Four-story Wood-frame Structure over Podium Slab
Design and Building Support for the Non-residential Market

WoodWorks provides free resources that allow engineers, architects and others to design and build non-residential structures out of wood more easily and at less cost. This includes one-on-one technical support as well as free educational events and training, online resources such as CAD and REVIT drawings, and one-stop access to information provided by wood associations nationwide.

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Wood provides more value—in terms of its beauty, design flexibility and environmental attributes—for less cost than other major building materials, all while meeting fire, safety and other code requirements.

1. **Wood is an inherently green building material** – It grows naturally, using energy from the sun, and is the only major building material that’s renewable and sustainable over the long term. Life cycle assessment studies also show that it’s better for the environment than other materials in areas such as embodied energy, air and water pollution, and global warming potential.

2. **Wood performs well in earthquakes and high winds** – Because wood-frame buildings are lighter and have more connections than structures built with other materials, they are very effective at resisting lateral and uplift forces from seismic or wind loads.

3. **Wood structures can be designed for safety and code acceptance** – The International Building Code offers a wide range of options for designing wood schools, offices, multi-family residences and other non-residential building types.

4. **Wood buildings are adaptable** – Studies show that most buildings in North America have a service life of less than 50 years and tend to be demolished because of changing needs and increasing land values as opposed to performance issues. When one considers the embodied energy in these structures and issues related to disposal, the adaptability of wood structures and building systems, either through renovation or deconstruction and reuse, is a significant advantage.

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Overview

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This design example illustrates the seismic design of a four story wood framed hotel over one story of concrete podium slab which is assigned to Seismic Design Category D. The gravity load framing system consists of wood-frame bearing walls for the upper stories and concrete bearing walls for the lower story. The lateral load resisting system consists of wood-framed shear walls for the upper stories and concrete shear walls for the lower story. Typical building elevation and floor plan of the structure are shown in Figures 1 and 2 respectively. A typical section showing the heights of the structure is shown in Figure 4. The wood roof is framed with pre-manufactured wood trusses. The floor is framed with prefabricated wood I-joists. The floors have a 1-1/2 inch lightweight concrete topping. The roofing is composition shingles.

This design example uses the term “podium slab” which, while not included in the 2006 International Building Code (IBC) or 2007 California Building Code (CBC), is commonly used in the building industry. This type of construction is also referred to as an uppermost “structural slab” or “transfer slab” (both can have a slab and beam system) that is designed to support the entire weight of the wood superstructure.

When designing this type of “mid-rise” wood-frame structure, there are several unique design elements to consider. The following steps provide a detailed analysis of some of the important seismic requirements of the shear walls per the 2006 IBC and 2007 CBC.

This example is not a complete building design. Many aspects have not been included, specifically the gravity load framing system, and only certain steps of the seismic design related to portions of a selected shear wall have been illustrated. In addition, the lateral requirements for wind design related to the selected shear wall have not been illustrated (only seismic). The steps that have been illustrated may be more detailed than what is necessary for an actual building design but are presented in this manner to help the design engineer understand the process.

Codes and Reference Documents Used

2006 International Building Code (IBC)
2005 Special Design Provisions for Wind and Seismic (SDPWS)
2007 California Building Code (CBC)

This design example focuses on the IBC and NDS requirements. Where there is a difference between the IBC and CBC, a comment and reference is made.
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Outline

This design example illustrates the following selected parts of the design process:

1. Four stories Type V wood framing over Type I concrete
2. Two-stage design for lateral analysis
3. Seismic design of flexible upper portion and rigid lower portion
4. Code requirements for use of fire-retardant-treated wood (FRTW)
5. Vertical displacement (shrinkage) in multi-level wood framing
6. Shear wall design example
7. Considerations with continuous and discontinuous anchor tie-downs
8. Shear wall deflection, tie-down and take-up devices
9. Discontinuous system considerations with the over strength (Ω) factor

Given Information

<table>
<thead>
<tr>
<th>ROOF WEIGHTS:</th>
<th>FLOOR WEIGHTS:</th>
</tr>
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<tbody>
<tr>
<td>Roofing + re-roof:</td>
<td>Flooring:</td>
</tr>
<tr>
<td>Sheathing</td>
<td>1.0 psf</td>
</tr>
<tr>
<td>Trusses + blocking</td>
<td>Lt. wt. concrete:</td>
</tr>
<tr>
<td>Insulation + sprinklers</td>
<td>14.0</td>
</tr>
<tr>
<td>Ceiling + misc.</td>
<td>Sheathing:</td>
</tr>
<tr>
<td>Beams</td>
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<tr>
<td>Insulation + sprinklers</td>
<td>I-joist + blocking:</td>
</tr>
<tr>
<td>Ceiling + misc.</td>
<td>4.0</td>
</tr>
<tr>
<td>Beams</td>
<td>Ceiling + misc.:</td>
</tr>
<tr>
<td>Dead load</td>
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<tr>
<td>Live load</td>
<td>Beams:</td>
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<td></td>
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<td></td>
<td>20.0 psf</td>
</tr>
<tr>
<td></td>
<td>40.0 psf</td>
</tr>
</tbody>
</table>
Interior and exterior wall weights have not been included in the above loads; they have been included in the diaphragm weights shown below. Typical interior and exterior partition weights can vary between 10 psf and 20 psf depending on room sizes, number of layers of gypsum board on walls, etc.

Weights of respective diaphragm levels, including tributary exterior and interior walls:

**FLEXIBLE UPPER PORTION**

\[ W_{\text{roof}} = 587 \text{ k} \]
\[ W_{\text{5th floor}} = 639 \text{ k} \]
\[ W_{\text{4th floor}} = 647 \text{ k} \]
\[ W_{\text{3rd floor}} = 647 \text{ k} \]
\[ W = 2,520 \text{ k} \]

**RIGID LOWER PORTION**

\[ W_{\text{upper}} = 2,520 \text{ k} \]
\[ W_{\text{2nd floor}} = 2,632 \text{ k} \]
\[ W = 5,152 \text{ k} \]

Weights of roof diaphragms are typically determined by taking one half the height of the walls from the fifth floor to the roof. Weights of floor diaphragms are typically determined by taking one-half of the walls above and below for the fifth, fourth and third floor diaphragms. The weights of all walls, including interior non-bearing partitions, are included in the respective weights of the various levels. The weight of parapets (where they occur) has been included in the roof weight.

The roof is 1/2-inch-thick DOC PS 1 or DOC PS 2-rated sheathing, 32/16 span rating with Exposure I glue.

The floor is 23/32-inch-thick DOC PS 1 or DOC PS 2-rated Sturd I Floor 24 inches o.c. rating, 48/24 span rating with Exposure I glue.

