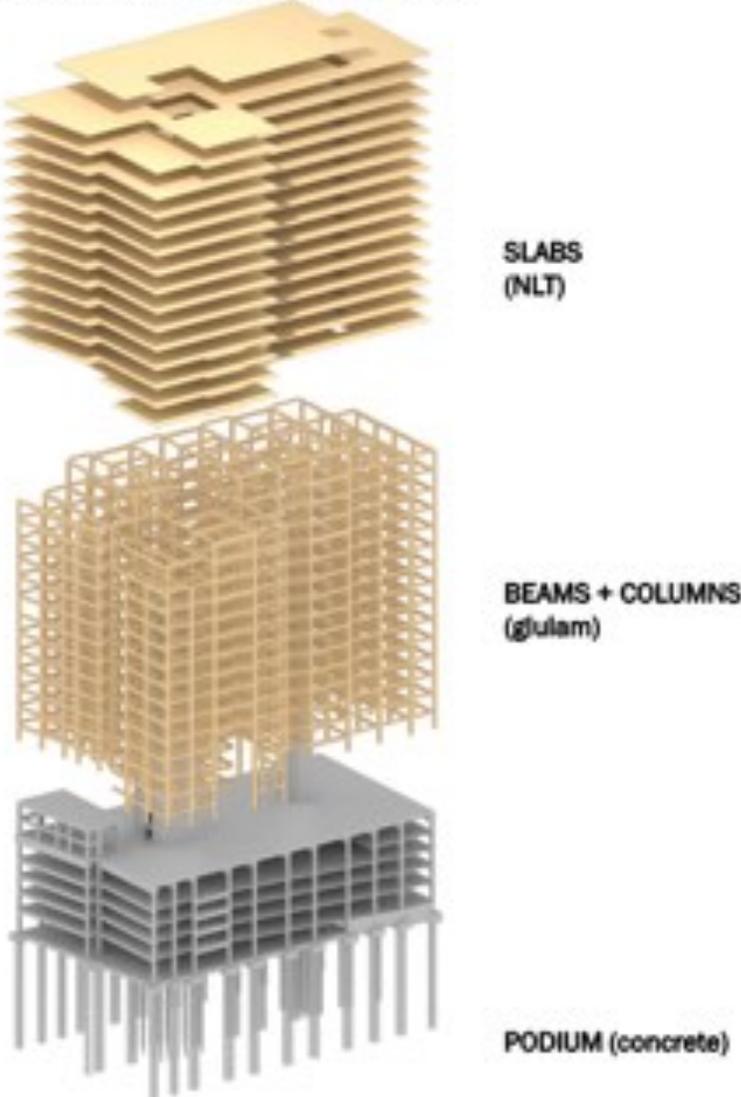


Ascent Tower, Milwaukee, WI

21 stories (5+16) @ 238 ft



STRUCTURAL SYSTEM - WOOD



Mass Timber Products



Nail Laminated Decking



SHRINKAGE / SWELLING GAP TO BE FILLED IN AFTER BUILDING IS ENCLOSED. GLUE OR FINISH.

2 SHRINKAGE / SWELLING GAP
TYP. GRIDS B, C, F AND G ONLY
1-10

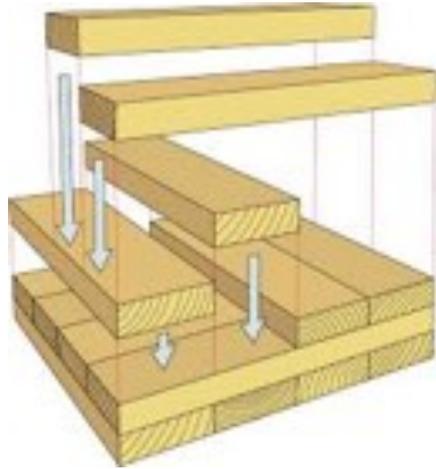
Mass Timber Products



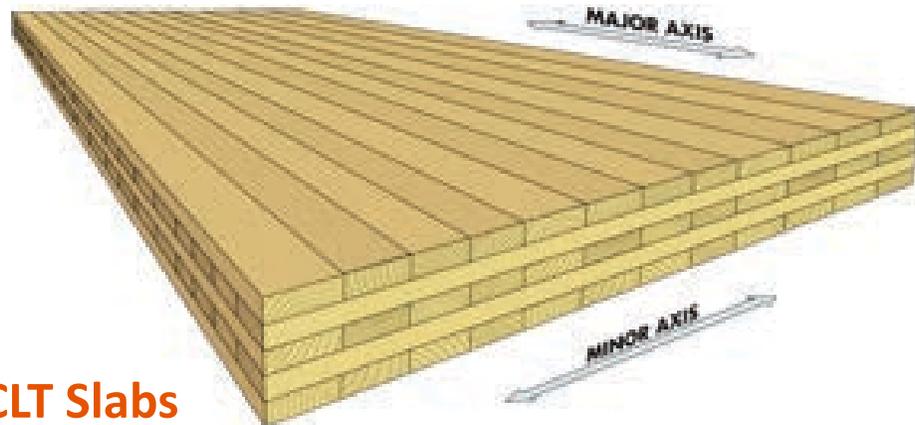
Dowel Laminated Decking



Cross-Laminated Timber



Non-homogeneous, anisotropic material



CLT Slabs

Images source: CLT Handbook

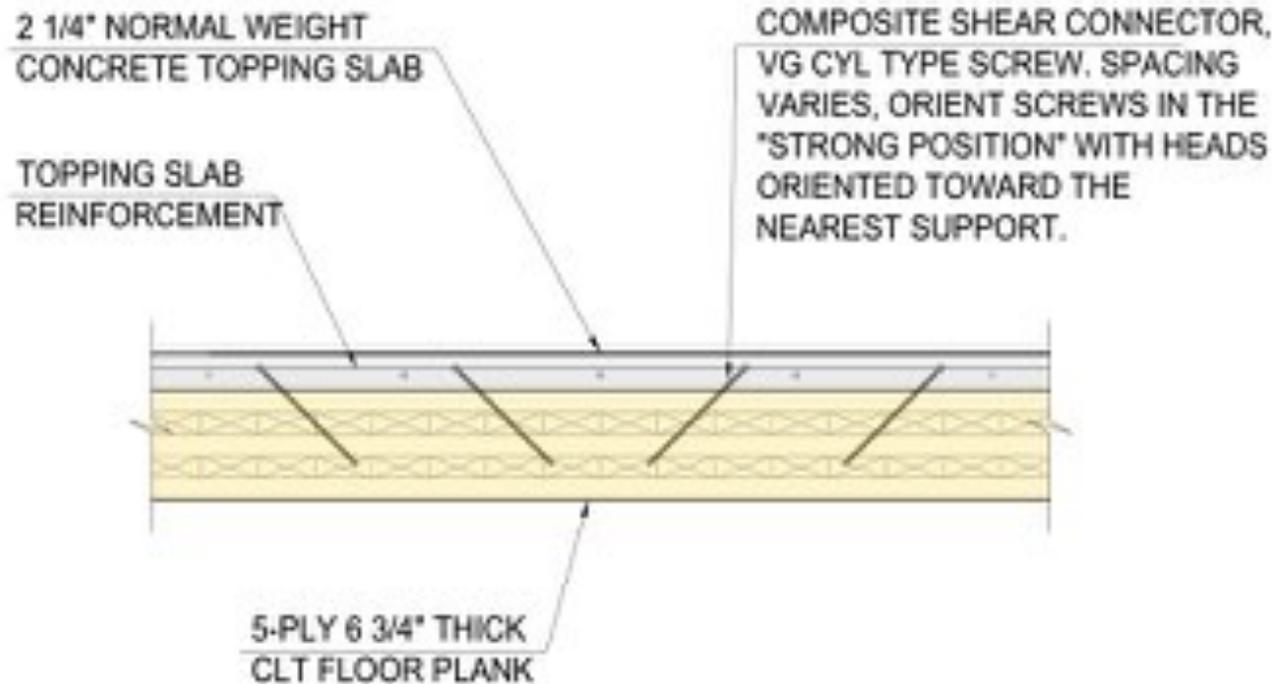
Composition

- 3-ply minimum, up to 9 ply
- Pieces 5/8" to 2 inch thick
- Pieces 2.4 inches to 9.5 inches wide
- Boards finger jointed
- MSR or visual, all kiln dried
- Width and length by manufacturer

Advantages

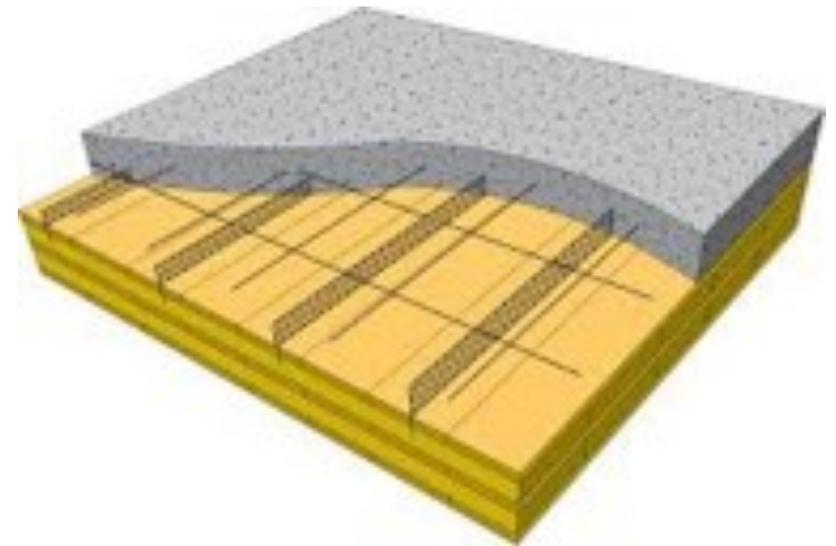
- Dimensionally stable product
- High strength to weight ratio
- Long, wide slabs
- High in-plane, out of plane strength + stiffness
- two-way action
- Connector splitting resistance

Composite CLT



screw connector field applied

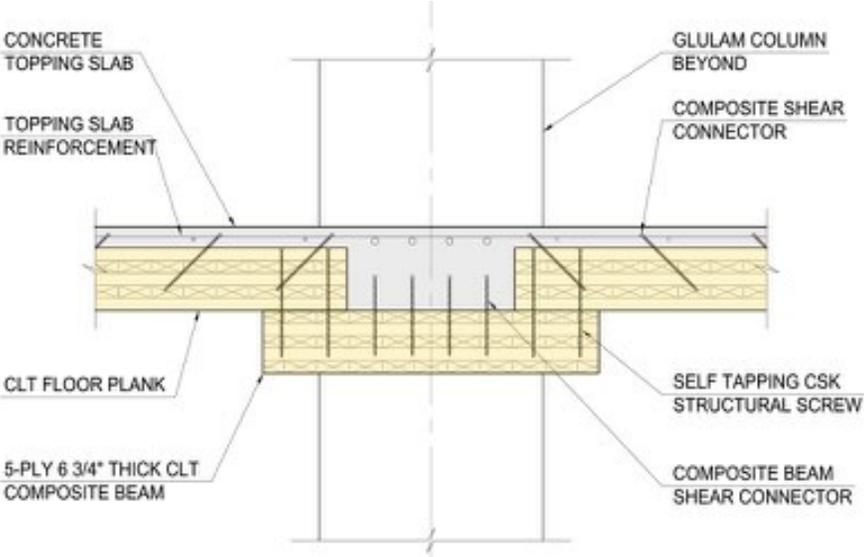
Images source: SOM



**proprietary mesh connector
epoxied into CLT**

Images source: Setragian/Kusuma

Composite Construction



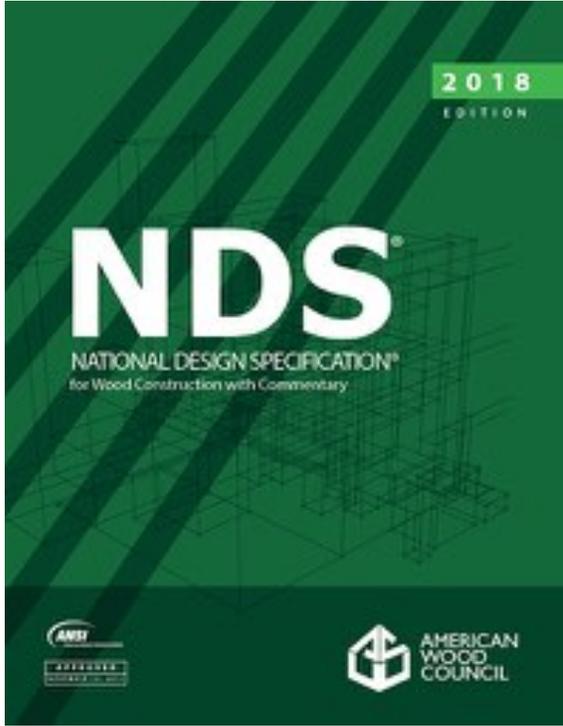
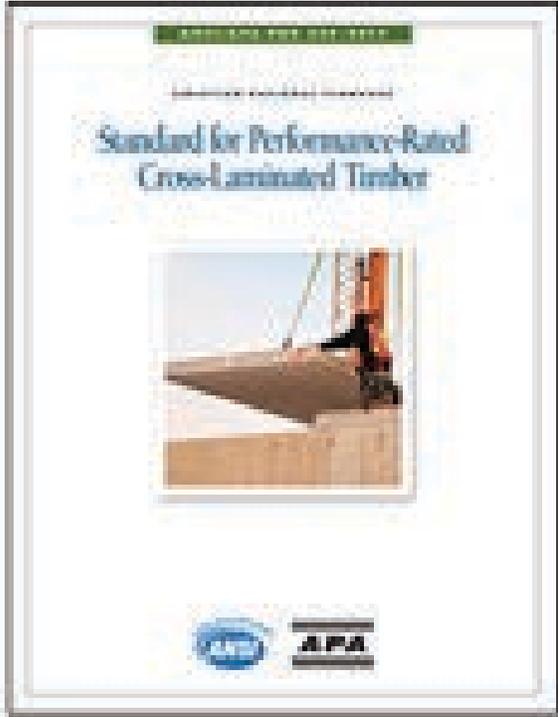
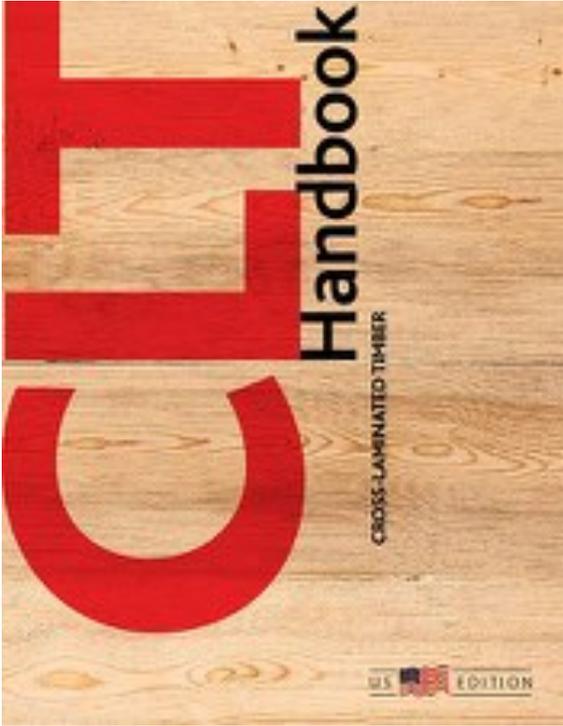
Images source: SOM

Mass Timber Design

Design Considerations – In-Plane and Out-of-Plane

- Bending Strength
 - Shear Strength
- }] strength
- Bending Stiffness
 - Shear Stiffness
 - Vibration
- }] serviceability

Mass Timber Design Guides



Common CLT Layups

3-ply 3 layer
(3.43"-4.14")



5-ply 5 layer
(5.47"-6.90")



5-ply 3 layer
(5.47"-6.90")

7-ply 7 layer
(7.52"-9.66")



7-ply 5 layer
(7.52"-9.66")

9-ply 9 layer
(9.57"-12.42")



9-ply 7 layer
(9.57"-12.42")

Figure 2
Examples of CLT panel cross-sections

Images source: PRG 320-2018

CLT Stress Grades

Stress Grade	Major Axis	Minor Axis
E1	1950f-1.7E MSR SPF	#3 Spruce Pine Fir
E2	1650f-1.5E MSR DFL	#3 Doug Fir Larch
E3	1200f-1.2E MSR Misc	#3 Misc
E4	1950f-1.7E MSR SP	#3 Southern Pine
V1	#2 Doug Fir Larch	#3 Doug Fir Larch
V2	#1/#2 Spruce Pine Fir	#3 Spruce Pine Fir
V3	#2 Southern Pine	#3 Southern Pine

CLT Stress Grades

TABLE A1

ASD REFERENCE DESIGN VALUES^{a,b,c} FOR LAMINATIONS (FOR USE IN THE U.S.)