DOC PS 1 and DOC PS 2 are the U.S. Department of Commerce (DOC) Prescriptive and Performance-based standards for plywood and oriented strand board (OSB), respectively.

Wall framing is a modified balloon framing where the joists hang from the walls in joist hangers (see Figure 6).

Framing lumber for studs and posts

*NDS Table 4A*

**DOUGLAS FIR LARCH-NO. 1 GRADE:**

\[ F_b = 1,450 \text{ psi} \]
\[ F_c = 1,500 \text{ psi} \]
\[ F_t = 1,500 \text{ psi} \]
\[ E = 1,700,000 \text{ psi} \]
\[ E_{min} = 620,000 \text{ psi} \]
\[ C_m = 1.0 \]
\[ C_f = 1.0 \]

Common wire nails are used for shear walls, diaphragms and straps. When specifying nails on a project, specification of the penny weight, type, diameter and length (example 10d common = 0.148” x 3”) are recommended.
The IBC, NDS and associated *Special Design Provisions for Wind and Seismic (SDPWS)* list values for shear walls and diaphragms. For values using nail and sheathing thickness not listed in the IBC and NDS/SDPWS, the engineer can also consider using the values listed in *International Code Council-Evaluation Service (ICC-ES)* Report ESR-1539 from the International Staple, Nail and Tool Association (ISANTA). This report can be downloaded from ISANTA's website at http://www.isanta.org or from the International ICC-ES website at http://www.icc-es.org.

**Figure 1. Building Elevation**

![Building Elevation](image)

**NOTE FOR FIGURE 1:**
See Figure 2 for building plan dimensions and Figure 4 for building height dimensions.

**Figure 2. Typical Floor Plan**

![Typical Floor Plan](image)

**NOTE FOR FIGURE 2:**
In Figure 2, the prefabricated wood I-joists run east-west spanning to the wood-bearing walls separating the hotel guest units running north-south at 13 feet o.c. The floor area is 12,000 square feet.
Factors That Influence Design

Prior to starting the seismic design of a structure, the following must be considered:

**Species of Lumber**

The species of lumber used in this design example is Douglas Fir-Larch (DF-L), which is common on the west coast. The author does not intend to imply that this species can or should be used in all areas or for all markets. Species that are both appropriate for this type of construction and locally available vary by region, and also commonly include (among others) Southern Yellow Pine (SYP) and Spruce Pine Fir (SPF).

**Grade of Lumber**

The lower two stories of the wood-frame structure carry significantly higher gravity loads than the upper two stories. One approach is to use a higher grade of lumber for the lower two stories than the upper two stories. This approach can produce designs that yield a consistent wall construction over the height of the building. Another approach would be to choose one grade of lumber for all four wood-frame stories. This approach produces the need to change the size and/or spacing of the studs based on the loading requirements. Sill plate crushing may control stud sizing at lower levels. For simplicity, this design example illustrates the use of one lumber grade for all floor levels.

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**Moisture Content and Wood Shrinkage**

From a serviceability and performance perspective, the most significant issue related to multistory wood-frame construction is wood shrinkage—which is impacted by the moisture content (MC) and, more specifically, whether the wood used is “green” or “kiln dried.”

The availability of both types is largely dependent on the region and associated market conditions. Typically, wood used in construction in the U.S. southwest is “green” (S-GRN) and kiln dried (KD) wood is relatively rare, while the opposite is true in other parts of the country. The engineer should consider the availability of kiln dried lumber in the area of the proposed construction. The WoodWorks website provides access to technical support offered either one-on-one or via wood associations nationwide, to help designers looking for this type of information. To learn more, visit: www.Woodworks.org/aboutWoodworks/technical-support.aspx
**Condition of Seasoning**

There are three levels of wood seasoning (drying), which denotes the moisture content of the lumber at the time of surfacing. The identification “stamps” are as follows:

- **S-GRN** = over 19% moisture content (unseasoned)
- **S-DRY, KD or KD-HT** = 19% maximum moisture content (seasoned)
- **MC 15 or KD 15** = 15% maximum moisture content

These designations may be found in the grade stamp.

Unseasoned lumber (S-GRN) is manufactured oversized so that when the lumber reaches 19 percent moisture content it will be approximately the same size as the dry (seasoned) size.

Heat treated (HT) lumber is lumber that has been placed in a closed chamber and heated until it attains a minimum core temperature of 56°C for a minimum of 30 minutes.

The word “DRY” indicates that the lumber was either kiln or air dried to a maximum moisture content of 19 percent.

Kiln dried (KD) lumber is lumber that has been seasoned in a chamber to a pre-determined moisture content by applying heat.

Kiln dried heat treated (KD-HT) lumber has been placed in a closed chamber and heated until it achieves a minimum core temperature of 56°C for a minimum of 30 minutes.

Moisture content restrictions apply at time of shipment as well as time of dressing if dressed lumber is involved, and at time of delivery to the buyer unless shipped exposed to the weather.

Engineered I-joists were used for this design example; however, given the short span on the floor joists, sawn lumber could have been used. In this case, the joist shrinkage perpendicular to grain would need to be included in the overall shrinkage calculation. Also, sawn lumber joists can be supported in joist hangers (see Figure 6) so as not to contribute to the overall building shrinkage. For this design example, “sawn” lumber is used for the stud-framed walls and pre-manufactured roof trusses.

For further explanation of moisture content and wood shrinkage, see section 5.

**Location of Shear Walls**

The lateral force-resisting system in this design example uses both interior and exterior walls for shear walls (see Figure 2). The seismic force-resisting system for the transverse direction (north-south) utilizes the interior walls between the hotel guest rooms. A seismic design of a selected interior shear wall in the transverse direction is illustrated in this design example. The seismic force-resisting system for the longitudinal direction (east-west) utilizes the long interior corridor walls located at the center of the structure, with shear walls on both sides of the corridor in addition to shear walls on the exterior walls and shear walls at the bathroom walls.

Related to the lateral force-resisting system in the longitudinal direction for structures similar to this design example, it is recognized that some structural engineers will only utilize the interior corridor walls and not place shear walls on the exterior walls. This type of design uses a rigid diaphragm approach to the distribution of lateral forces to the shear walls. Code requirements for semi-rigid or flexible diaphragms on structures similar to this design example would not allow the elimination of the exterior shear walls in the longitudinal direction. While the code does not explicitly prohibit the elimination of exterior shear walls for wood-framed structures, from a performance perspective, the elimination is not recommended.
Support of Floor Joists

This design example uses balloon framing. The floor joists are supported in joist hangers hung from the top plates (see Figure 6). The wall studs and posts have a simple span between the top of the sole plate and the bottom of the lower top plate.