CLT Layup	Laminations Used in Major Strength Direction						Laminations Used in Minor Strength Direction					
	F_b (psi)	E^d (10^3 psi)	F_c (psi)	$F_{c\parallel}$ (psi)	$F_{c\perp}$ (psi)	$F_{c\parallel}$ (psi)	F_b (psi)	E^d (10^3 psi)	F_c (psi)	$F_{c\parallel}$ (psi)	$F_{c\perp}$ (psi)	$F_{c\parallel}$ (psi)
E1	1,950	1.7	1,375	1,800	135	45	500	1.2	250	650	135	45
E2	1,650	1.5	1,020	1,700	180	60	525	1.4	325	775	180	60
E3	1,200	1.2	600	1,400	110	35	350	0.9	150	475	110	35
E4	1,950	1.7	1,375	1,800	175	55	450	1.3	250	725	175	55
V1	900	1.6	575	1,350	180	60	525	1.4	325	775	180	60
V2	875	1.4	450	1,150	135	45	500	1.2	250	650	135	45
V3	750	1.4	450	1,250	175	55	450	1.3	250	725	175	55

For SI: 1 psi = 0.006895 MPa

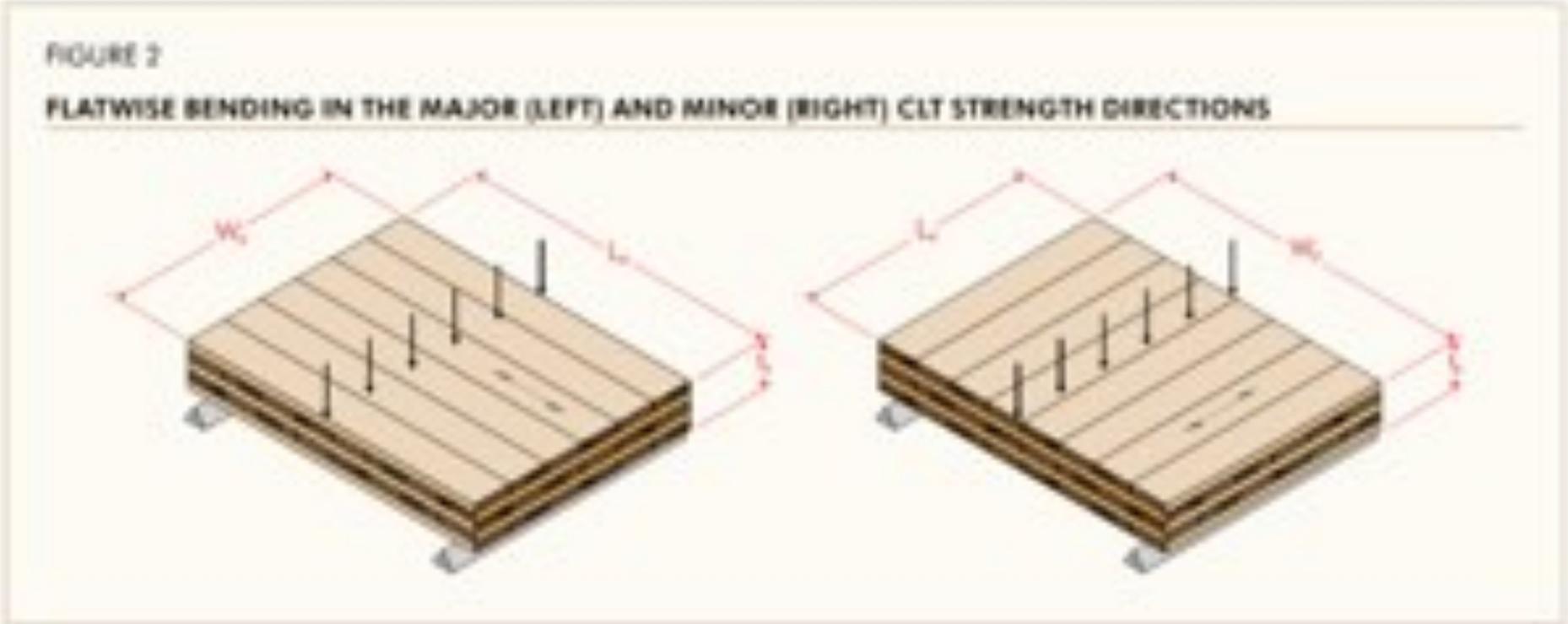
- See Section 4 for symbols.
- Tabulated values are ASD reference design values and not permitted to be increased for the lumber size and flat use adjustment factors in accordance with the NDS. The design values shall be used in conjunction with the section properties provided by the CLT manufacturer based on the actual layup used in manufacturing the CLT panel (see Table A2).
- Custom CLT layups that are not listed in this table shall be permitted in accordance with 7.2.1.
- The tabulated E values are published E for lumber. For calculating the CLT design properties shown in Table A2, the transverse E of the lamination is assumed to be E/30, the longitudinal G of the lamination is assumed to be E/16, and the transverse G of the lamination is assumed to be longitudinal G/10.



CLT Supply Options

Suppliers	Location	Panel Length (ft)	Panel Width (ft)	Grades	Availability
● Structurlam	British Columbia	40	8, 10	V2, E1	Available
● Nordic	Quebec	64	8	E1	Available
● DR Johnson	Oregon	42	8, 10	E2, V1	Available
● International Beam	Alabama	52.5	8, 10, 12	V3	Available
Smartlam	Montana	40/64	8, 10	V4	Available
KLH	Austria	38	7.33		Available
● Binderholz	Austria	38	11.5	Spruce, E1, V2	Available
StructureCraft	British Columbia	60	8, 10, 12		Available
Katerra	Washington	60	12	E1, V2	Available
● Vaagen	Washington	60	4	E2, V1	Available
Freres (MPP)	Oregon	48	12	E2	Available
● Kalesnikoff	British Columbia	-	-	-	Available 2020
Ligna Terra	Maine	-	-	-	Available 2022?

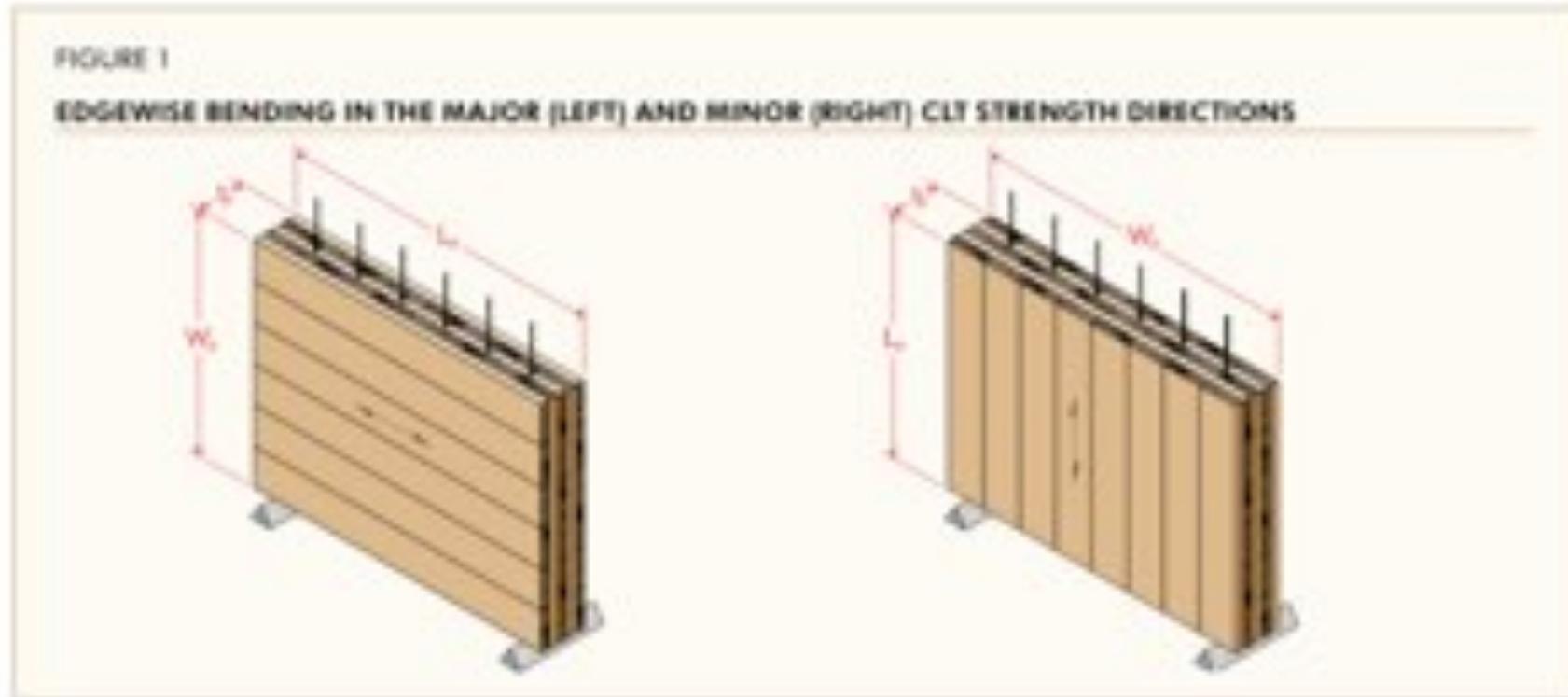
Flatwise Panel Loading



MAJOR

MINOR

Edgewise Panel Loading



Bending Members- Flexure (out of plane)

PRG 320- calculates capacity using extreme fiber capacity approach

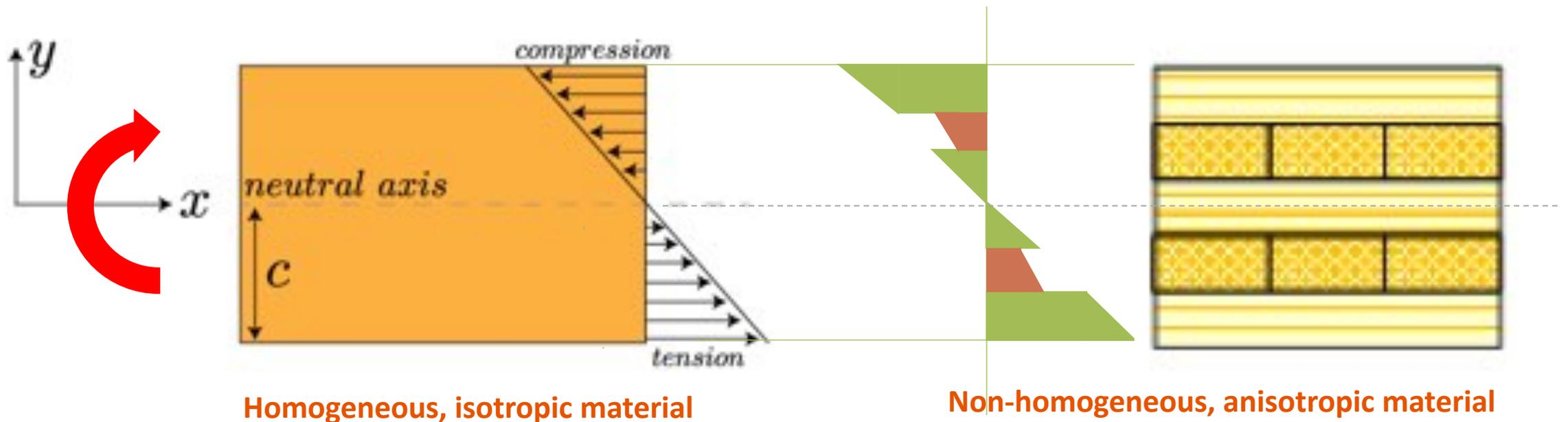
From Strength of Materials/Engineering Mechanics, we know

$$F_b = \frac{M c}{I}$$

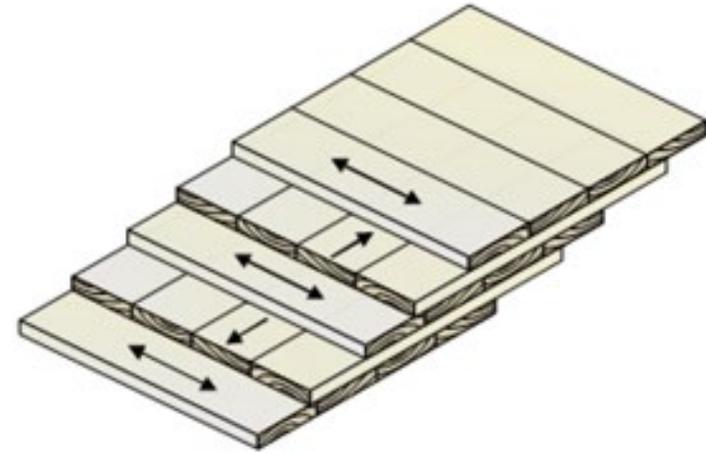
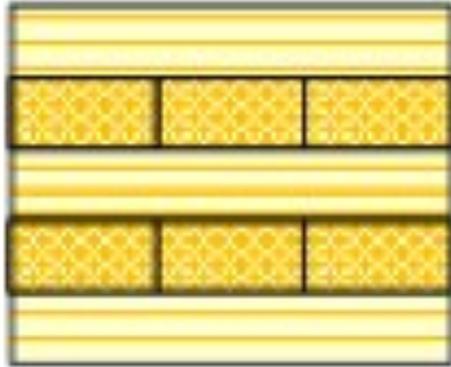
$$S = \frac{I}{c}$$

$$M = F_b S$$

$$M_b \leq (F_b S_{\text{eff}})'$$



Bending Members- Flexure (out of plane)



Flexural Capacity Check:

$$M_b \leq (F_b S_{\text{eff}})'$$

M_b = applied bending moment

$(F_b S_{\text{eff}})'$ = adjusted bending capacity

S_{eff} = effective section modulus

F_b = reference bending design stress of outer lamination

$$S_{\text{eff}} = \frac{2EI_{\text{eff}}}{E_1 h}$$

where:

EI_{eff} = Effective bending stiffness

E_1 = Modulus of elasticity of outermost layer

h = Entire thickness of panel

Bending Members- Flexure (out of plane)

$$EI_{eff} = \sum_{i=1}^n E_i \cdot b_i \cdot \frac{h_i^3}{12} + \sum_{i=1}^n E_i \cdot A_i \cdot z_i^2 \quad [24]$$

Table 3

Parallel axis theorem calculations for EI_{eff}

Layer	E (x 10 ⁶ psi)	z (in.)	Ebh ³ /12 (lb.-in. ²)	EAz ² (lb.-in. ²)	Sum of Layer
1	1.7	2.75	4.4	212.1	216.5
2	1.2/30=0.04	1.375	0.1	1.2	1.4
3	1.7	0.0	4.4	0.0	4.4
4	0.04	1.375	0.1	1.2	1.4
5	1.7	2.75	4.4	212.1	216.5
				Total	440

Bending Members- Flexure (out of plane)

TABLE A2
ASD REFERENCE DESIGN VALUES^{a,b,c} FOR CLT (FOR USE IN THE U.S.)

CLT Layup	Lamination Thickness (in.) in CLT Layup									Major Strength Direction				Minor Strength Direction			
	CLT t_p (in.)	=	⊥	=	⊥	=	⊥	=	⊥	$(F_v S)_{allow}$ (lb-ft/ft of width)	$(EI)_{allow}$ (10 ⁶ lb-ft ² /ft of width)	$(GA)_{allow}$ (10 ³ lb/ft of width)	V_{LH} (lb/ft of width)	$(F_v S)_{allow}$ (lb-ft/ft of width)	$(EI)_{allow}$ (10 ⁶ lb-ft ² /ft of width)	$(GA)_{allow}$ (10 ³ lb/ft of width)	V_{LH} (lb/ft of width)
E1	4 1/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	4,525	115	0.46	1,430	160	3.1	0.61	495
	6 7/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	10,400	440	0.92	1,970	1,370	81	1.2	1,430	
	9 5/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	18,375	1,089	1.4	2,490	3,125	309	1.8	1,960	
E2	4 1/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	3,825	102	0.53	1,910	165	3.6	0.56	660	
	6 7/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	8,825	389	1.1	2,625	1,430	95	1.1	1,910	
	9 5/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	15,600	963	1.6	3,325	3,275	360	1.7	2,625	
E3	4 1/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	2,800	81	0.35	1,110	110	2.3	0.44	385	
	6 7/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	6,400	311	0.69	1,530	955	61	0.87	1,110	
	9 5/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	11,325	769	1.0	1,940	2,180	232	1.3	1,520	
E4	4 1/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	4,525	115	0.50	1,750	140	3.4	0.62	605	
	6 7/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	10,400	440	1.0	2,410	1,230	88	1.2	1,750	
	9 5/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	18,400	1,089	1.5	3,050	2,800	335	1.9	2,400	
V1	4 1/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	2,090	108	0.53	1,910	165	3.6	0.59	660	
	6 7/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	4,800	415	1.1	2,625	1,430	95	1.2	1,910	
	9 5/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	8,500	1,027	1.6	3,325	3,275	360	1.8	2,625	
V2	4 1/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	2,030	95	0.46	1,430	160	3.1	0.52	495	
	6 7/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	4,675	363	0.91	1,970	1,370	81	1.0	1,430	
	9 5/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	8,275	898	1.4	2,490	3,125	309	1.6	1,960	
V3	4 1/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	1,740	95	0.49	1,750	140	3.4	0.52	605	
	6 7/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	4,000	363	0.98	2,420	1,230	88	1.0	1,750	
	9 5/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	1 3/8	7,100	899	1.5	3,050	2,800	335	1.6	2,400	

For SI: 1 in. = 25.4 mm; 1 ft = 304.8 mm; 1 lb = 4.448 N

a. See Section 4 for symbols.

b. This table represents one of many possibilities that the CLT could be manufactured by varying lamination grades, thicknesses, orientations, and layer arrangements in the layup.

c. Custom CLT layups that are not listed in this table shall be permitted in accordance with 7.2.1.

Note A1. The rounding rules in Table A2 are as follows:

$F_v S$ (lb-ft/ft) and V_L (lb/ft)—Nearest 25 for values greater than 2,500, nearest 10 for values between 1,000 and 2,500, or nearest 5 otherwise.

EI (lb-ft²/ft) and GA (lb/ft)—Nearest 10⁶ for values greater than 10⁶, nearest 10⁵ for values between 10⁵ and 10⁶, or nearest 10⁴ otherwise.

Bending Members- Flexure Design Example

Given:

16.5 ft span

38 psf dead load, 40 psf live load

Assume:

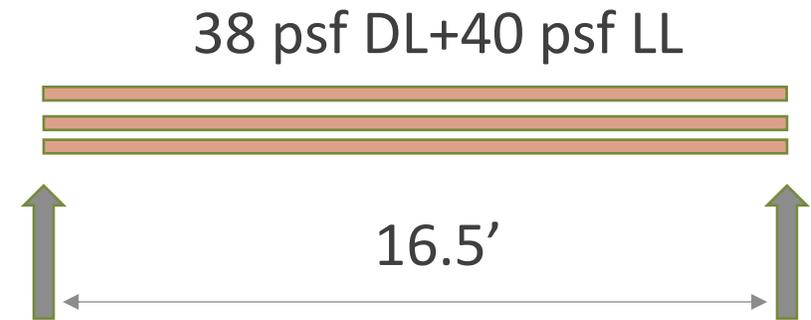
one span along major axis of CLT

Analysis based on 1 ft width

Calculate:

ASD dead + live load applied moment

$$M_b = wL^2/8 = (38+40 \text{ psf}) (16.5 \text{ ft})^2/8 = 2,655 \text{ lb-ft/ft}$$



Bending Members- Flexure Design Example

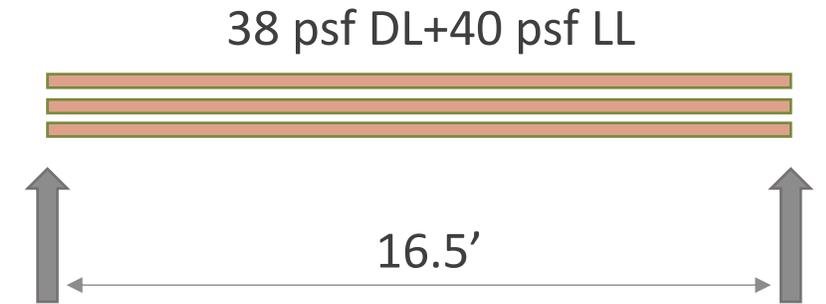
CLT GRADE	MAJOR LAYER	WEIGHT lb/ft ²	MAJOR STRENGTH DIRECTION					MINOR STRENGTH DIRECTION				
			$F_b S_{eff,0}$ (lb-ft/ft)	$EI_{eff,0}$ (10 ⁶ lb-ft ² /ft)	$GA_{eff,0}$ (10 ⁶ lb-ft/ft)	$M_{allow,0}$ (lb-ft/ft)	$V_{allow,0}$ (lb-ft/ft)	$F_b S_{eff,90}$ (lb-ft/ft)	$EI_{eff,90}$ (10 ⁶ lb-ft ² /ft)	$GA_{eff,90}$ (10 ⁶ lb-ft/ft)	$M_{allow,90}$ (lb-ft/ft)	$V_{allow,90}$ (lb-ft/ft)
V2.1	87 V	7.5	1444	56	0.5	1444	1220	37	0.4	0.30	32	240
	139 V	11.9	3329	206	1.0	3329	1770	537	21	0.60	457	850
	191 V	16.3	5917	503	1.4	5917	2290	1216	83	0.91	1034	1080
	243 V	20.8	9212	995	1.9	9219	2800	2133	209	1.20	1814	1320
V2M1.1	105 V	9.0	2042	96	0.5	2042	1440	277	3.7	0.53	235	495
	175 V	15.0	4701	366	1.1	4701	1970	2403	96	1.10	2042	1440
	245 V	21.0	8315	906	1.6	8315	2500	5531	366	1.60	4701	1970
	315 V	27.0	12896	1806	2.1	12896	3025	9782	906	2.10	8315	2470

Choose 5-ply 6 7/8" (175mm) thick V2 panel,
 $F_b S_{eff,0} = 4,701 \text{ lb-ft/ft}$

Bending Members- Flexure Design Example

$$M_b \leq (F_b S_{\text{eff}})' \quad \leftarrow \quad \text{Adjusted Bending Strength}$$

$$M_b \leq \underbrace{C_D C_M C_t C_L}_{\text{Per NDS}} (F_b S_{\text{eff}})$$



$$M_b = 2,655 \text{ lb-ft/ft} \leq (1.0) (1.0) (1.0) (1.0) 4,701 \text{ lb-ft/ft}$$

$$M_b = 2,655 \text{ lb-ft/ft} \leq 4,701 \text{ lb-ft/ft}$$

Flexure Strength is OK!

Flatwise Shear Strength

Design Properties based on Extreme Fiber Model:

Shear Capacity Check:

$$V_a \leq F_s (Ib/Q)_{\text{eff}}'$$

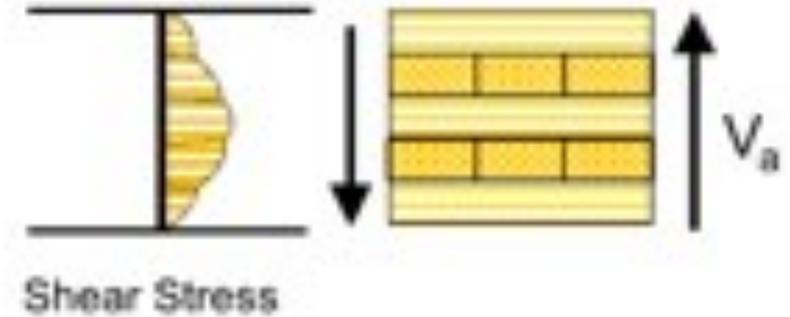
V_a = applied shear

$F_s (Ib/Q_{\text{eff}})'$ = adjusted shear strength

From Strength of Materials

$$v_s = \frac{V Q}{I t}$$

$$V = \frac{v_s I t}{Q}$$



Flatwise Shear Strength

$$(Ib/Q)_{eff} = \frac{EI_{eff}}{\sum_{i=1}^{n+2} E_i h_i z_i}$$

Non-homogeneous, anisotropic material

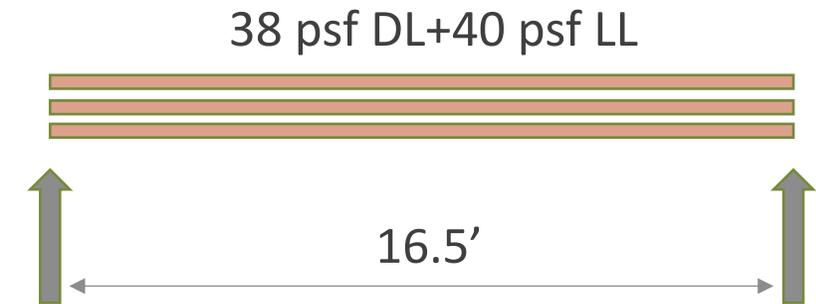
where:

EI_{eff} = Effective bending stiffness

E_i = Modulus of elasticity of an individual layer

h_i = Thickness of an individual layer, except the middle layer, which is half its thickness

z_i = Distance from the centroid of the layer to the neutral axis, except for the middle layer, where it is to the centroid of the top half of that layer.



Flatwise Shear Strength

$$V_{planar} \leq F'_v (Ib / Q)_{eff} \quad [4]$$

where:

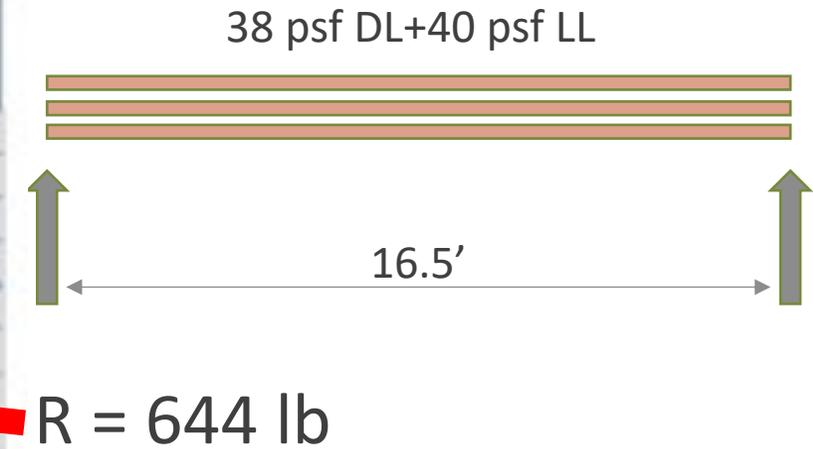
V_{planar} = induced shear due to loads

$F'_v (Ib/Q)_{eff}$ = shear strength of the panel provided by the manufacture or calculated per the simplified method multiplied by the applicable adjustment factors.

$$V_{planar} \leq C_d C_m C_t (F_s (IbQ)_{eff})$$

Flatwise Shear Strength

CLT GRADE	MAJOR LAYER	WEIGHT lb/ft ²	MAJOR STRENGTH DIRECTION					MINOR STRENGTH DIRECTION				
			F_s _{allow} (lb-ft ² /ft)	EI _{allow} (10 ⁶ lb-ft ² /ft)	GA _{allow} (10 ⁶ lb/ft)	M _{allow} (lb-ft/ft)	V _{allow} (lb/ft)	F_s _{allow} (lb-ft ² /ft)	EI _{allow} (10 ⁶ lb-ft ² /ft)	GA _{allow} (10 ⁶ lb/ft)	M _{allow} (lb-ft/ft)	V _{allow} (lb/ft)
V2.1	87 V	7.5	1444	56	0.5	1444	1220	37	0.4	0.30	32	240
	139 V	11.9	3329	206	1.0	3329	1770	537	21	0.60	457	850
	191 V	16.3	5917	503	1.4	5917	2290	1216	83	0.91	1034	1080
	243 V	20.8	9212	995	1.9	9219	2800	2133	209	1.20	1814	1320
V2M1.1	105 V	9.0	2042	96	0.5	2042	1440	277	3.7	0.53	235	495
	175 V	15.0	4701	366	1.1	4701	1980	553	96	1.10	2042	1440
	245 V	21.0	8315	906	1.6	8315	2500	5531	366	1.60	8315	1970
	315 V	27.0	12896	1806	2.1	12896	3025	9782	906	2.10	8315	2470



Choose 5-ply 6 7/8" (175mm) thick V2 panel

$$V_{\text{allow}} = 1,980 \text{ lb} > 644 \text{ lb} \quad \text{OK!}$$

Flatwise Flexural Stiffness (Deflection)

- Bending Stiffness
- Shear Stiffness

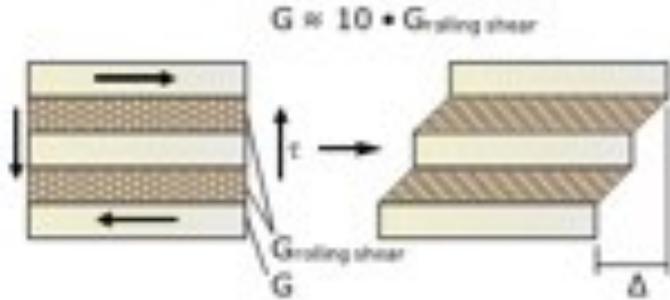
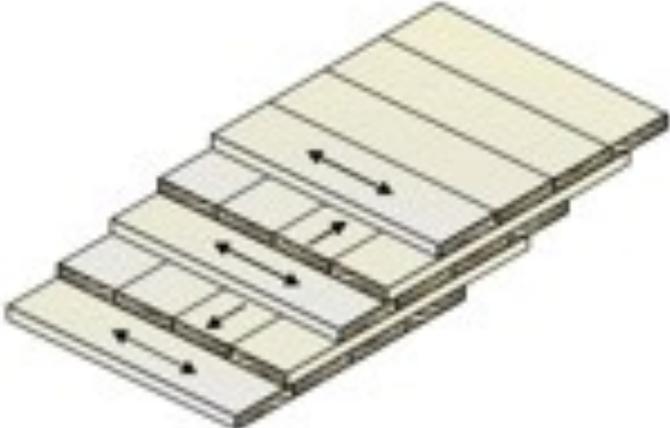
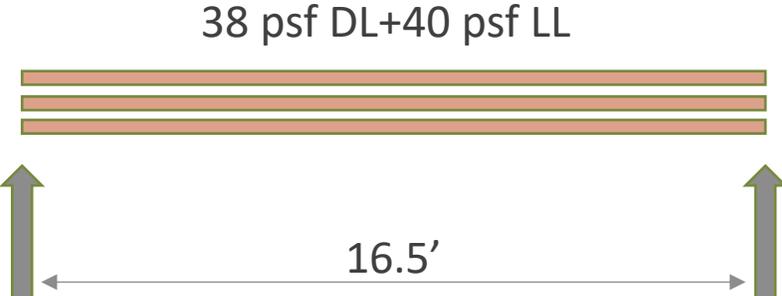


Figure 1
Rolling shear deformation of a 5-layer CLT panel



$R = 644 \text{ lb}$

G = Shear Modulus

Flatwise Flexural Stiffness (Deflection)

Using Shear Analogy Method

$$\Delta_{\max} = \frac{5}{384} \cdot \frac{wL^4}{EI_{\text{eff}}} + \frac{1}{8} \cdot \frac{wL^2 k}{GA_{\text{eff}}}$$

Because Shear deflections can be a significant in CLTs, adjust the effective bending stiffness to an apparent bending stiffness.

$$EI_{\text{app}} = \frac{EI_{\text{eff}}}{1 + \frac{K_s EI_{\text{eff}}}{GA_{\text{eff}} L^2}}$$

K_s = constant based on loading and end conditions per Table 2, Chapter 3 CLT Handbook (simple, pinned $K_s = 11.5$)

Deflection Under Long-Term Loading

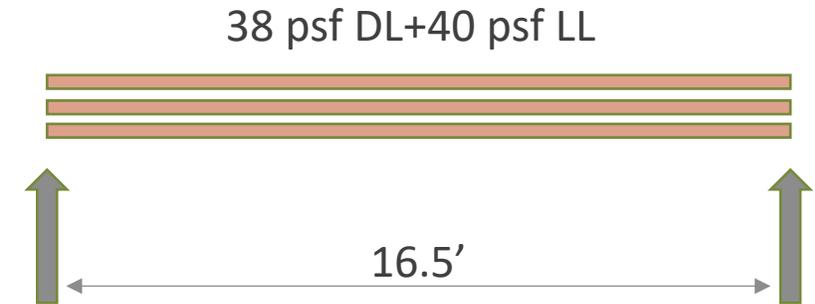
Design Example

$$\Delta_{\max} = \frac{5}{384} \cdot \frac{wL^4}{EI_{\text{app}}}$$

$$\Delta_{\text{DL}} = \text{from } 38 \text{ psf} = 0.19 \text{ in}$$

$$\Delta_{\text{LL}} = \text{from } 40 \text{ psf} = 0.20 \text{ in}$$

$$\Delta_{\max} = (.19) + (.20) = 0.39 \text{ in } (L/507)$$



Deflection Under Long-Term Loading

$$\Delta_T = K_{cr} \Delta_{LT} + \Delta_{ST}$$

K_{cr} = Time Dependent Creep Factor, 2.0 for dry service CLT

Δ_{LT} = Immediate Deflection Due to Long Term Component of load

Δ_{ST} = Deflection due to Short Term or Normal Component of load

$$\Delta_T = 2.0 (\Delta_{LT}) + (\Delta_{ST})$$

Deflection Under Long-Term Loading

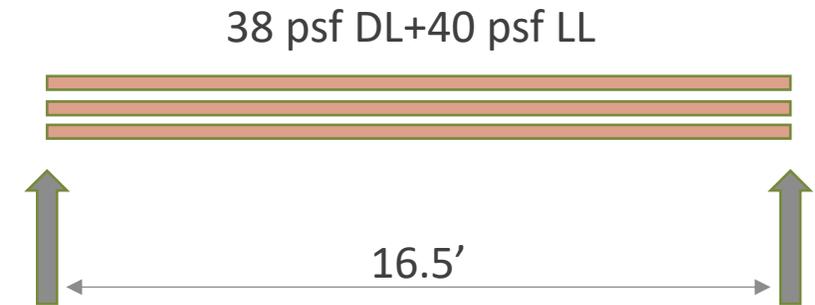
Design Example

$$\Delta_{\text{max}} = \frac{5}{384} \cdot \frac{wL^4}{EI_{\text{app}}}$$

$$\Delta_{\text{LT}} = \text{from } 38 \text{ psf} = 0.19 \text{ in}$$

$$\Delta_{\text{ST}} = \text{from } 40 \text{ psf} = 0.20 \text{ in}$$

$$\Delta_{\text{total}} = 2.0 (0.19) + (0.20) = 0.58 \text{ in } (L/341)$$



Floor Vibration

Occupant perception of vibration is significant design consideration,
Human sensitivity to vibration @ frequency between 4 – 8Hz

Natural Frequency not best measure of vibration performance; accelerations felt is better measure but difficult to calculate accurately given the variability of inputs esp, damping

Vibration response to footfall is dependent on natural frequency and damping

Mass Timber Floors – 2.5% to 3.5% modal damping

Ignore composite action of concrete topping unless floor designed and detailed as such

Simplified Analysis per CLT Handbook, AISC Design Guide 11, CSA 086 Annex A, ISO 10137

Floor Vibration

Human sensitivity to Vibration - frequency between 4 – 8Hz

One approach: US CLT Handbook, Chapter 7 (FPI Method)

Calculated natural frequency of simple span of bare CLT:

$$f = \frac{2.188}{2l^2} \sqrt{\frac{EI_{app}}{\rho A}}$$

Where:

EI_{app} = apparent stiffness for 1 foot strip, pinned supported, uniformly loaded, simple span ($K_s = 11.5$) (lb-in²)

ρ = specific gravity of the CLT

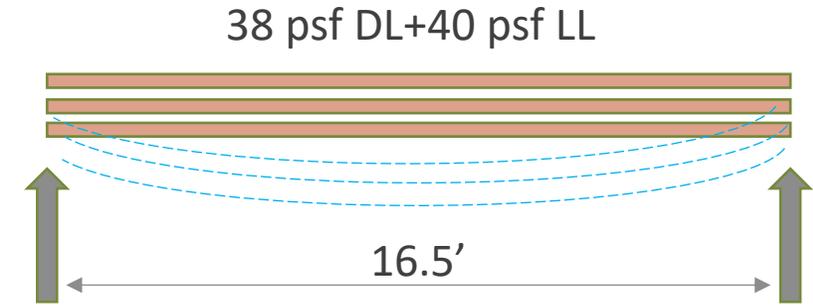
A = the cross section area (thickness x 12 inches) (in²)