For wood-frame structures built with regular platform construction, the floor joists are supported by direct bearing onto the top plate(s) (see Figure 6A).

Calculations and Discussion

1. Four Stories Type V Wood Framing over Type I Concrete

   ASCE 7-05 §12.2.3.1

1a. Structural/Seismic Height Limitation

   The heights of the floors and roof are shown in Figure 4.

   **MAXIMUM HEIGHT OF STRUCTURE:**

   ASCE 7-05 Table 12.2.1

   Table 12.2.1 of ASCE 7-05 lists the maximum height of a structure, measured from its base, related to the seismic force-resisting system (SFRS) and the Seismic Design Category (SDC). Section 11.2 defines the base of the structure as “the level at which horizontal seismic ground motions are considered to be imparted on the structure.”

   Industry standard for the height of the wood-framed building is measured from the top of the podium slab to the average roof sheathing elevation. Using the podium slab as the base for the light-framed walls sheathed with wood structural panels:

   The height limit in SDC ‘D’ is 65 feet

   The average (mean) height of the structure is 49.1 feet

   65 > 49.1 okay

   **1b. Fire and Life Safety Height and Area Limitations**

   **TYPE V OVER TYPE IA (OR TYPE II) CONSTRUCTION:**

   IBC Table 503

   **Lower Portion**

   Type 1A construction

   Occupancy is S2, B, E and A2

   Per IBC Table 503:

   Allowable height is unlimited

   Allowable number of stories is unlimited

   Per IBC Table 503:

   Allowable area is unlimited
Upper Portion-try as Type VA Construction

Type VA construction
Occupancy is R-2
Per IBC Table 503:
Allowable height is 50 feet
Allowable number of stories is three
Allowable area is 12,000 square feet per story $\geq$ 12,000 square feet okay

IBC §504.2 states that for Group R buildings equipped with an automatic sprinkler system, the value specified in Table 503 for the maximum height can be increased by 20 feet and the maximum number of stories increased by one, but shall not exceed 60 feet in height or four stories.

Modified allowable height is 60 feet (max) $>$ 49.1 feet okay
Modified number of stories is four $\leq$ four stories okay

IBC Table 503 defines the height limit and story limit as being above grade plane; hence it cannot count the upper structure only, but must consider the building as a whole. However, IBC §509.2 defines the number of stories allowed as pertaining to the wood portion above the podium slab horizontal assembly.

SUMMARY:
Structural/seismic height limit controls the building height at 65 feet.
This structure will be a Type VA structure over a Type I structure with automatic fire sprinklers.

1c. Wood Studs in Fire-resistance-rated Walls

When wood-frame structures exceed the limits for Type V construction, the code requires either Type III or Type IV construction.

IBC §602.3 defines Type III construction as buildings with exterior walls made from non-combustible materials. Therefore, the use of fire-retardant-treated wood (FRTW) is required for the exterior load-bearing wall assemblies.

Fire-rated assemblies can be found in a number of sources including the IBC, the Underwriters Laboratories (UL) Fire-resistance-rated Systems and Products, the UL Fire Resistance Directory, and the Gypsum Association’s Fire Resistance Design Manual.

Table 720.1(2) of the IBC lists fire ratings for various wall construction types. Many of the wall construction types using wood construction reference footnote ‘m.’ Footnote ‘m’ of the table requires the reduction of $F'_c$ to be 78 percent of the allowable when the slenderness ratio $l_e/d > 33$.

The American Forest & Paper Association (AF&PA) has tested a number of wood-frame fire-rated assemblies. There is a disparity between the IBC and publications such as AF&PA’s Fire-Rated Wood-Frame Wall and Floor/Ceiling Assemblies, which does not require the reduction in allowable stress. The building’s architect and/or engineer should check with the local jurisdiction to determine the accepted approach. The AF&PA procedure is detailed at: http://www.awc.org/pdf/CalculatingtheSuperimposedLoadonWoodFrameWalls.pdf.
DETERMINATION OF $C_L$: NDS-05 3.3.3.2

When studs have gypsum sheathing or structural panel sheathing on both sides of the studs and posts, where the compressive edges are held in line, $C_L$ may be assumed to be 1.0.

$l_u = h_u = $ the clear height of the studs

This design example has sheathing on both sides, therefore $C_L = 1.0$.

However, when a sound wall is used and the studs are staggered where one edge of the stud does not have its compressive edge held in line, $C_L$ needs to be calculated. For this loading condition, the effective unbraced length $l_u$ for the studs and posts is listed in NDS-05 Table 3.3.3 as follows:

For a 10'-0" floor-to-floor height with a 2x4 sole plate with a 4x4 top plate:

$$l_u = \frac{114 \text{in}}{3.5 \text{in}} = 33 > 7$$

Therefore:

$$l_u = 1.631l_u + 3d$$

Solving for $l_u/d = 33$ yields the following stud and post lengths for the footnote ‘m’ reduction in $F'c$:

For 4x studs and posts:

$l_u > 5'-4"$

For 6x studs and posts:

$l_u > 8'-5"$

Since most wall heights for new buildings are 9 to 10 feet, this reduction in $F'c$ is basically applied to all bearing walls in a fire-rated wall.

It should be noted that this is an IBC requirement and not an NDS requirement.

NOTE:
American Wood Council publication DCS3 (which can be downloaded at www.awc.org) provides wood stud walls tested to 100 percent design load. These walls can be used without the 0.78 reduction factor. Local building department requirements should be checked.

2. Two-stage Design for Lateral Analysis ASCE 7-05 §12.2.3.1

Due to IBC Table 508.3.3 requirements for building occupancies, a one-hour area separation between the first floor (A-3 Occupancy) and the second floor (R-1 Occupancy) is necessary. Also, if the sub-structure (first floor) is for parking, a three-hour separation is required per IBC §509.2.

The seismic response coefficient $R$ for the first floor special concrete shear walls and special reinforced masonry shear walls is 5.0. The seismic response coefficient $R$ for the wood structural panel shear walls is 6.5. Section 12.2.3.1 of ASCE 7-05 requires the least value of $R$ to be used for the building for the seismic design in that direction.

One approach that can be used for the seismic design would be to design the entire structure for the $R$ value of 5.0. However, this would require the upper wood-framed portion of the structure to be designed for 30 percent higher forces in addition to inverting more of the building’s mass (second floor) into the upper stories.
A more realistic approach (from both a seismic and economic perspective) would be to design the structure using the two-stage equivalent lateral force procedure prescribed in ASCE 7-05. This procedure can be used where there is a flexible upper portion and a rigid lower portion. This structure type (two-stage design) would be in effect the structural opposite to the “soft story” structures that are not desirable.

The allowance of two-stage-equivalent lateral force procedure for a flexible upper portion above a rigid lower portion has been in the building code since the 1988 Uniform Building Code with essentially the same variables. This procedure is permitted when the structure complies with the following criteria:

A. The stiffness of the lower portion must be at least 10 times the upper portion.
B. The period of the entire structure shall not be greater than 1.1 times the period of the upper portion.
C. The flexible upper portion shall be designed as a separate structure using the appropriate values of $R$ and $\rho$.
D. The rigid lower portion shall be designed as a separate structure using the appropriate values of $R$ and $\rho$.

For the purpose of this design example, the building is regular and qualifies for the Equivalent Lateral Force Procedure to be used.

### 2a. Stiffness Determinations

Stiffness of the lower portion must be at least 10 times the upper portion.

Wall rigidity (stiffness):

$$ F = k \delta $$

Or

$$ k = \frac{F}{\delta} $$

Where:

- $F$ = the applied force to the wall
- $k$ = the stiffness of the wall
- $\delta$ = deflection of the wall

**STIFFNESS OF FLEXIBLE UPPER PORTION:**

Determine stiffness of typical interior cross wall:

**Table 1. Determine stiffness of typical interior wall**

<table>
<thead>
<tr>
<th>Level</th>
<th>$F$</th>
<th>$\delta$</th>
<th>$\frac{F}{\delta}$</th>
</tr>
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<tbody>
<tr>
<td></td>
<td>$(k)$</td>
<td>$(\text{in})$</td>
<td>$(\text{k/in})$</td>
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<tr>
<td>Roof</td>
<td>13.935</td>
<td>0.27</td>
<td>51.61</td>
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<td>5th Floor</td>
<td>23.415</td>
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<td>78.05</td>
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<td>4th Floor</td>
<td>29.820</td>
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<td>96.19</td>
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<td>3rd Floor</td>
<td>33.045</td>
<td>0.31</td>
<td>106.60</td>
</tr>
</tbody>
</table>

Where: $F$ = the applied force to the wall as determined from Table 6

$\delta$ = the computed shear wall deflection from Table 16
STIFFNESS OF RIGID LOWER PORTION:

Determine stiffness of typical interior cross wall:

From 3-D finite element analysis of the rigid lower portion, the average deflection of the first floor transverse shear wall at design seismic loading:

\[ \delta_{\text{walls}} = 0.02 \text{ in} \]

\[ F_{\text{wall}} = 190 \text{ kips} \]

\[ k = \frac{190k}{0.02 \text{ in}} = 9,500 \frac{k}{\text{in}} \]

Ratio of rigid lower portion stiffness to flexible upper portion stiffness:

\[ \text{ratio} = \frac{9,500}{106.60} = 89 > 10 \implies \text{okay} \]

2b. Period Determinations

Check for conformance to the requirement that the period of the entire structure must not be greater than 1.1 times the period of the upper portion.

First determine building periods (see Figure 4 for section through structure) using the approximate fundamental period equations of ASCE 7-05 as opposed to computer model calculations.

For the flexible upper portion:

\[ T_b = C_t(h_n)^x = 0.020(62.84)^{3/4} = 0.45 \text{ sec} \]

\[ \text{ASCE 7-05 Eq. 12.8-7} \]

For the entire structure:

\[ T_b = C_t(h_n)^x = 0.020(74.84)^{3/4} = 0.50 \text{ sec} \]

\[ \text{ASCE 7-05 Eq. 12.8-7} \]

Ratio of periods:

\[ \frac{0.50}{0.45} = 1.14 \approx 1.1 \implies \text{close-enough} \]

Using the ASCE 7-05 equation can produce period ratios > 1.1. This equation is problematic since the same equation is used for both wood and concrete shear walls to determine the building period.

ALTERNATE METHOD OF PERIOD DETERMINATION:

\[ T = 2\pi \sqrt{\frac{\sum (w_i \delta_i^2)}{\sum (g_i f_i \delta_i)}} \]

\[ \text{FEMA 450 Eq. C5.2-1} \]

The above equation, which produces a more accurate building period, is based on Rayleigh's method and was the equation that appeared in the Uniform Building Codes (Eq. 30-10 in the 1997 UBC).
Table 2. Determine period of flexible upper portion

<table>
<thead>
<tr>
<th>Level</th>
<th>w (k)</th>
<th>f (k)</th>
<th>δ(in)</th>
<th>w(δ)^2</th>
<th>fδ</th>
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<tr>
<td>Roof</td>
<td>587</td>
<td>197.9</td>
<td>0.27</td>
<td>42.79</td>
<td>53.43</td>
</tr>
<tr>
<td>5th Floor</td>
<td>639</td>
<td>134.6</td>
<td>0.30</td>
<td>57.51</td>
<td>40.38</td>
</tr>
<tr>
<td>4th Floor</td>
<td>647</td>
<td>91.0</td>
<td>0.31</td>
<td>62.18</td>
<td>28.21</td>
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<tr>
<td>3rd Floor</td>
<td>647</td>
<td>45.5</td>
<td>0.31</td>
<td>62.18</td>
<td>14.10</td>
</tr>
<tr>
<td>∑</td>
<td>2,520</td>
<td>469.0</td>
<td></td>
<td>224.66</td>
<td>136.12</td>
</tr>
</tbody>
</table>

\[ T = 2\pi \sqrt{\frac{224.66}{(32.2 \times 12) \times 136.12}} = 0.41 \text{ sec} \]

Table 2A. Determine period of entire structure

<table>
<thead>
<tr>
<th>Level</th>
<th>w (k)</th>
<th>f (k)</th>
<th>δ(in)</th>
<th>w(δ)^2</th>
<th>fδ</th>
</tr>
</thead>
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<tr>
<td>4th Floor</td>
<td>647</td>
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<td>0.31</td>
<td>62.18</td>
<td>28.21</td>
</tr>
<tr>
<td>3rd Floor</td>
<td>647</td>
<td>45.5</td>
<td>0.31</td>
<td>62.18</td>
<td>14.10</td>
</tr>
<tr>
<td>2nd Floor</td>
<td>2,632</td>
<td>489.5</td>
<td>0.02</td>
<td>1.05</td>
<td>9.79</td>
</tr>
<tr>
<td>∑</td>
<td>5,152</td>
<td>958.50</td>
<td></td>
<td>225.71</td>
<td>145.91</td>
</tr>
</tbody>
</table>

\[ T = 2\pi \sqrt{\frac{225.71}{(32.2 \times 12) \times 145.91}} = 0.40 \text{ sec} \]

Ratio of periods:

\[ \frac{0.40}{0.41} = 0.98 \leq 1.1 \implies \text{okay} \]

2c. Design of Flexible Upper Portion

Design coefficients for the Seismic Force-Resisting System (SFRS) from ASCE 7-05 Table 12.2-1 are as follows:

Type A-13: Light-framed walls with wood sheathing
- \( R = 6.5 \)
- \( \Omega_0 = 3.0 \)
- \( C_d = 4.0 \)

Maximum building height:
- No height limit for seismic design categories B & C
- 65 feet for seismic design categories D, E & F
The flexible upper portion will be designed using the seismic response coefficient $R = 6.5$ and the redundancy factor $\rho$ for that portion.