Floor Vibration – Span Limitations

Human sensitivity to Vibration - frequency between 4 – 8Hz

FPI Method Floor Span Limitations

Frequency $f > 9.0$ Hz



$$\text{Span } L \leq \frac{1}{12.05} \frac{(EI_{app})^{0.293}}{(\rho A)^{0.122}}$$

$$EI_{app} = \frac{EI_{eff}}{1 + \frac{K_s EI_{eff}}{GA_{ex} L^2}}$$

Using Spreadsheet and Iterate

1. Estimate L
2. Calculate EI_{app}
3. Calculate L limit
4. Repeat until convergence

Floor Vibration Controlled Span - Example

- Grade = E1
- Thickness = 6 7/8 in. (0.175 m)
- Specific gravity = 0.56 (560.66 kg/m³)
- $EI_{eff} = 440 \times 10^6 \text{ lb.-in.}^2/\text{ft.}$ ($4.140 \times 10^6 \text{ N-m}^2/\text{m}$)
- $GA_{eff} = 0.92 \times 10^6 \text{ lb./ft.}$ ($1.343 \times 10^7 \text{ N/m}$)
- l = vibration controlled span (ft.)

$$EI_{app} = \frac{EI_{eff}}{1 + \frac{K_s EI_{eff}}{GA_{eff} L^2}} \quad l \leq \frac{1}{12.05} \frac{(EI_{app})^{0.293}}{(\rho A)^{0.122}}$$

Table 5

Excel calculation for the example

Thickness (in.)	Trial Span (ft.)	EI_{eff} ($\times 10^6 \text{ lb.-in.}^2/\text{ft.}$)	GA_{eff} ($\times 10^6 \text{ lb./ft.}$)	EI_{app} Equation [5] ($\times 10^6 \text{ lb.-in.}^2/\text{ft.}$)	Specific Gravity	New Span Equation [4] (ft.)
6.875	17.188	440	0.92	389.5	0.56	17.10
6.875	17.100	440	0.92	389.1	0.56	17.09
6.875	17.090	440	0.92	389.0	0.56	17.09

FPI Vibration Span Limits for Std Grades / Layups

Grade	Layup	Thickness	FPI Span Limit
E1	3ply	4 1/8"	12' 5"
	5ply	6 7/8"	17' 4"
	7ply	9 5/8"	21' 8"
E2	3ply	4 1/8"	12' 0"
	5ply	6 7/8"	16' 8"
	7ply	9 5/8"	20' 10"
E3	3ply	4 1/8"	11' 7"
	5ply	6 7/8"	16' 1"
	7ply	9 5/8"	20' 1"
E4	3ply	4 1/8"	12' 2"
	5ply	6 7/8"	17' 0"
	7ply	9 5/8"	21' 3"

Grade	Layup	Thickness	FPI Span Limit
V1	3ply	4 1/8"	12' 2"
	5ply	6 7/8"	17' 0"
	7ply	9 5/8"	21' 3"
V2	3ply	4 1/8"	11' 11"
	5ply	6 7/8"	16' 8"
	7ply	9 5/8"	20' 10"
V3	3ply	4 1/8"	12' 0"
	5ply	6 7/8"	16' 9"
	7ply	9 5/8"	21' 0"

- These are approximate only!
- Verify based on manufactures properties
- Verify based on project specifics
- Check strength and deflection

Floor Vibration

4.4 CLT Floor with a Heavy Topping [$>20 \text{ lb./ft.}^2$ (100 kg/m^2)]

It is known that without a suspended ceiling, a heavy topping is normally necessary for CLT floor to achieve the satisfactory airborne and impact sound insulation. The heavy topping adds significant mass to the floor system, and reduces the fundamental natural frequency to below 9 Hz. Based on the experience of the authors, even though the topping increases the floor stiffness, the low first natural frequency makes the floor susceptible to annoying vibrations (Hu, 2007). For lightweight wood-joisted floor systems, the design method requires to reduce the spans of the joisted floors after a heavy cementitious topping is added (Hu, 2007). A similar approach should be applied to CLT floors with a heavy topping. As an interim measure, it is recommended that the span be calculated using equation [4] for vibration controlled design of such heavy topping CLT floor system, assuming the bare CLT floor mass and stiffness be reduced by 10%. This interim recommendation will be further refined through laboratory study.

Recommendation seems conservative

Mass Timber Floor Vibration Guide coming 2020 – more specific design info

Two-Way Action

Flexure

- Manufactures provide flexure and shear capacity in both major axis
- NDS 2018 Chapter 10 (CLT) - Adjustment factors to check capacity against the design code using ASD / LRFD design checks
- NDS 2018 C3.9.2-2 could check the combined loading condition - very conservative approach
- Laminations in orthogonal directions share load based upon their relative stiffness
- Treat the major / minor direction flexural and shear checks independently. This is the common state of practice in European design

Two-Way Action

Bearing Capacity at Supports

NDS 2018 Chapter 10 includes design provisions for the bearing capacity of CLT panels to loads on the surface

Local Punching Shear at Supports

This limit state is critical for point supported CLT panels.

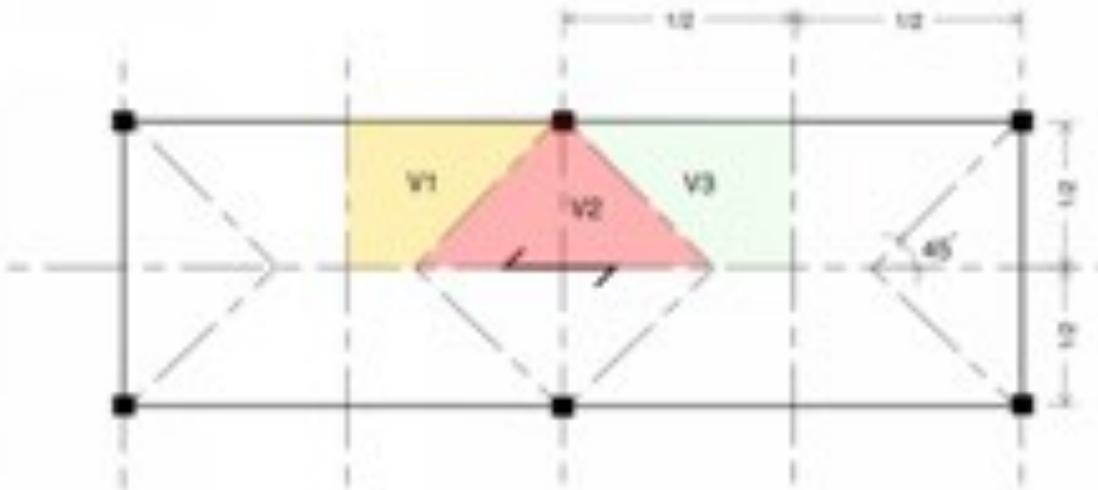


Figure 5: Plan View of CLT Panel – Shear Approximation

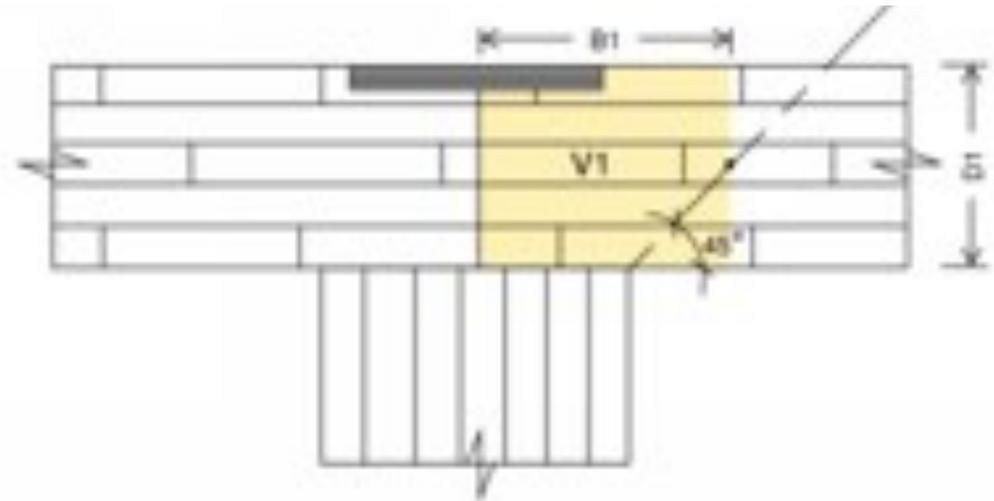
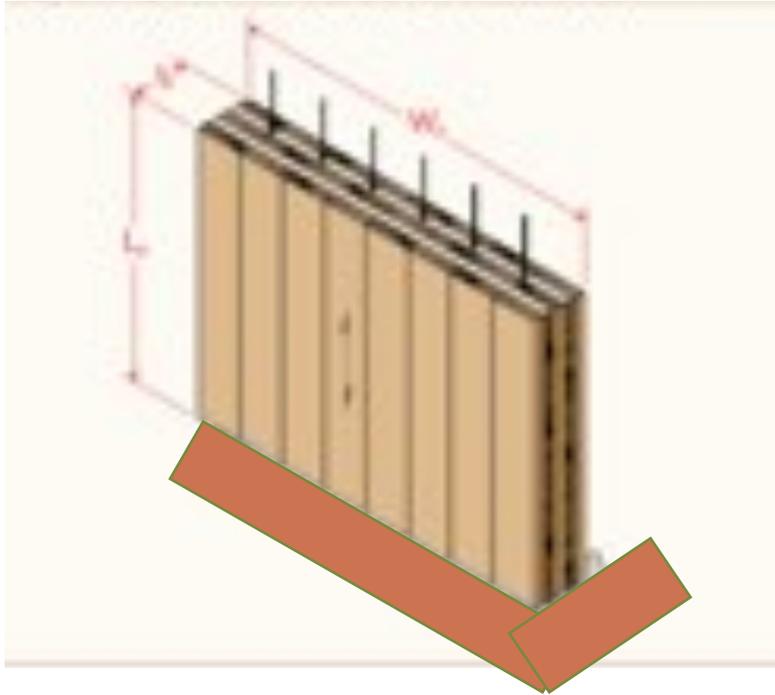


Figure 6: V1 or V3 Shear Area

Bearing Walls



$$P_{parallel} \leq F'_c A_{parallel}$$

where:

$P_{parallel}$ = Load applied parallel to the direction of the fibers

F'_c = Adjusted compression strength

$A_{parallel}$ = Area of layers with fibers running parallel to the direction of the load

$$F'_c A_{parallel} = F_c * A_{parallel} = F_c C_p A_{parallel}$$

Bearing Walls

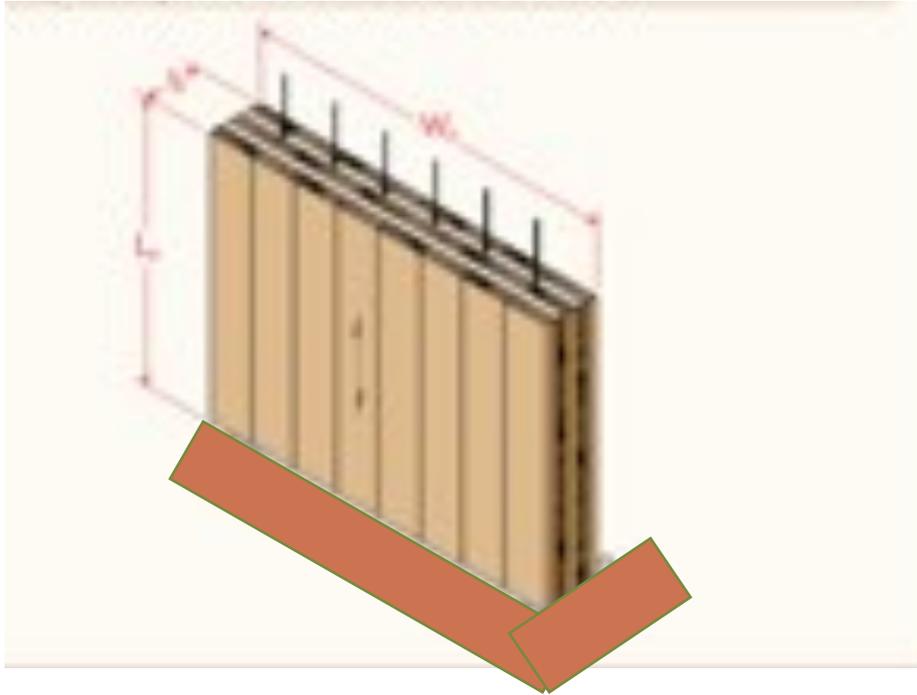


Image: PRG 320-2018

$$C_p = \frac{1 + (F_{ax}/F_c^*)}{2c} - \sqrt{\left[\frac{1 + (F_{ax}/F_c^*)}{2c} \right]^2 - \frac{F_{ax}/F_c^*}{c}} \quad (3.7-1)$$

where:

F_c^* = reference compression design value parallel to grain multiplied by all applicable adjustment factors except C_p (see 2.3), psi

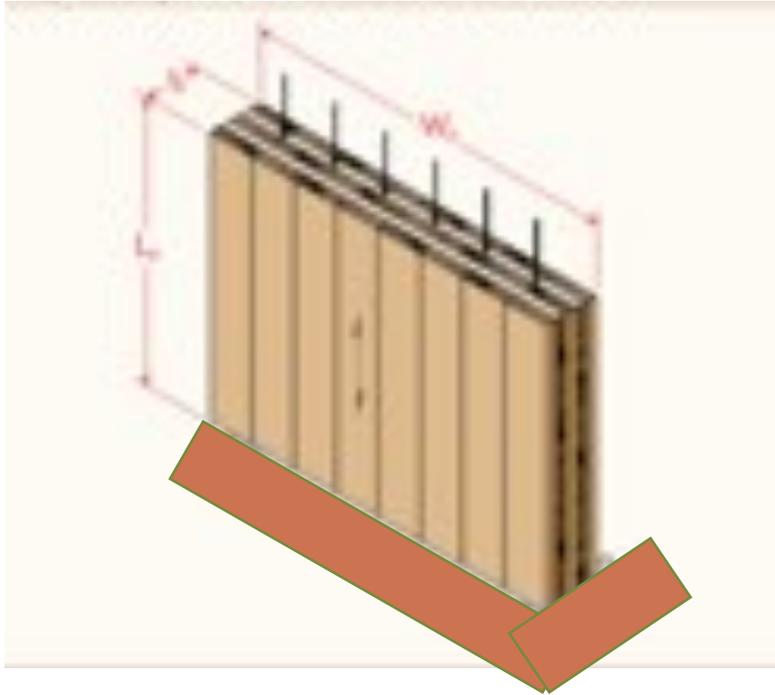
$$F_{ax} = \frac{0.822 E_{min}'}{(l_e/d)^2}$$

$c = 0.8$ for sawn lumber

$c = 0.85$ for round timber poles and piles

$c = 0.9$ for structural glued laminated timber, structural composite lumber, and cross-laminated timber

Bearing Walls



$$C_p = \frac{1 + (P_{dE} / P_c^*)}{2c} - \sqrt{\left[\frac{1 + (P_{dE} / P_c^*)}{2c} \right]^2 - \frac{P_{dE} / P_c^*}{c}}$$

where:

P_c^* = Composite compression design capacity ($F_c^* A$) where F_c^* is multiplied by all applicable adjustment factors except C_p

c = 0.9 for CLT

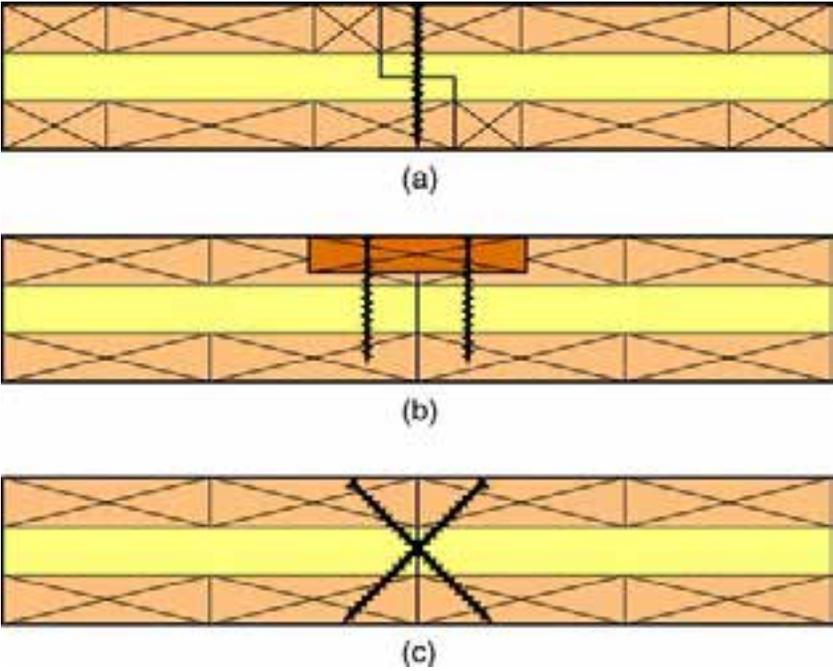
P_d = $\frac{\pi^2 EI'_{app-min}}{l_e^2}$ (see Section 2.2.3).