2d. Design of Rigid Lower Portion
Design coefficients for the SFRS:

Usually $A1/A7$:

For special reinforced concrete shear walls
- $R = 5.0$
- $\Omega_0 = 2.5$
- $C_d = 5.0$

For special reinforced masonry shear walls
- $R = 5.0$
- $\Omega_0 = 2.5$
- $C_d = 3.5$

The rigid lower portion will be designed using the seismic response coefficient $R = 5.0$ and the redundancy factor $\rho$ for that portion.

3. Seismic Design of Flexible Upper Portion and Lower Rigid Portion

3a. Seismic Design of Flexible Upper Portion

**Figure 4. Typical Cross-section through Building**

NOTE FOR FIGURE 4:
If parallel chord trusses are used instead of pitched chord trusses, the overall building height can be reduced.
SEISMIC AND SITE DATA:
Seismic Design Category D

For building frame systems with light-frame walls sheathed with wood structural panels

\[ R = 6.5 \quad \text{ASCE 7-05 Table 12-2.1} \]

Redundancy factor \( \rho = 1.0 \) \quad \text{ASCE 7-05 §12.3.4.2}
(See section 3d)

**Design base shear is:**

\[ V = C_s W \quad \text{ASCE 7-05 Eq.12.8-1} \]

Note: design base shear is a strength design basis.

\[ C_s = \frac{S_S}{R} \quad \text{ASCE 7-05 Eq.12.8-2} \]

Where:

Site Class D (stiff soil)

Site Class D has been determined by a geotechnical investigation. Without a geotechnical investigation, Site Class D shall be used as the default value.

\[ I = 1.0 \]

\[ R = 6.5 \]

Values for \( S_S \) and \( S_I \) can be determined from ASCE 7-05 maps or from the U.S. Geological Survey (USGS) website, which provides the values by either zip code or longitude and latitude coordinates. It is recommended that the longitude and latitude coordinates (which can be obtained from the street address) be used.

USGS website link:

http://earthquake.usgs.gov/research/hazmaps/design

Download the JAVA Ground Motion Parameter Calculator and enter latitude and longitude.

\[ S_S = 1.809 \quad \text{ASCE 7-05 Figure 22-1} \]

**MAXIMUM VALUE IN DETERMINATION OF \( C_S \)** \quad \text{ASCE 7-05 §12.8.1.3}

For regular structures five stories or less in height and having a period of 0.5 seconds or less, ASCE 7-05 permits the value of \( S_S \) to be limited to 1.5. Since the structure in this design example has a “Type II” weight (mass) irregularity between the second and third floors, a vertical irregularity exists. It is not clear whether a building that is designed using the two-stage analysis (ASCE 7-05 §12.2.3.1) should be exempted from this provision. Since each structure can be treated separately, it seems reasonable to conclude that the weight mass irregularity does not apply in the two-stage design approach. However, this design example does not exempt the irregularity and hence the cutoff value for \( S_S \) is not used. For actual projects, building officials in the local jurisdiction should be contacted for their interpretation of the code.
$S_I = 0.692$  \hspace{1cm} \textit{ASCE 7-05 Figure 22-2}

$F_a = 1.0$  \hspace{1cm} \textit{ASCE 7-05 Table 11.4-1}

$F_v = 1.5$  \hspace{1cm} \textit{ASCE 7-05 Table 11.4-2}

$S_{MS} = F_a S_S = 1.0(1.809) = 1.809$  \hspace{1cm} \textit{ASCE 7-05 Eq. 11.4-1}

$S_{M1} = F_v S_I = 1.5(0.692) = 1.038$  \hspace{1cm} \textit{ASCE 7-05 Eq. 11.4-2}

$S_{DS} = \frac{2}{3} S_{MS} = \frac{2}{3} (1.809) = 1.206$  \hspace{1cm} \textit{ASCE 7-05 Eq. 11.4-3}

$S_{D1} = \frac{2}{3} S_{M1} = \frac{2}{3} (1.038) = 0.692$  \hspace{1cm} \textit{ASCE 7-05 Eq. 11.4-4}

Values for $T_L$ (long-period transition period) are obtained from ASCE 7-05 maps and are used in formula 12.8-3 for determining the cut-off value of $C_s$ below.

$T_L = 4 \text{ sec}$  \hspace{1cm} \textit{ASCE 7-05 Figure 22-15}

$C_s = \frac{1.206}{\frac{6.5}{1.0}} = 0.186$

The seismic response coefficient need not exceed:

$C_s = \frac{S_{D1}}{T (\frac{R}{I})} = \frac{0.692}{0.45 \frac{6.5}{1.0}} = 0.236$  \hspace{1cm} \textit{ASCE 7-05 Eq. 12.8-3}

For $T \leq T_L$

The seismic response coefficient shall not be less than:

$C_s = 0.01$  \hspace{1cm} \textit{ASCE 7-05 Eq. 12.8-5}$

In addition, for structures located where $S_I$ is equal to or greater than 0.6g:

$C_s = \frac{0.55 I}{R (\frac{R}{I})} = \frac{0.5 \times 0.692}{0.45 \frac{6.5}{1.0}} = 0.053$  \hspace{1cm} \textit{ASCE 7-05 Eq. 12.8-6}

$\therefore V = 0.186W$

For the flexible upper portion:

$W = 2,520 \text{ k}$

$V = C_s W = 0.186 \times 2,520 = 469 \text{ k}$
For the building as a whole using the same $R = 6.5$:

$W = 5,152 \text{ k}$

$V = C_S W = 0.186 \times 5,152 = 958 \text{ k}$

**VERTICAL DISTRIBUTION OF FORCES**  
*ASCE 7-05 §12.8.3*

The biggest advantage of using a two-stage design is that the base for the upper flexible portion is set on top of the podium slab. The heavy mass of the podium slab (second floor) is not inverted into the upper flexible portion of the structure. Hence, the base shear is based on the weight ($W$) of the structure that is above the podium slab.