$$EI_{app-min} = 0.5184 EI_{app}$$

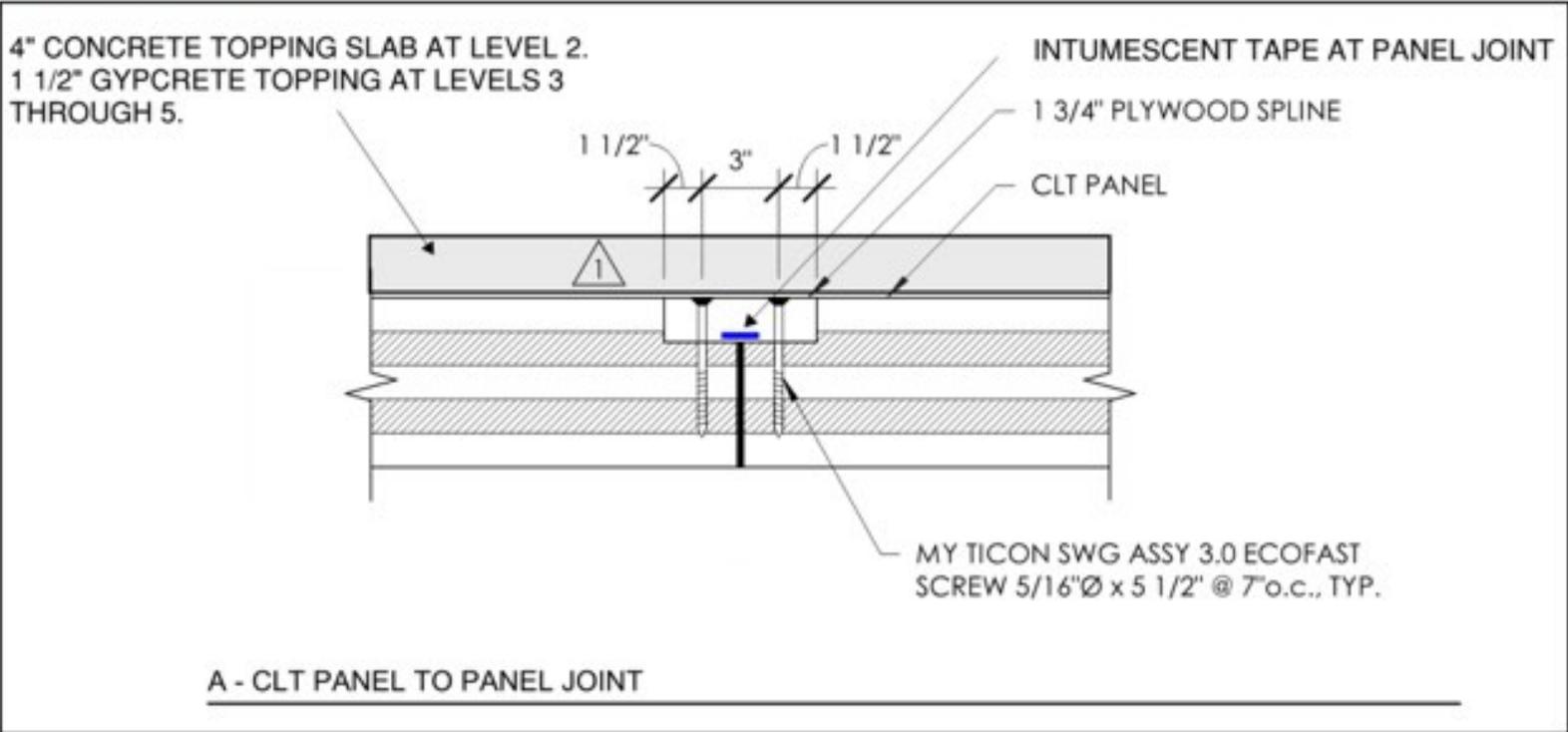
$$P_{parallel} \leq P_c C_p A_{parallel}$$

Connections

Panel to Panel at floors, walls and roof

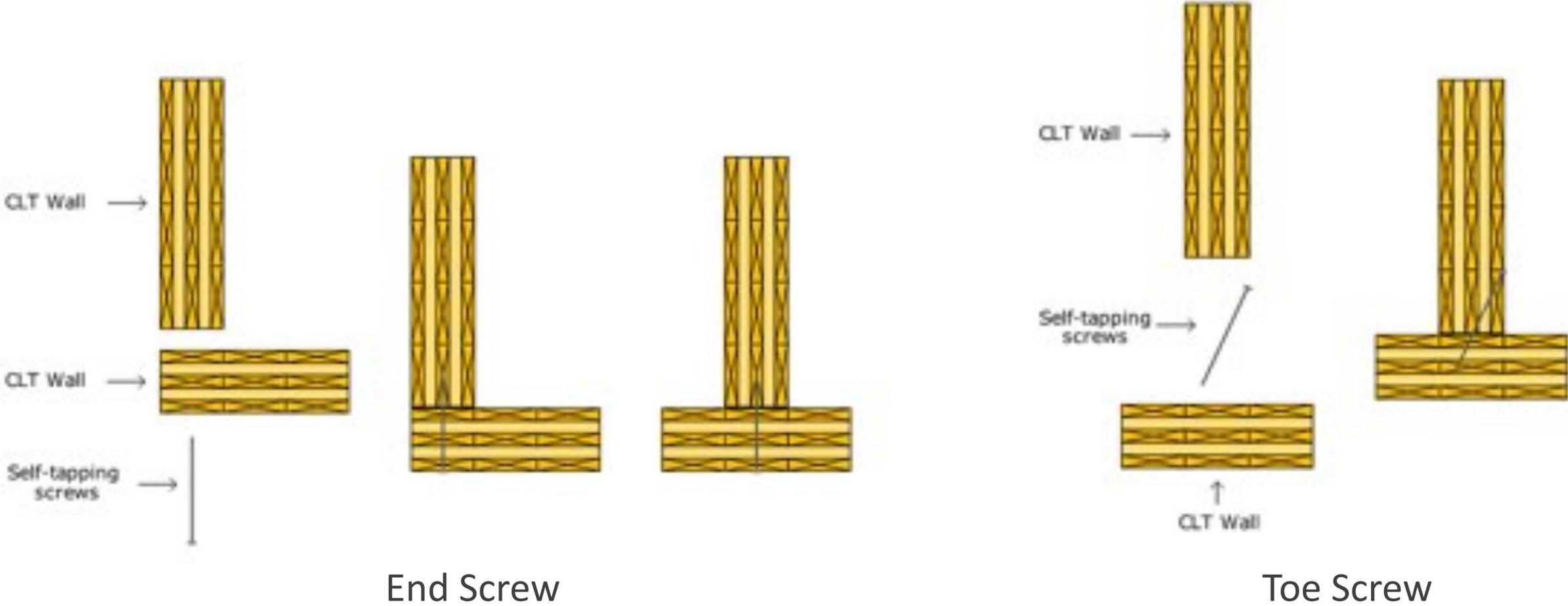


Proposed Design



Connections

Wall to Wall

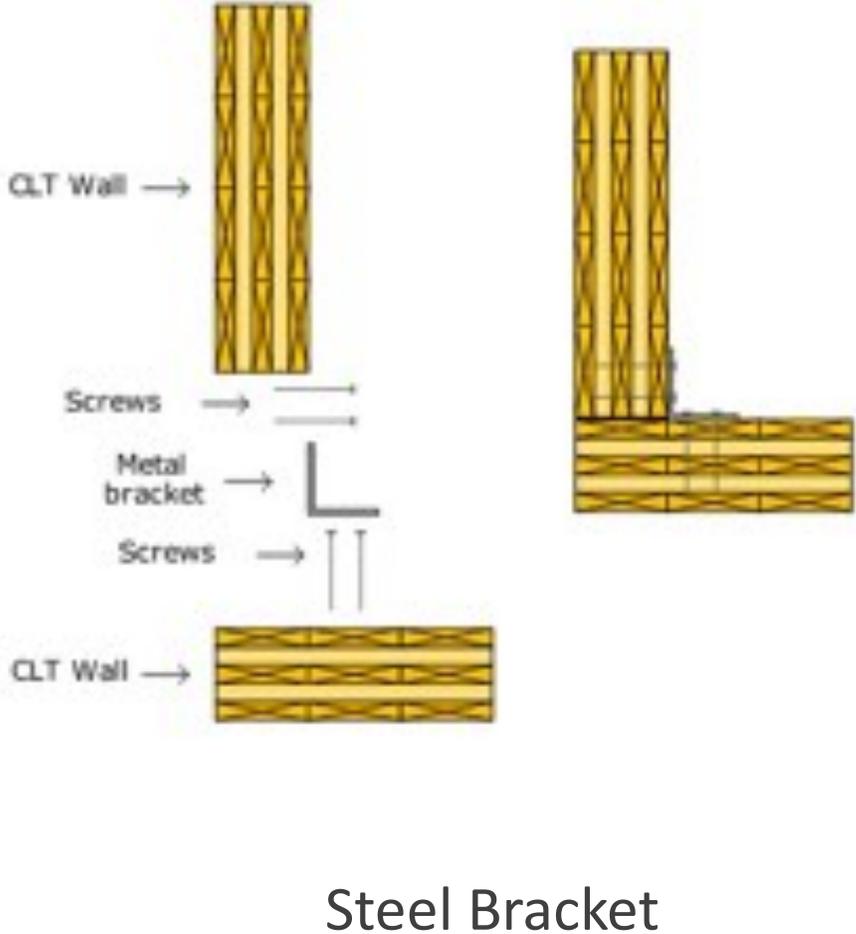
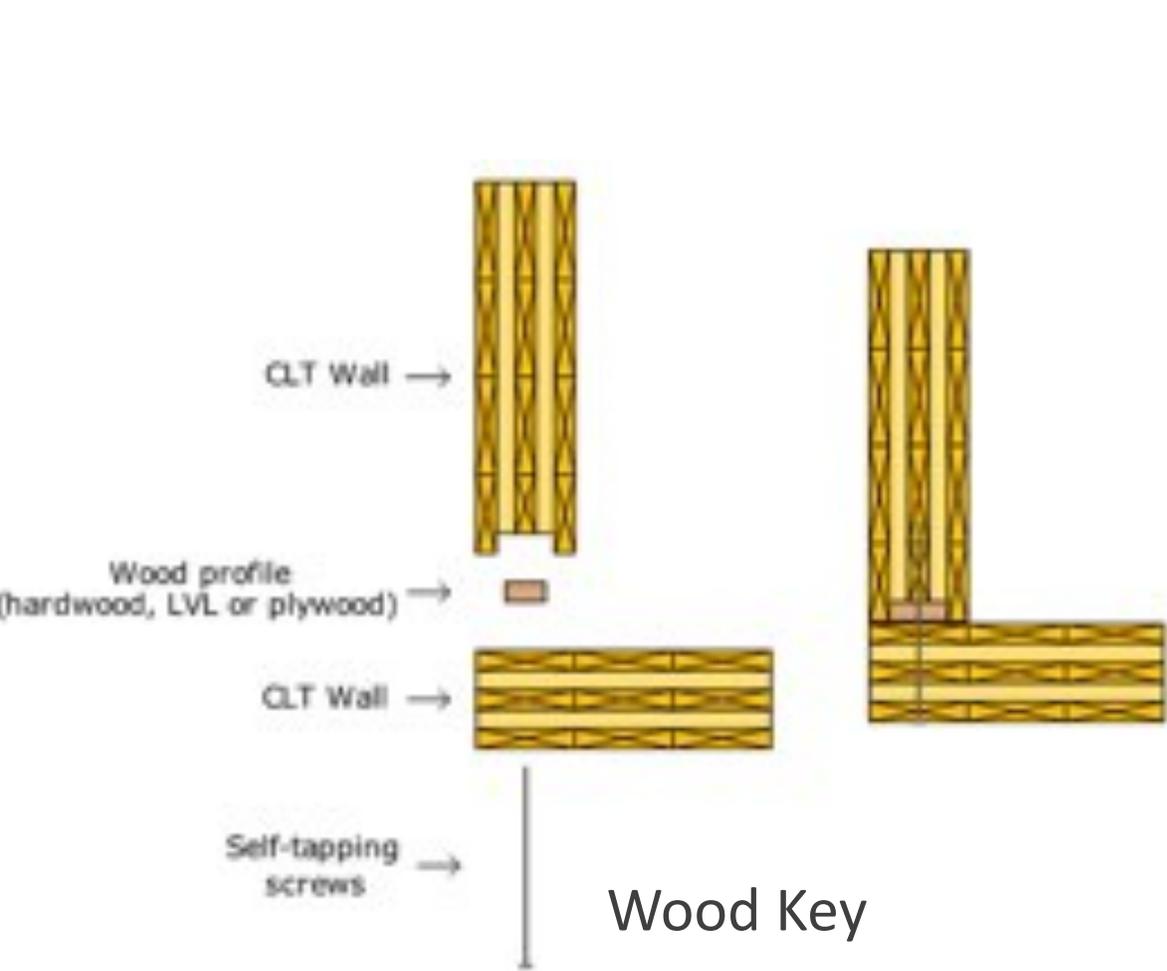


End Screw

Toe Screw

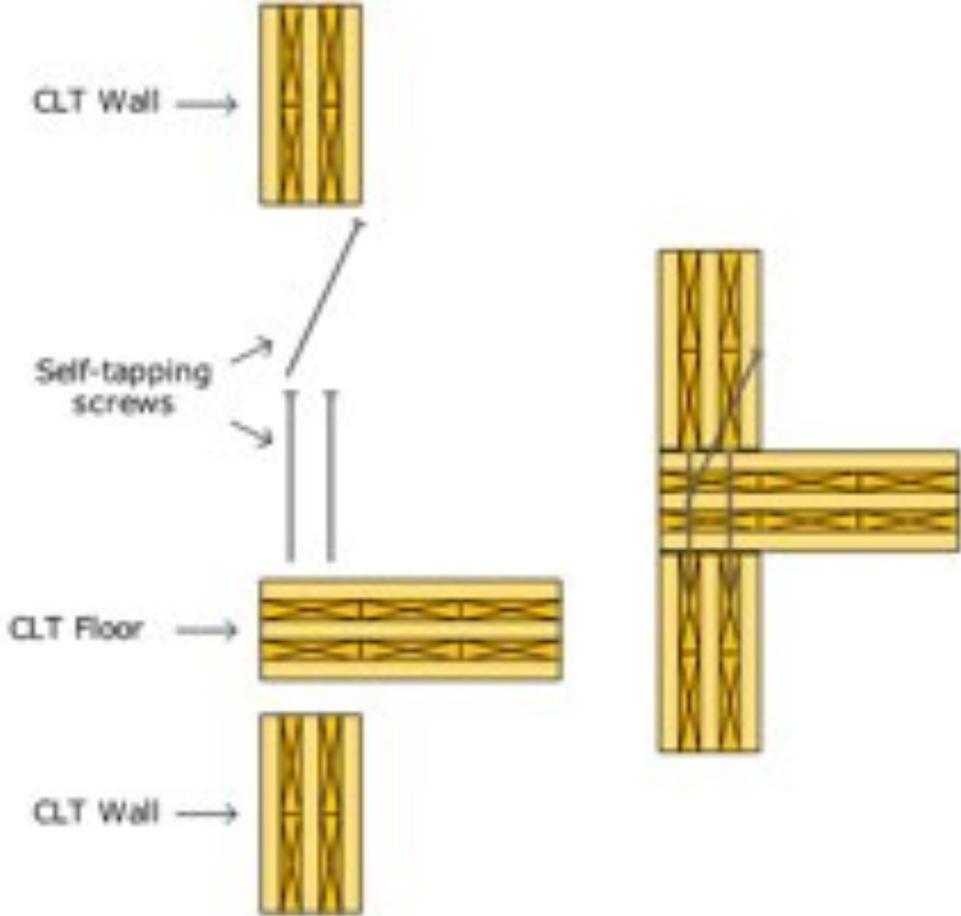
Connections

Wall to Wall

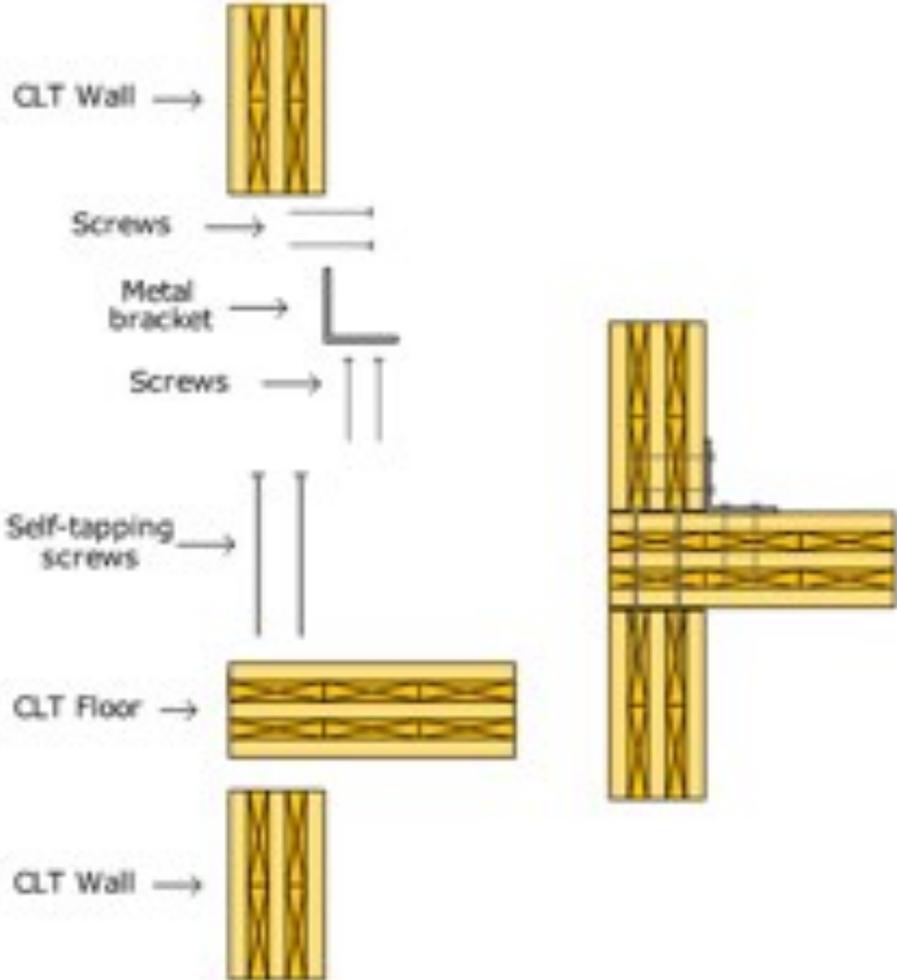


Connections

Wall to Wall



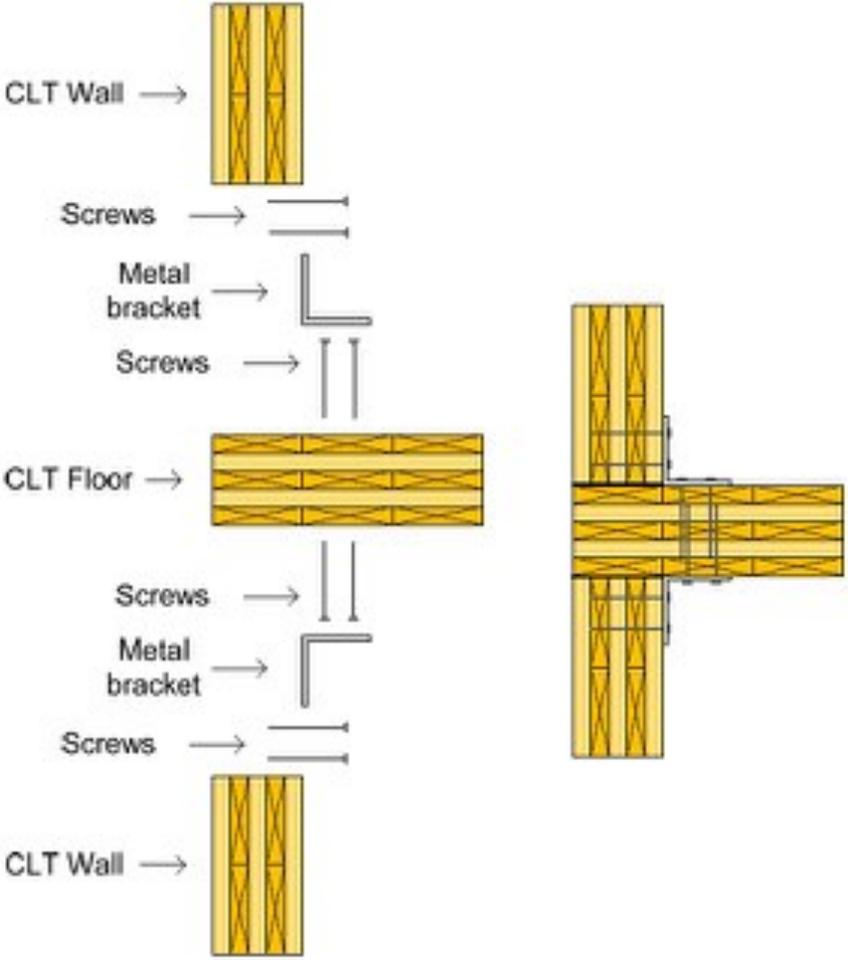
End Screw, Toe Screw



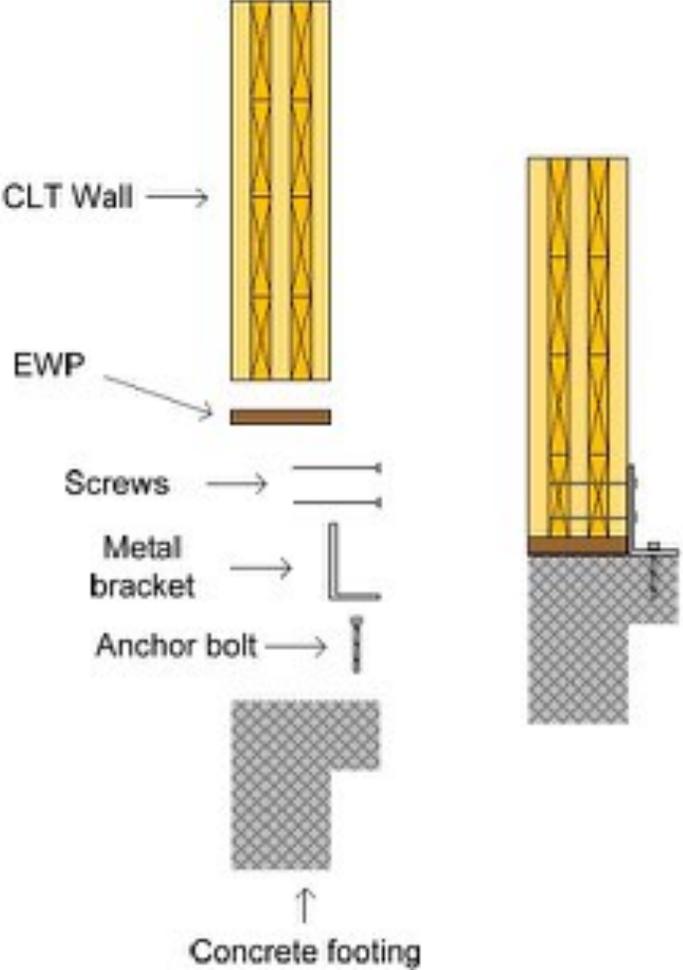
Steel Bracket

Connections

Panel to Panel at floors, walls and roof



Double Steel Bracket



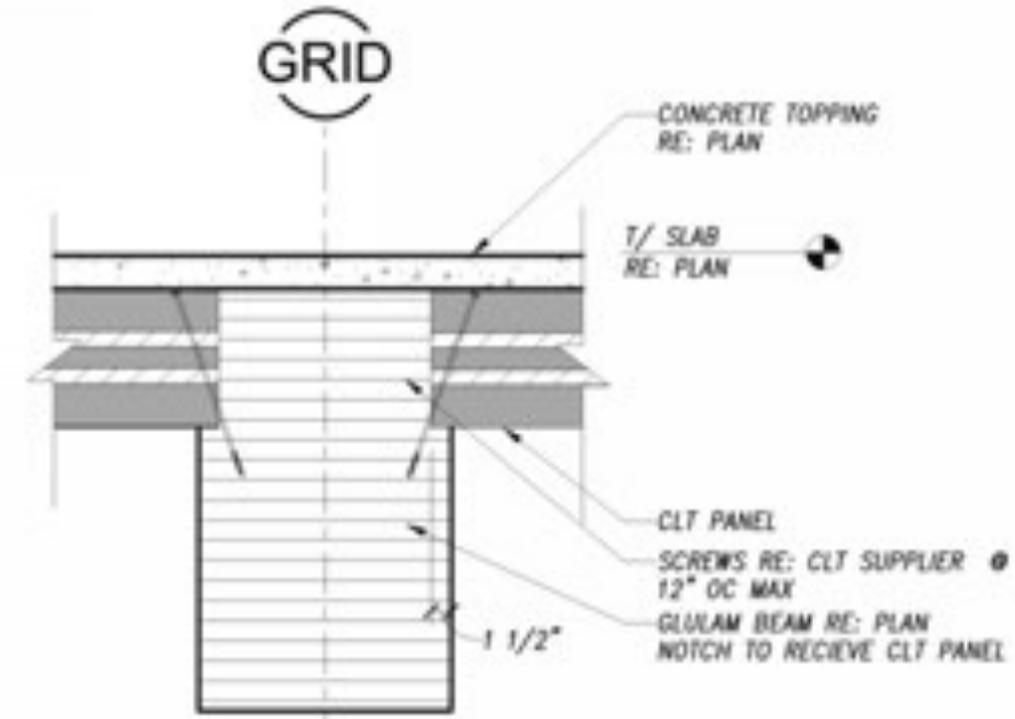
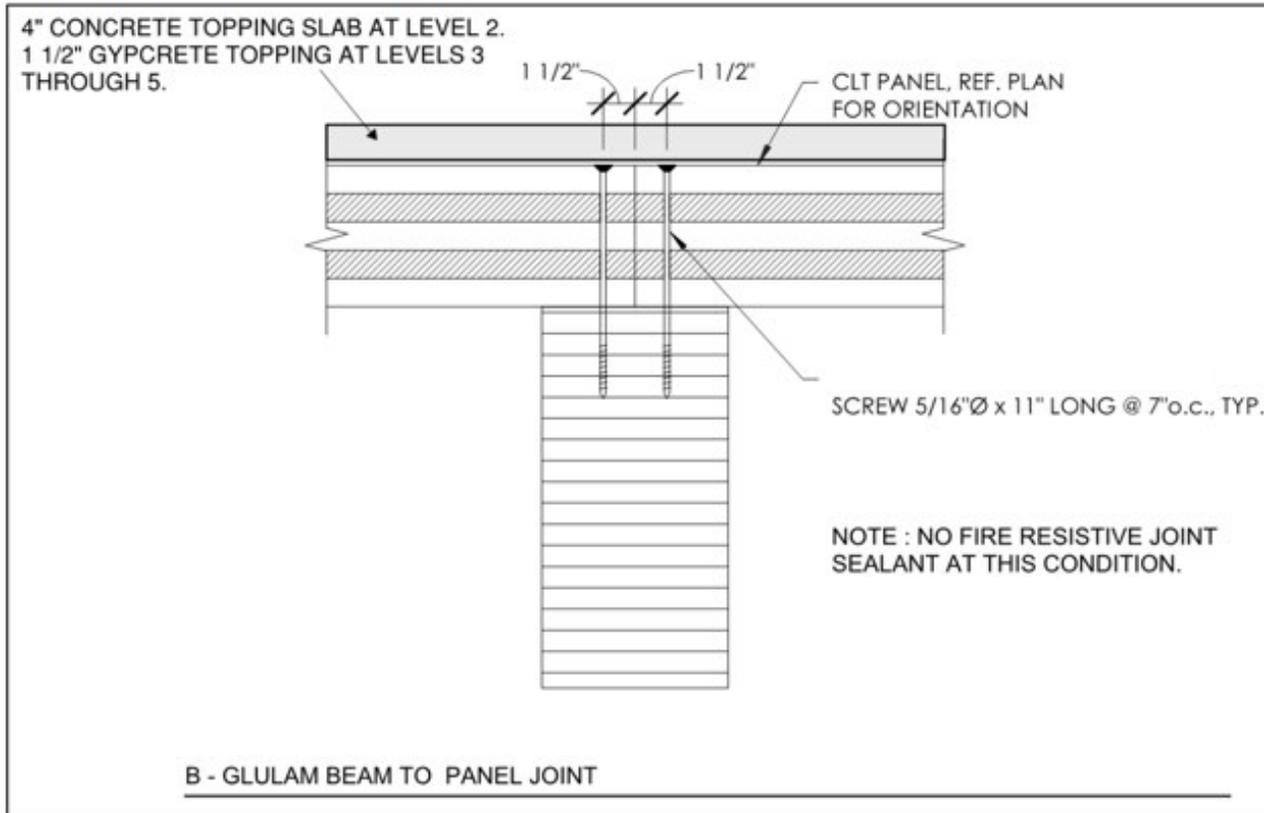
Steel Bracket

reference: CLT Handbook Chapter 5

Connections

Panel to GLB

Glulam beam to panel joint



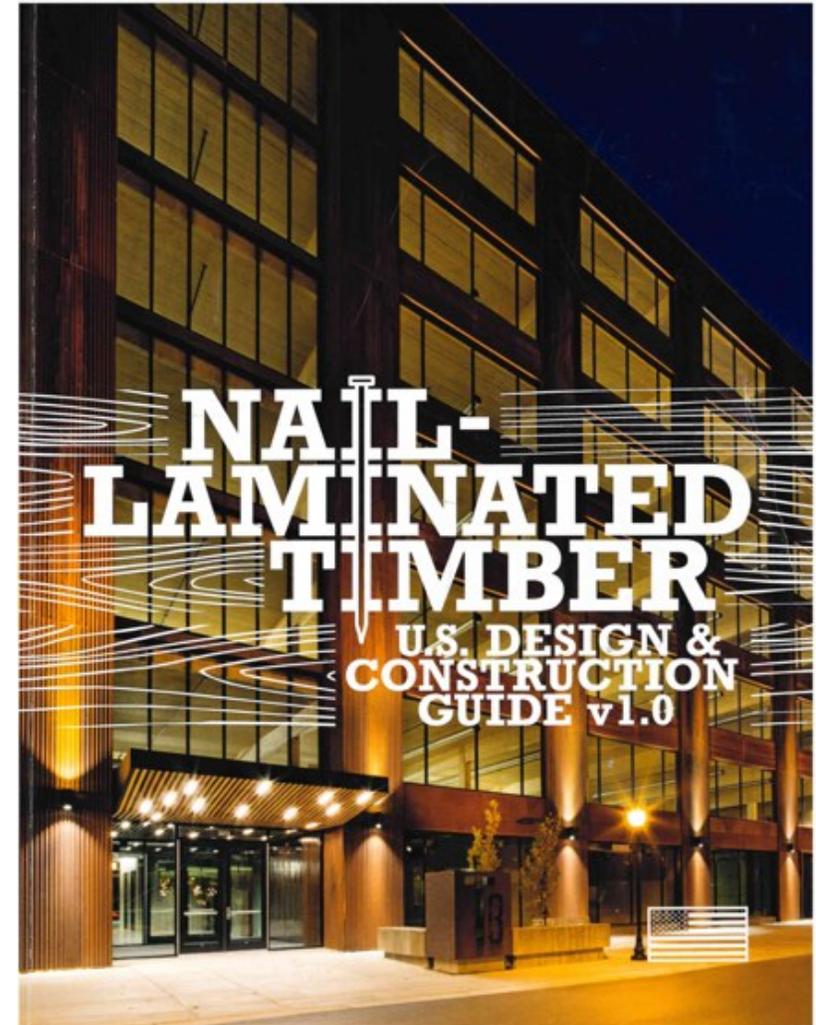
CLT TO INTERIOR BEAM CONNECTION

Mass Timber Products - NLT



1/2" (12.5mm)
1" OR 2" LAMINATION
GAP TO BE FILLED IN AFTER
BUILDING IS ENCLOSED
GLUE OR FINISH

2 SHRINKAGE / SWELLING GAP
TYP. GRIDS B, C, F AND G ONLY
1:10



download -rethinkwood.com

NLT Design

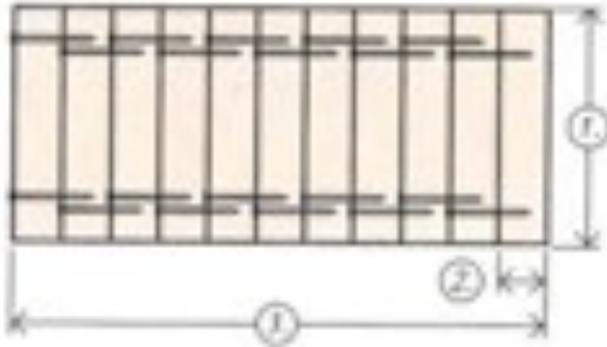


Figure 4.1: NLT Cross Section

Key

1. NLT depth (d)
2. Lamination thickness (b_{lam})
3. NLT panel width (b)

Treat NLT as built-up beam per NDS provisions

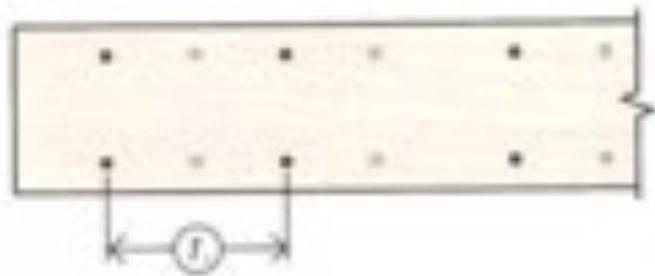
Beam Stability Factor (C_L) = 1

Size factor (C_F) based on individual lam thickness (b_{lam})

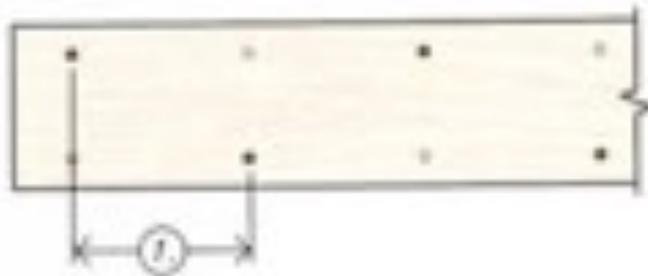
Repetitive Member (C_r) = 1.15

Layup Factor (K_{layup}) adjusts bending and stiffness

NLT Design



Two Rows



One Row

TABLE 4.6 MINIMUM LAMINATION NAILING

NLT TYPE	NLT DEPTH (NOMINAL)	NAILING PATTERN	
		3 in. long, 0.148 in. diameter nails (staggered)	3 in. long, 0.128 in. diameter nails (staggered)
Continuous Laminations	Less than 6 in.	One row @ 7 in. o.c.	One row @ 5 in. o.c.
	More than 6 in.	Two rows @ 14 in. o.c.	Two rows @ 10 in. o.c.
Butt-Jointed Laminations*	Less than 6 in.	One row @ 7 in. o.c.	One row @ 5 in. o.c.
	More than 6 in.	Two rows @ 10 in. o.c.	Two rows @ 10 in. o.c.

Note: Nails are smooth shank galvanized steel nails.

*Provide two additional nails on each side of every butt joint.