The base shear must be distributed to each level. This is done as follows:

- $F_x = C_v \chi V$  
  *ASCE 7-05 Eq.12.8-11*

- $C_{vx} = \frac{w_x h_x}{\sum w_i h_i}$  
  *ASCE 7-05 Eq.12.8-12*

Where $h_x$ is the average height at level $i$ of the sheathed diaphragm in feet above the base, $k$ is a distribution exponent related to the building period.

Since $T = 0.45$ second $< 0.5$ seconds, $k = 1$

Determination of $F_x$ is shown in Table 3.

Note that the vertical distribution of seismic forces using the base of the structure at the first floor (Table 3A) produces overly conservative results due to the tall first floor of 22 feet. For illustrative purposes, the vertical distribution of seismic forces including the second floor (without the two-stage analysis) and using the $R$ coefficient of 6.5 for the wood sheathed walls is included in Table 3B. However, this design example uses the vertical distribution of seismic forces using the base of the structure at the second floor (Table 3) using the two-stage analysis.

**Table 3. Vertical distribution of seismic forces (with base at second floor)**

<table>
<thead>
<tr>
<th>Level</th>
<th>$w_x$</th>
<th>$h_x$</th>
<th>$w_x h_x$</th>
<th>$w_x h_x$</th>
<th>$F_x$</th>
<th>$F_x$</th>
<th>$F_{tot}$</th>
<th>$F_x$</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td>$\sum w_i h_i$</td>
<td></td>
<td>$A$ (psf)</td>
<td></td>
<td>$A$</td>
</tr>
<tr>
<td>Roof</td>
<td>587</td>
<td>48</td>
<td>28,176</td>
<td>42.2</td>
<td>197.9</td>
<td>0.337</td>
<td>197.9</td>
<td>16.49</td>
</tr>
<tr>
<td>5th Floor</td>
<td>639</td>
<td>30</td>
<td>19,170</td>
<td>28.7</td>
<td>134.6</td>
<td>0.211</td>
<td>332.5</td>
<td>11.22</td>
</tr>
<tr>
<td>4th Floor</td>
<td>647</td>
<td>20</td>
<td>12,940</td>
<td>19.4</td>
<td>91.0</td>
<td>0.141</td>
<td>423.5</td>
<td>7.58</td>
</tr>
<tr>
<td>3rd Floor</td>
<td>647</td>
<td>10</td>
<td>6,470</td>
<td>9.7</td>
<td>45.5</td>
<td>0.070</td>
<td>469.0</td>
<td>3.79</td>
</tr>
<tr>
<td>$\sum$</td>
<td>2,520</td>
<td>66,756</td>
<td>100.0</td>
<td>469.0</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Where: $A =$ area of the floor plate which is 12,000 square feet
Table 3A. Vertical distribution of seismic forces (with base at first floor) not including second floor in distribution

<table>
<thead>
<tr>
<th>Level</th>
<th>( w_x ) (k)</th>
<th>( h_x ) (ft)</th>
<th>( w_x h_x ) (k-ft)</th>
<th>( \frac{w_x h_x}{\sum w_i h_i} ) (%)</th>
<th>( F_x ) (k)</th>
<th>( \frac{F_x}{w_x} ) (k)</th>
<th>( F_{tot} ) (k)</th>
<th>( \frac{F_x}{A} ) (psf)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Roof</td>
<td>587</td>
<td>60</td>
<td>35,220</td>
<td>36.3</td>
<td>170.2</td>
<td>0.290</td>
<td>170.2</td>
<td>14.18</td>
</tr>
<tr>
<td>5th Floor</td>
<td>639</td>
<td>42</td>
<td>26,868</td>
<td>27.7</td>
<td>130.0</td>
<td>0.203</td>
<td>300.2</td>
<td>10.83</td>
</tr>
<tr>
<td>4th Floor</td>
<td>647</td>
<td>32</td>
<td>20,704</td>
<td>21.3</td>
<td>99.9</td>
<td>0.154</td>
<td>400.1</td>
<td>8.33</td>
</tr>
<tr>
<td>3rd Floor</td>
<td>647</td>
<td>22</td>
<td>14,234</td>
<td>14.7</td>
<td>68.9</td>
<td>0.106</td>
<td>469.0</td>
<td>5.74</td>
</tr>
<tr>
<td>∑</td>
<td>2,520</td>
<td>96,996</td>
<td>100.0</td>
<td>469.0</td>
<td></td>
<td></td>
<td>469.0</td>
<td></td>
</tr>
</tbody>
</table>

Table 3B. Vertical distribution of seismic forces (with base at first floor) including second floor in distribution

<table>
<thead>
<tr>
<th>Level</th>
<th>( w_x ) (k)</th>
<th>( h_x ) (ft)</th>
<th>( w_x h_x ) (k-ft)</th>
<th>( \frac{w_x h_x}{\sum w_i h_i} ) (%)</th>
<th>( F_x ) (k)</th>
<th>( \frac{F_x}{w_x} ) (k)</th>
<th>( F_{tot} ) (k)</th>
<th>( \frac{F_x}{A} ) (psf)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Roof</td>
<td>587</td>
<td>60</td>
<td>35,220</td>
<td>27.4</td>
<td>262.5</td>
<td>0.447</td>
<td>262.5</td>
<td>21.9</td>
</tr>
<tr>
<td>5th Floor</td>
<td>639</td>
<td>42</td>
<td>26,868</td>
<td>20.9</td>
<td>200.3</td>
<td>0.313</td>
<td>462.8</td>
<td>16.7</td>
</tr>
<tr>
<td>4th Floor</td>
<td>647</td>
<td>32</td>
<td>20,704</td>
<td>16.1</td>
<td>154.2</td>
<td>0.238</td>
<td>617.0</td>
<td>12.9</td>
</tr>
<tr>
<td>3rd Floor</td>
<td>647</td>
<td>22</td>
<td>14,234</td>
<td>11.1</td>
<td>106.3</td>
<td>0.164</td>
<td>723.3</td>
<td>8.86</td>
</tr>
<tr>
<td>2nd Floor</td>
<td>2,632</td>
<td>12</td>
<td>31,584</td>
<td>24.5</td>
<td>234.7</td>
<td>0.089</td>
<td>958.0</td>
<td>19.6</td>
</tr>
<tr>
<td>∑</td>
<td>5,152</td>
<td>128,610</td>
<td>100.0</td>
<td>958.0</td>
<td></td>
<td></td>
<td>958.0</td>
<td></td>
</tr>
</tbody>
</table>

3b. Assumption of Flexible Diaphragms

IBC §1613.6.1

ASCE 7-05 §12.3.1.1 allows wood diaphragms in one and two-family dwellings to be idealized as flexible diaphragms. Section 1613.6.1 of the IBC amends §12.3.1.1 of ASCE 7-05 by extending the use of flexible diaphragm design assumptions to most wood-framed structures, provided all of the following conditions are met:

1. Toppings of concrete are nonstructural and are a maximum of 1-1/2 inches thick.
2. Each line of vertical elements of the lateral force-resisting system complies with the allowable story drift.
3. Vertical elements of the lateral force-resisting system are light-frame structural walls sheathed with wood structural panels rated for shear resistance or steel sheets.
4. Portions of wood structural panel diaphragms that cantilever beyond the vertical elements of the lateral force-resisting system are designed in accordance with IBC §2305.2.5.