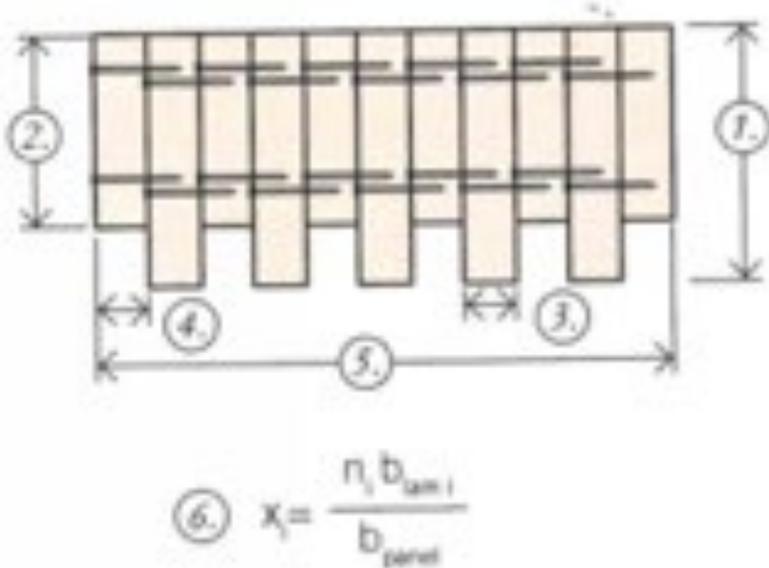
NLT Design – Butt Joints – (K_{layup})

TABLE 4.1: NLT LAYUP TYPES AND ADJUSTMENT FACTORS

LAYUP TYPE	
Laminations continuous and single span	
Laminations continuous and multi-span	
Laminations with controlled random butt joints over 4 or more supports	
Laminations with controlled random butt joints over fewer than 4 supports	

ADJUSTMENT FACTOR		NOTES
Bending Strength (K_{bend})	Stiffness (K_{stiff})	
$K_{bend} = 1.0$ $M = \frac{w\ell^2}{8}$	$K_{stiff} = 1.0$ $\Delta = \frac{5w\ell^4}{384E (d^3/12)}$	Maximum strength for a given depth. Typical maximum length for laminations of 16 to 20 feet. Longer laminations can be fabricated with structural finger joints (certified exterior joints or certified end joints).
$K_{bend} = 1.0$ $M = \frac{w\ell^2}{8}$	$K_{stiff} = 1.0$ $\Delta = \frac{w\ell^4}{185E (d^3/12)}$	Maximum strength and stiffness for a given depth. Typical maximum length for laminations of 16 to 20 feet. Longer laminations can be fabricated with structural finger joints (certified exterior joints or certified end joints).
$K_{bend} = 0.67$ $M = 0.10w\ell^2$	$K_{stiff} = 0.69$ $\Delta = \frac{0.0069w\ell^4}{E (d^3/12)}$	Maximum stiffness for a butt-jointed system. Rules for joint locations are given in IBC 2304.9.2.5 and 2304.9.3.3, and illustrated in the adjacent figure.
$K_{bend} = 0.202 \frac{(E/d)^{0.4}}{s^{1.6}}$ $M = \frac{w\ell^2}{8}$	for single span: $\Delta = \frac{5w\ell^4}{384E (d^3/12)}$ for double span: $\Delta = \frac{w\ell^4}{185E (d^3/12)}$	Based on European research, rules for joint locations per IBC should be amended as follows: <ul style="list-style-type: none"> Where butt joints occur in the same general line (±6 in.), they must be separated by a minimum of three intervening laminations. Each lamination must extend over a minimum of one support. See Section 4.3.1 for minimum nailing requirements.

NLT Design - Variable Depth Members (K_{section})



- Nails do not provide necessary stiffness for full composite
- All lams do not reach maximum bending capacity
- Deeper lams reach full capacity first
- Shallow lams reach only a portion of their capacity
- Based on relative stiffness

TABLE 4.2 STAGGERED NLT ADJUSTMENT FACTORS

STIFFNESS ($K_{\text{section},E}$)	BENDING ($K_{\text{section},b}$)	SHEAR ($K_{\text{section},v}$)
$K_{\text{section},E} = X_1 + X_2 \left[\frac{d_2}{d_1} \right]^3$	$K_{\text{section},b} = X_1 + X_2 \left[\frac{d_2}{d_1} \right]^3$	$K_{\text{section},v} = X_1$

NLT Design - Variable Depth Members (K_{section})

TABLE 4.3 BENDING DESIGN EQUATIONS

NLT STRESS	NLT CAPACITY
$f_b = \frac{6M}{b_{\text{panel}} d^2}$	$F_{b,NLT}' = F_b' K_{\text{layup},b} K_{\text{section},b}$

TABLE 4.4 SHEAR DESIGN EQUATIONS

NLT STRESS	NLT CAPACITY
$f_v = \frac{3V}{2b_{\text{panel}} d}$	$F_{v,NLT}' = F_v' K_{\text{section},v}$

Deflection

$$EI = E_{NLT}' I = E' K_{\text{layup},E} K_{\text{section},E} \frac{b_{\text{panel}} d^3}{12}$$

Glu-Lams

- Fabricated from conventional sawn lumber
- Laminations glued together to create a built-up beam
- Typically Southern Pine or Douglas Fir— high architectural quality

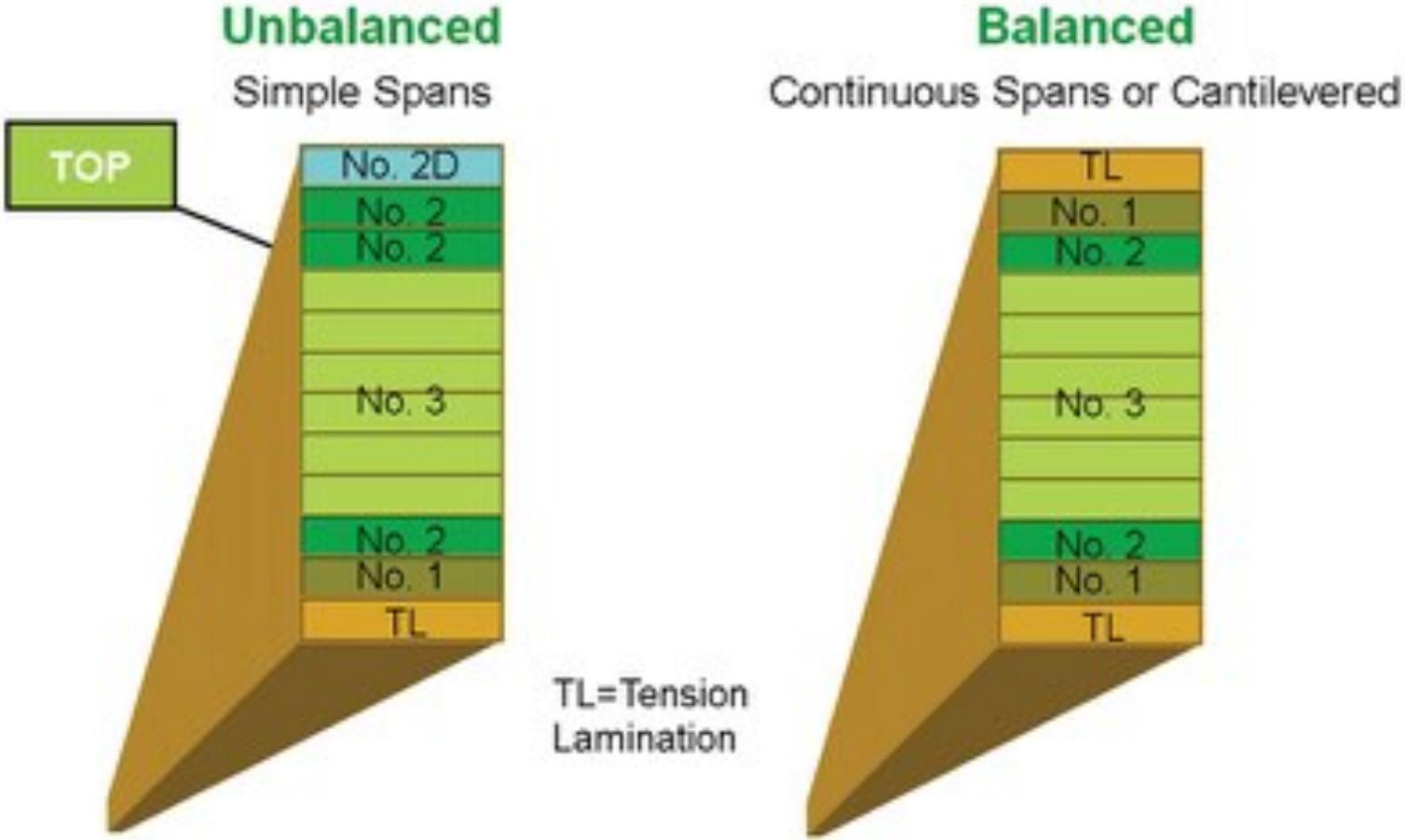


Glu-lams

- Specified by size, grade and finish (architectural versus industrial)
- Beam design
 - Unbalanced layup – 24F-V3 or 24F-1.8E
 - Higher grade laminations at bottom, weaker grade laminations at middle and top
 - Conventional layup - works for simple spans
 - Balanced layups – 24F-E4 or 24F-1.8E balanced
 - Same grade laminations at top and bottom
 - Cantilevers and continuous beams

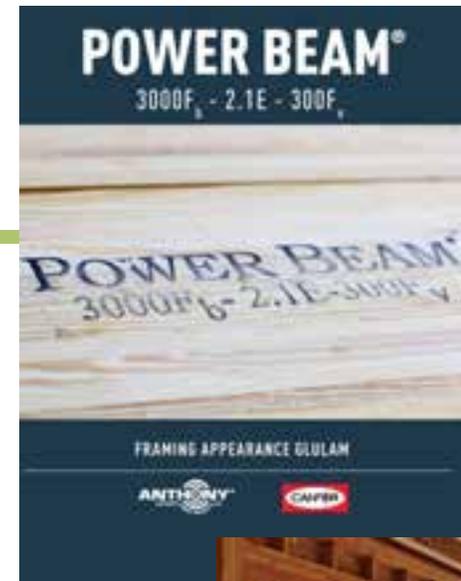
Glu-lams

Engineered Layups



Glulam – Manufacturer options

- “Off the shelf”
 - Stock beams: Power Beams by Anthony Forest Product, X-beam by Rosboro, etc..
 - Size up to 7”x28 7/8” (Anthony Powers); 8 3/4”x30” (Rosboro)
 - Available as architectural grade and treated for exterior
 - Connection made in the field
- Specialized manufacturer
 - High quality, custom product: Unalam, CLT list of Manuf
 - Shop fabricated, connection design, CNC
 - Curved!
 - Can be treated for exterior
 - Cost is a function of width - 2 beams cheaper?



Glulam Beams – Design (NDS Chapter 5)

- Values included for width (Table 5.1.3), Section Properties (Supplement Table 1C and 1D) and Reference Design Values (Supplement Table 5a)
- Check with local manufacturer



Table 5A Expanded - Reference Design Values for Structural Glued Laminated Softwood Timber Combinations¹ (Cont.) (Members stressed primarily in bending) (Tabulated design values are for normal load duration and dry service conditions. See NDS 5.3 for a comprehensive description of design value adjustment factors.)

Use with Table 5A Adjustment Factors

Combination Symbol	Species Outer/ Core	Bending About X-X Axis (Loaded Perpendicular to Wide Faces of Laminations)					Bending About Y-Y Axis (Loaded Parallel to Wide Faces of Laminations)					Axially Loaded		Fasteners			
		Bending		Compression Perpendicular to Grain		Shear Parallel to Grain	Modulus of Elasticity	Bending	Compression Perpendicular to Grain	Shear Parallel to Grain	Modulus of Elasticity	Tension Parallel to Grain	Compression Parallel to Grain	Specific Gravity for Fastener Design			
		Bottom of Beam Stressed in Tension (Positive Bending)	Top of Beam Stressed in Tension (Negative Bending)	Tension Face	Compression Face									For Deflection Calculations	For Stability Calculations	For Deflection Calculations	For Stability Calculations
		F_{bx}^+	F_{bx}^-	$F_{c\perp x}$		$F_{vx}^{(2)}$	E_x	$E_{x\ min}$	F_{by}	$F_{c\perp y}$	$F_{vy}^{(2)(3)}$	E_y	$E_{y\ min}$	F_t	F_c	G	
(psi)	(psi)	(psi)		(psi)	(10 ³ psi)	(10 ³ psi)	(psi)	(psi)	(psi)	(10 ³ psi)	(10 ³ psi)	(psi)	(psi)				
24F-1.8E		2400	1450	650		265	1.8	0.95	1450	560	230	1.6	0.85	1100	1600	0.50	
24F-V4	DF/DF	2400	1850	650	650	265	1.8	0.95	1450	560	230	1.6	0.85	1100	1650	0.50	0.50
24F-V8	DE/DE	2400	2400	650	650	265	1.8	0.95	1550	560	230	1.6	0.85	1100	1650	0.50	0.50
24F-E4	DF/DF	2400	1450	650	650	265	1.8	0.95	1400	560	230	1.7	0.90	1100	1700	0.50	0.50
24F-E13	DF/DF	2400	2400	650	650	265	1.8	0.95	1750	560	230	1.7	0.90	1250	1700	0.50	0.50
24F-E18	DF/DF	2400	2400	650	650	265	1.8	0.95	1550	560	230	1.7	0.90	975	1700	0.50	0.50
24F-V3	SP/SP	2400	2000	740	740	300	1.8	0.95	1700	650	260	1.6	0.85	1150	1650	0.55	0.55
24F-V8	SP/SP	2400	2400	740	740	300	1.8	0.95	1700	650	260	1.6	0.85	1150	1650	0.55	0.55
24F-E1	SP/SP	2400	1450	805	650	300	1.8	0.95	1550	650	260	1.7	0.90	1150	1600	0.55	0.55
24F-E4	SP/SP	2400	2400	805	805	300	1.9	1.00	1850	650	260	1.8	0.95	1450	1750	0.55	0.55

Table 5.1.3 Net Finished Widths of Structural Glued Laminated Timbers

Nominal Width of Laminations (in.)	3	4	6	8	10	12	14	16
Western Species								
Net Finished Width (in.)	2-1/2	3-1/8	5-1/8	6-3/4	8-3/4	10-3/4	12-3/4	14-3/4
Southern Pine								
Net Finished Width (in.)	2-1/2	3	5	6-3/4	8-1/2	10-1/2	12	14

Glulam Beams – Design

- Design as standard wood member using NDS Table 5.3.1 adjustment factors

Table 5.3.1 Applicability of Adjustment Factors for Structural Glued Laminated Timber

	ASD	ASD and LRFD										LRFD			
	only	Load Duration Factor	Wet Service Factor	Temperature Factor	Beam Stability Factor ¹	Volume Factor ¹	Flat Use Factor	Curvature Factor	Stress Interaction Factor	Shear Reduction Factor	Column Stability Factor	Bearing Area Factor	Format Conversion Factor	Resistance Factor	Time Effect Factor
													K _F	φ	
$F_b' = F_b$ x	C _D	C _M	C _t	C _L	C _V	C _{fu}	C _c	C _I	-	-	-	-	2.54	0.85	λ
$F_t' = F_t$ x	C _D	C _M	C _t	-	-	-	-	-	-	-	-	-	2.70	0.80	λ
$F_v' = F_v$ x	C _D	C _M	C _t	-	-	-	-	-	C _{vr}	-	-	-	2.88	0.75	λ
$F_{rt}' = F_{rt}$ x	C _D	C _M	C _t	-	-	-	-	-	-	-	-	-	2.88	0.75	λ
$F_c' = F_c$ x	C _D	C _M	C _t	-	-	-	-	-	-	-	C _P	-	2.40	0.90	λ
$F_{c\perp}' = F_{c\perp}$ x	-	C _M	C _t	-	-	-	-	-	-	-	C _b	-	1.67	0.90	-
$E' = E$ x	-	C _M	C _t	-	-	-	-	-	-	-	-	-	-	-	-
$E_{min}' = E_{min}$ x	-	C _M	C _t	-	-	-	-	-	-	-	-	-	1.76	0.85	-

1. The beam stability factor, C_L, shall not apply simultaneously with the volume factor, C_V, for structural glued laminated timber bending members (see 5.3.6). Therefore, the lesser of these adjustment factors shall apply.

Glulam Columns - Design

APA design guide for “first pass” tables

TABLE 5

ALLOWABLE AXIAL LOADS (POUNDS) FOR COMBINATION NO. 2 DOUGLAS-FIR GLULAM COLUMNS
Side loads are not permitted. End loads are limited to a maximum eccentricity of either 1/6 column width or depth, whichever is worse.