In this design example, the first condition is met since our structure does not exceed 1-1/2 inches of lightweight concrete.
Condition 2 is met since section 8c of this design example for drift check of typical shear wall complies with the allowable story drift.

Condition 3 is met since the design example includes wood-sheathed walls.

Condition 4 is met since the structure does not have any cantilever portions of the diaphragms.

3c. Flexible vs. Rigid Diaphragm Analysis
With the IBC’s extension of assumption of flexible diaphragms for most wood structures, the engineer is left to use judgment regarding whether to use flexible or rigid diaphragm analysis to determine shear distributions to the shear walls. With the uniformity of shear wall lengths and spacing in the building’s transverse direction (north-south), flexible diaphragm assumptions are certainly justifiable from a code compliance perspective.

Current industry standard is to consider rigidities of the shear walls in determining the horizontal distribution of lateral forces, either from an envelope method (highest from flexible diaphragm assumptions and rigid diaphragm assumptions) or by a distribution solely based on relative rigidities.

Some engineers designing structures similar to this design example will place shear walls at interior corridor walls (see Figure 2) and not place any lateral-resisting elements at the exterior walls (for longitudinal forces). This approach must utilize a rigid diaphragm design. Although some jurisdictions allow this type of design, it is not recommended from a performance perspective.

Engineers now have sophisticated design software available for designing structures of this type. With all that is available, many engineers still analyze “individual units.” Some engineers perform a rigid diaphragm analysis and a few perform envelope solutions. These varying designs all get permitted by local building officials and there is not a lot of continuity in the design process even within cities.

For this case study, an “envelope” design was utilized.

3d. Flexible Upper Portion Redundancy Factor
The redundancy factor ($\rho$) for the flexible upper portion is 1.0. Both conditions of ASCE 7-05 §12.3.4.2 have been met, though designers are only required to meet one of the two provisions.

3e. Seismic Design of Rigid Lower Portion
Since the center of mass of the flexible upper structure coincides with the center of mass of the rigid lower portion, the entire structure mass can be lumped together and applied at the center of the podium’s rigid diaphragm with the code-required eccentricities.

4. Code Requirements for use of Fire-Retardant-Treated Wood (FRTW)

Depending on the “code check” analysis performed by the architect, the proposed building may require a Type III construction. Type III construction requires the exterior walls to be constructed with noncombustible materials. As an exception to using noncombustible construction, section 602.3 of the IBC states that fire-retardant-treated wood (FRTW) framing complying with IBC §2303.2 is permitted for exterior wall assemblies with ratings of two-hours or less, basically allowing wood-frame construction for many structures where noncombustible materials are required.
The FRTW must comply with conditions in IBC sections 2303.2 and 2304.9.5 as follows:

**1) LABELING**

Fire-retardant-treated lumber and wood structural panels must be labeled and contain the following items:

A. Identification mark of the approved agency
B. Identification of the treating manufacturer
C. Name of the fire-retardant treatment
D. Species of the wood treated
E. Flame spread and smoke-developed index
F. Method of drying after treatment
G. Conformance with appropriate standards

If exposed to weather, damp or wet conditions, it must also include the words "No increase in the listed classification when subjected to the Standard Rain Test."

Sample labels for solid sawn framing lumber and plywood are shown in Figure 5. It should be noted that FRTW sheathing is only available in plywood; the amount of resins and waxes in oriented strand board (OSB) is too high for the treatment process.

**Figure 5. Sample Labels for FRTW**

![Sample Labels for FRTW](image)

**2) STRENGTH ADJUSTMENTS**

The IBC requires that lumber design values be adjusted for the treatment and take into account the anticipated temperatures and humidity. Each manufacturer must publish the adjustment factors for service temperatures (not less than 80°F) and for roof-framing members (elevated temperatures). The adjustment factors vary from manufacturer to manufacturer, and should be obtained from the ICC-ES Evaluation Report. A sample of two manufacturers’ strength adjustments are shown in Table 4.
### Table 4. Sample strength reduction factors for FRTW

<table>
<thead>
<tr>
<th>Design Property</th>
<th>FRTW Brand A</th>
<th>FRTW Brand B</th>
</tr>
</thead>
<tbody>
<tr>
<td>$F_b$</td>
<td>0.97</td>
<td>0.91</td>
</tr>
<tr>
<td>$F_t$</td>
<td>0.95</td>
<td>0.88</td>
</tr>
<tr>
<td>$F_c$</td>
<td>1.00</td>
<td>0.94</td>
</tr>
<tr>
<td>$F_v$</td>
<td>0.96</td>
<td>0.95</td>
</tr>
<tr>
<td>$E$</td>
<td>0.96</td>
<td>0.95</td>
</tr>
<tr>
<td>$F_c$</td>
<td>0.95</td>
<td>0.95</td>
</tr>
<tr>
<td>Fasteners</td>
<td>0.90</td>
<td>0.90</td>
</tr>
</tbody>
</table>

3) **EXPOSURE TO WEATHER**  
*IBC §2303.2.3*

When FRTW is exposed to weather, damp or wet conditions, the identifying label needs to indicate “EXTERIOR.”

4) **FASTENERS**  
*IBC §2304.9.5*

Fasteners in preservative-treated and fire-retardant-treated wood shall be of hot-dipped zinc-coated galvanized steel, stainless steel, silicon bronze or copper. Fasteners in contact with treated wood need to meet this requirement. Rods in the tie-down system pass through an oversized hole in the wood and do not need to meet this requirement.

5) **CUTTING AND NOTCHING**

Treated lumber must not be ripped or milled as this will invalidate the flame spread. However, where FRTW joists or rafters are ripped for drainage conditions and FRTW plywood is placed on top of the ripped edge, this is considered acceptable.

End cuts and holes are usually not permitted; check the product evaluation report for requirements.