Effective Column Length (ft)	Lamination Net Width = 3-1/2 in.								
	Net Depth = 4-1/2 in. (3 lams)			Net Depth = 6 in. (4 lams)			Net Depth = 7-1/2 in. (5 lams)		
	Load Duration Factor			Load Duration Factor			Load Duration Factor		
	1.00	1.15	1.25	1.00	1.15	1.25	1.00	1.15	1.25
8	7,283	7,611	7,799	10,108	10,523	10,762	12,635	13,154	13,453
9	6,184	6,424	6,561	8,531	8,836	9,010	10,664	11,044	11,263
10	5,298	5,479	5,582	7,278	7,507	7,639	9,097	9,384	9,548
11	4,580	4,720	4,800	6,271	6,448	6,550	7,839	8,060	8,187
12	3,994	4,104	4,167	5,454	5,594	5,673	6,817	6,992	7,092
13	3,510	3,598	3,649	4,783	4,895	4,959	5,979	6,119	6,199
14	3,107	3,179	3,220	4,226	4,318	4,370	5,283	5,397	5,462

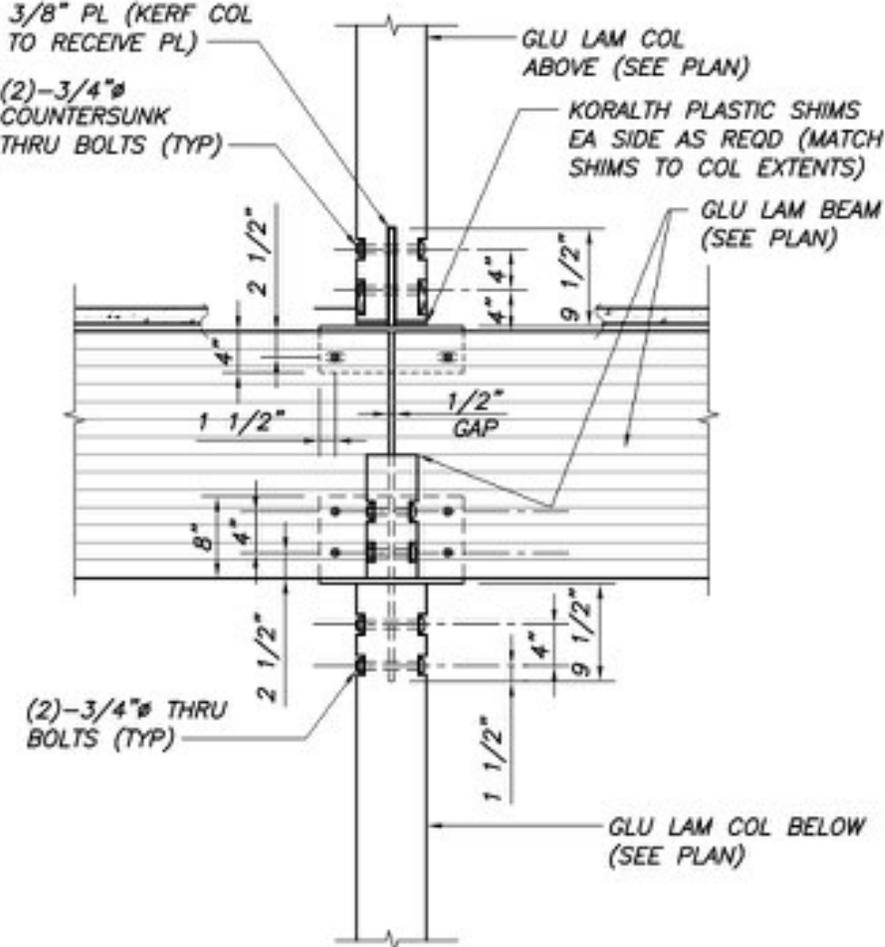
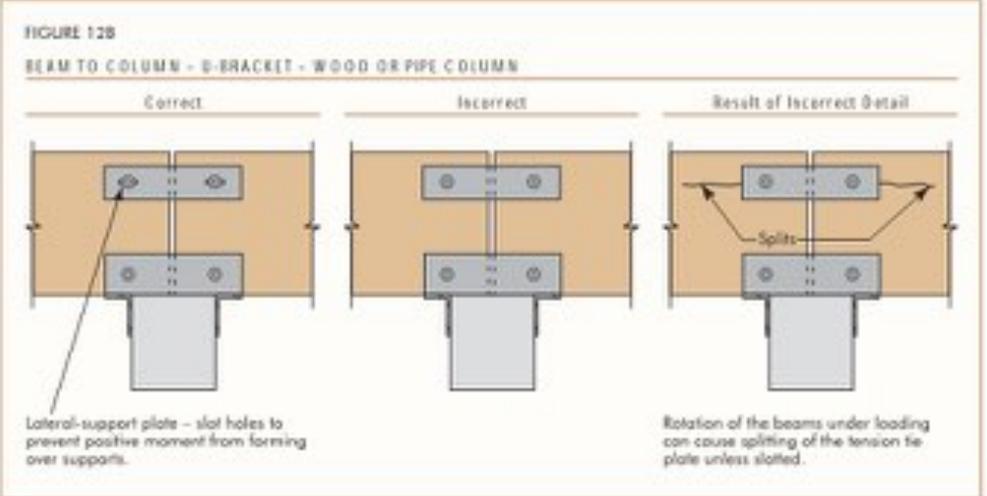
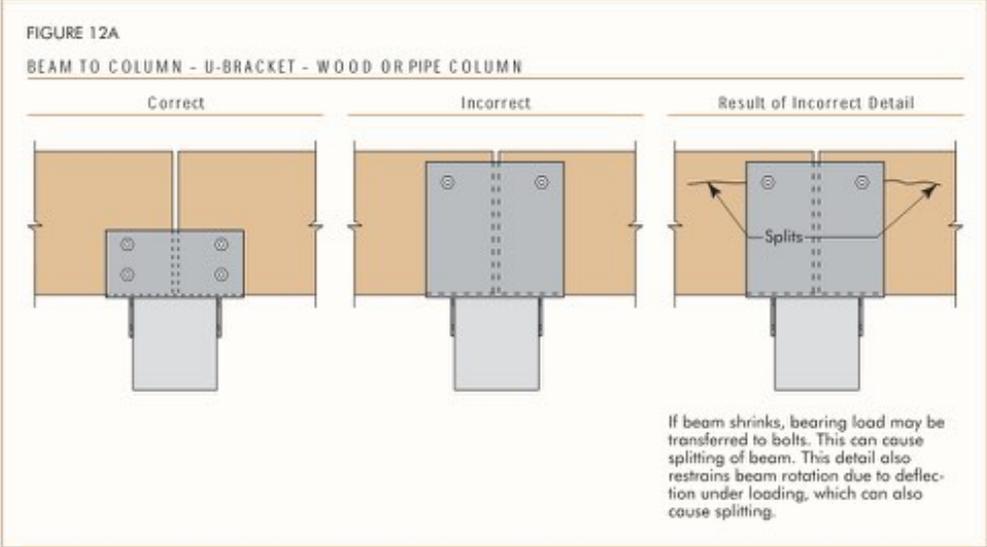
Notes:

1. The tabulated allowable loads apply only to one-piece glulam members made with all L2 laminations (Combination 2) without special tension laminations.
2. Applicable service conditions = dry.
3. The tabulated allowable loads are based on axially loaded columns subjected to a maximum eccentricity of either 1/6 column width or 1/6 column depth, whichever is worse. For side loads, other eccentric end loads, or other combined axial and flexural loads, see NDS.
4. The column is assumed to be unbraced, except at the column ends, and the effective column length is equal to the actual column length.
5. Design properties for normal load duration and dry-use service conditions:
 Compression parallel to grain (F_c) = 1,950 psi for 4 or more lams, or 1,600 psi for 2 or 3 lams.
 Modulus of elasticity (E) = 1.6×10^6 psi.
 Flexural stress when loaded parallel to wide faces of lamination ($F_{b\parallel}$) = 1,800 psi for 4 or more lams, or 1,600 psi for 3 lams.
 Flexural stress when loaded perpendicular to wide faces of lamination ($F_{b\perp}$) = 1,700 psi for 2 lams to 15 in. deep without special tension laminations.
 Volume factor for $F_{b\perp}$ is in accordance with NDS. Size factor for $F_{b\perp}$ is $(12/d)^{1.5}$, where d is equal to the lamination width in inches.
6. These values are for preliminary design use only. Final design should include a complete analysis, including bearing capacity of the foundation supporting the column.

Design of Structural Glued Laminated Timber Columns



Glu-Lam Connections per AITC / APA



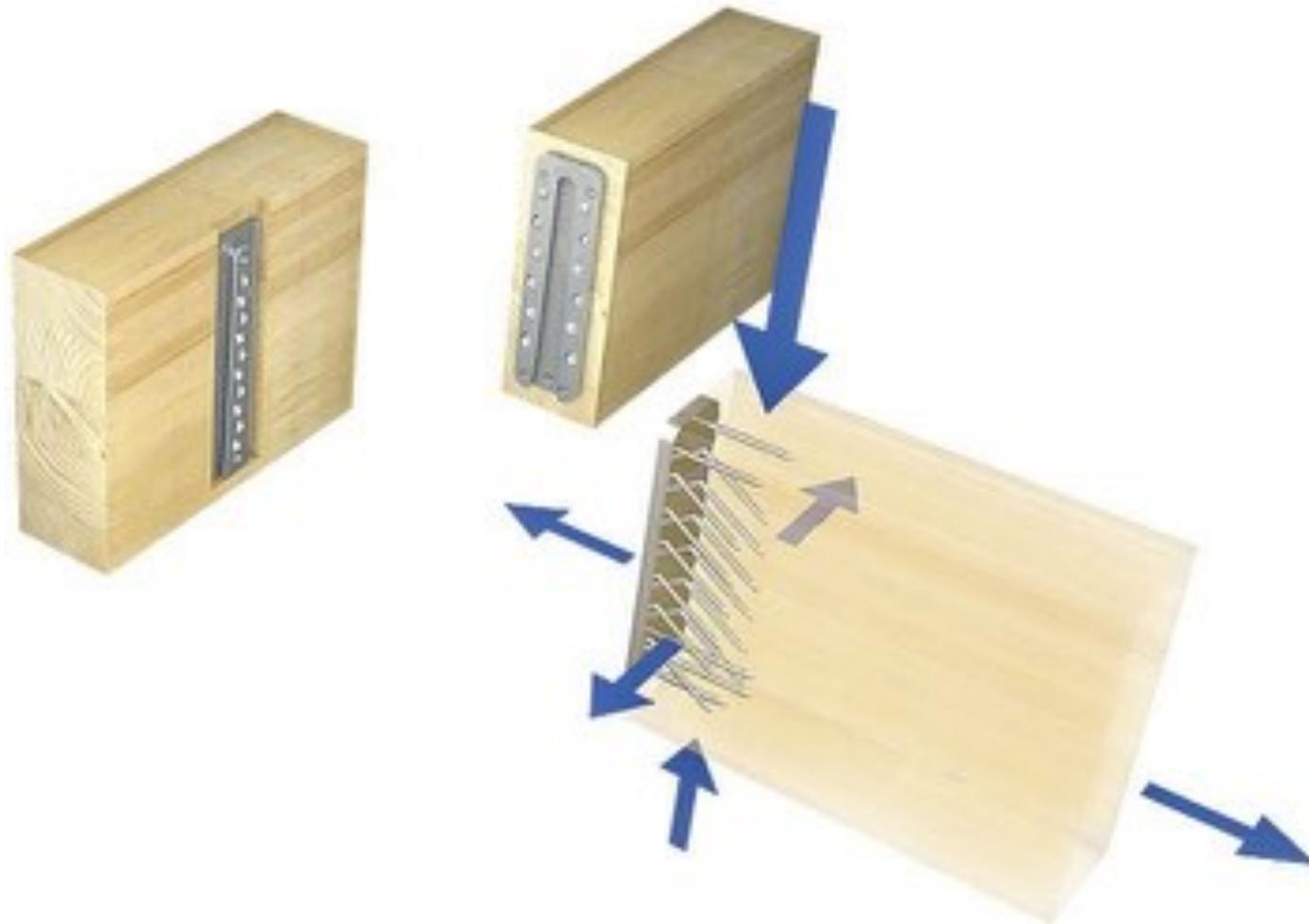
reference: APA Glulam Design Guide

Glu-Lam Connection Details



Glu-lam Connection Details

Beam - Beam



5,800-29,400 lb capacity

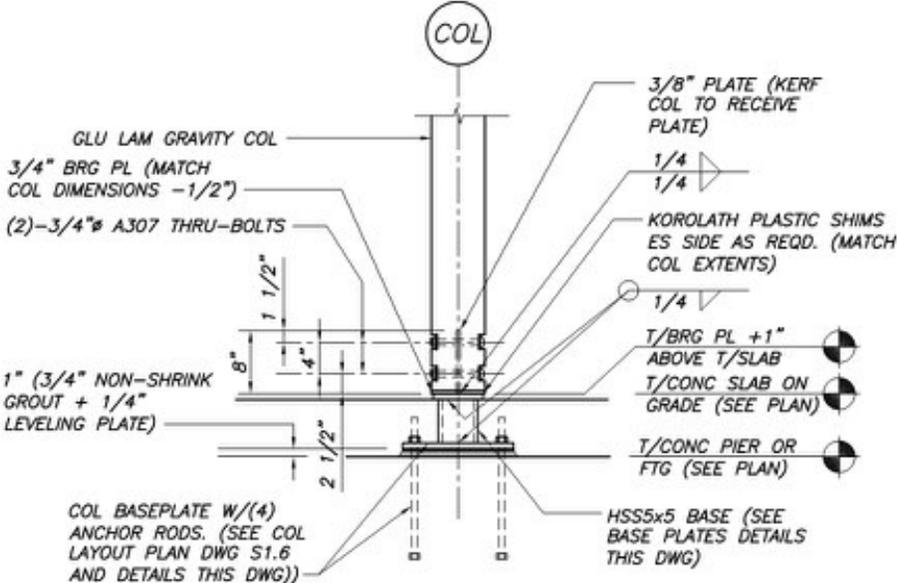
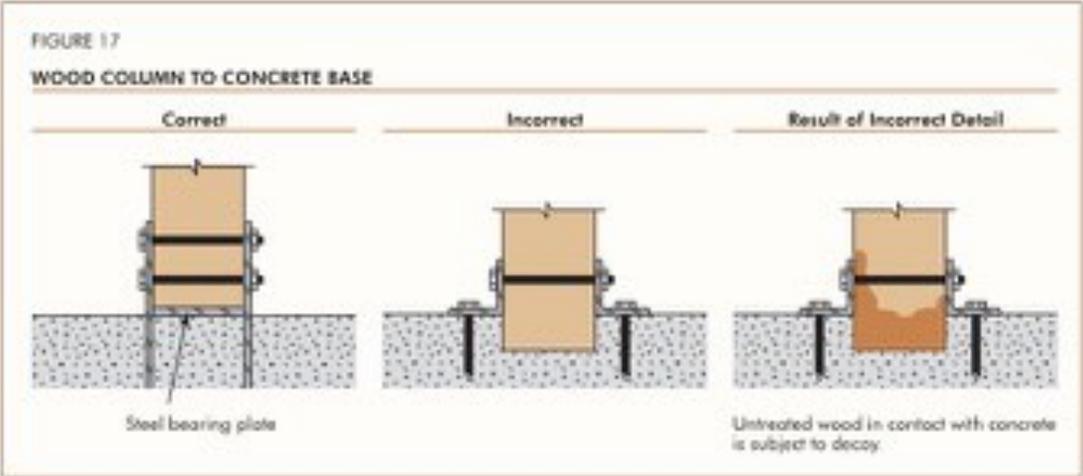
Glu-lam Connection Details

Beam - Column



Photo: structurlam

Glu-lam Connection Details



Glu-lam Connection Details

Column-column connections
concealed steel connection

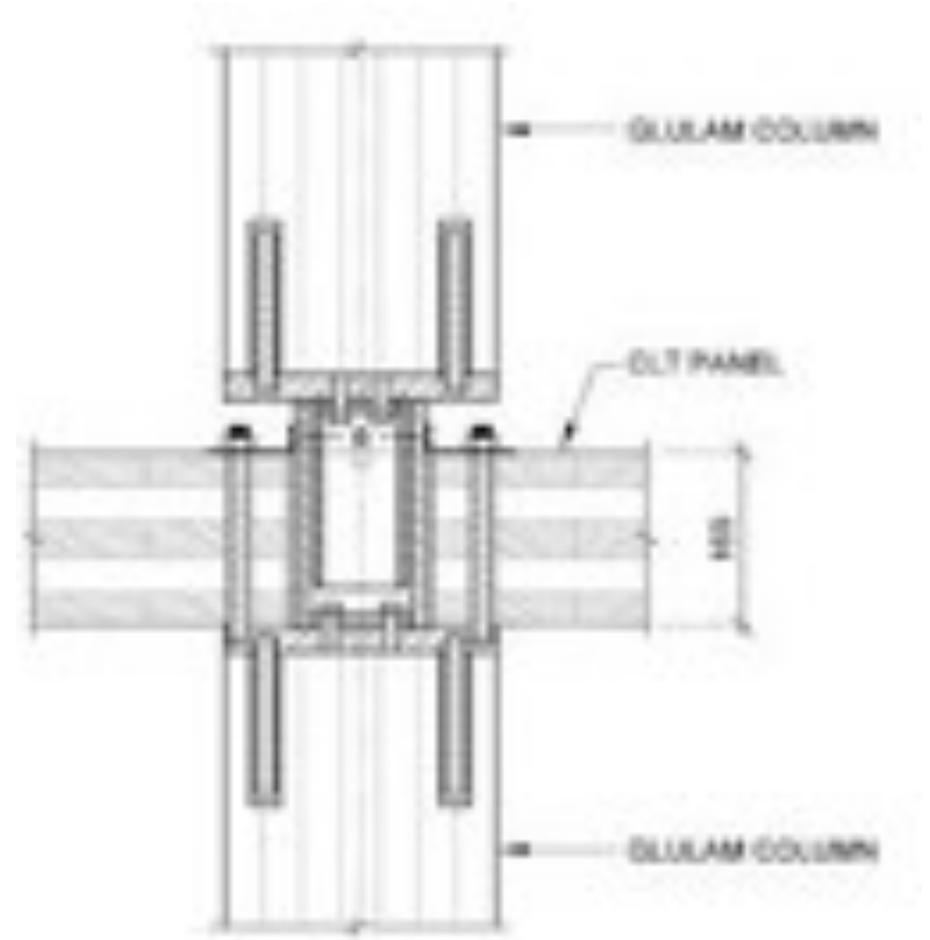


image: Structurecraft

Glu-lam Connection Details

Column-column connections
concealed steel connection



Brock Commons, Vancouver, BC



> QUESTIONS?

This concludes The American Institute
of Architects Continuing Education
Systems Course

Paul B. Becker, PE

Thornton Tomasetti

pbecker@thorntontomasetti.com