Some treated wood suppliers require the untreated wood to be shipped to their plant (from the framing contractor) for treatment, then shipped to the site.

Some suppliers stock most “sawn lumber” (2x, 3x and 4x) for immediate shipping.

Treatment adds about 50 percent to the cost of the material for interior and 80 percent for exterior applications.

5. **Vertical Displacement (Shrinkage) in Multi-level Wood Framing**  
*IBC §2303.7*

Vertical displacement can be a significant problem in multi-level wood framing unless special considerations are accounted for during design and construction. Vertical displacement may be caused by one or a combination of the following:
WOOD SHRINKAGE

Both the IBC and NDS require that consideration be given to the effects of cross-grain dimensional changes (shrinkage) when lumber is fabricated in a green condition. In addition, IBC §2304.3.3 requires that bearing walls supporting more than two floors and a roof be analyzed for shrinkage of the wood framing, and that possible adverse effects on the structure be satisfactorily demonstrated to the building official.

A free “shrinkage calculator” can be downloaded from the Western Wood Products Association website at: www2.wwpa.org.

The total shrinkage in wood-framed buildings can be calculated by summing the estimated shrinkage of the horizontal lumber members in walls and floors (wall plates, sills and floor joists). Most of the shrinkage is cross grain. The amount of shrinkage parallel to grain (length of studs) is approximately 1/40 of the shrinkage perpendicular to grain (cross grain) and can be neglected.

This case study illustrates two methods for determining the amount of wood shrinkage:

5a. Comprehensive Shrinkage Estimation

For a dimensional change with the moisture content limits of 6 to 14 percent, the formula is:

\[ S = D_i \left[ C_T (M_F - M_i) \right] \]

Where:

- \( S \) = shrinkage (in inches)
- \( D_i \) = initial dimension (in inches)
- \( C_T \) = dimension change coefficient, tangential direction
  - \( C_T = 0.00319 \) for Douglas Fir-Larch
  - \( C_T = 0.00323 \) for Hem-Fir
  - \( C_T = 0.00263 \) for Spruce-Pine-Fir
- \( M_F \) = final moisture content (%)
- \( M_i \) = initial moisture content (%)

The formulas are from the Wood Handbook: Wood as an Engineering Material and Dimensional Stability of Western Lumber Products.

For a dimension change with moisture content limits greater than 6 to 14 percent where one of the values is outside of those limits, the formula is:

\[ S = \frac{D_i (M_F - M_i)}{30 \left( \frac{100}{S_T} \right) - 30 + M_i} \]

Where:

- \( S \) = shrinkage (in inches)
- \( D_i \) = initial dimension (in inches)
- \( S_T \) = tangential shrinkage (%) from green to oven dry
  - \( S_T = 7.775 \) for Douglas Fir-Larch
- \( M_F \) = final moisture content (%)
- \( M_i \) = initial moisture content (%)

The final moisture content \( (M_F) \) for a building is referred to as the equilibrium moisture content (EMC). The final equilibrium moisture content can be higher in coastal areas and lower in inland or desert areas. These ranges are normally from 6 to 15 percent (low to high). The Western Wood Products Association
The EMC can be calculated with this formula:

\[
EMC = \frac{1800}{W} \left[ \frac{KH + (K_1KH + 2K_1K_2K_2H^2)}{1-KH} \right]
\]

Where:

- \( W = 330 + (0.452)T + (0.00415)T^2 \)
- \( K = 0.791 + (0.000463)T - (0.000000844)T^2 \)
- \( H = \text{relative humidity} \) (%)
- \( K_1 = 6.34 + (0.000775)T - (0.0000935)T^2 \)
- \( K_2 = 1.09 + (0.0284)T - (0.0000904)T^2 \)
- \( T = \text{temperature} \) (°F)

For this design example, a final moisture content \( M_F \) (EMC) of 12.0 percent is used.

Project specifications call for all top plates and sill (sole) plates to be Douglas Fir-Larch “kiln dried” (KD) or “surfaced dried” (S-Dry). Kiln dried lumber or surfaced dried has a maximum moisture content of 19 percent and an average of 15 percent.

It might be more realistic to use a lower number than 19 percent in the calculation so as to not overestimate the shrinkage.

Typical floor framing has a 4x4 top plate and a 2x4 sole plate (see Figure 6).

Find the individual shrinkage of the two members:

**DETERMINE SHRINKAGE OF 4X4 TOP PLATE:**

Since our initial \( MC (M_i) \) is 19 percent and the final \( MC (M_p) \) is 12 percent, the equation is:

\[
S = \frac{D_i (M_p - M_i)}{30 (100)} = \frac{3.5 (12 - 19)}{30 (100)} = -0.065 \text{ inch}
\]

The final size of our 4x4 is:

3.5 - 0.065 = 3.435 inches

**5b. Quick Shrinkage Estimation**

A close approximation that is much more easily used to determine amount of shrinkage is:

\[
S = CD_i (M_F - M_i)
\]

Where:

- \( S = \text{shrinkage (inches)} \)
- \( C = \text{average shrinkage constant} \)
- \( C = 0.002 \)
- \( M_F = \text{final moisture content} \) (%)
- \( M_i = \text{initial moisture content} \) (%)

has downloadable documents listing EMC for all major U.S. cities for each month of the year. At the web address after login, click “Shrinkage” followed by “EMC Charts” (free user login with password is required): www2.wwpa.org/Shrinkage/EMCUSLocations1997/tabid/888/Default.aspx
**DETERMINE SHRINKAGE OF 4X4 TOP PLATE:**
Since our initial MC ($M_i$) is 19 percent and the final MC ($M_f$) is 12 percent, the equation is:

$$S = CD_i (M_f - M_i) = 0.002 \times 3.5 \times (12 - 19) = -0.049 \text{ inch}$$

The final size of our 4x4 is:

$$3.5 - 0.049 = 3.451 \text{ inches}$$

Note that this quick estimation is within 0.5 percent of the actual calculated dimension of 3.435 inches using the comprehensive formulas.

$$S = CD_i (M_f - M_i) = 0.002 \times 1.5 \times (12 - 19) = -0.021 \text{ inch}$$

**DETERMINE SHRINKAGE OF 2X4 SOLE PLATE:**

$$S = CD_i (M_f - M_i) = 0.002 \times 1.5 \times (12 - 19) = -0.021 \text{ inch}$$

---

**Figure 6. Typical Floor Framing at Wall**

**NOTES FOR FIGURE 6:**

1. Blocking above the sole plate is to provide a nailing surface for the finishes. An alternative detail could use two sole plates, but this will increase shrinkage amounts for the building.

2. Web stiffeners at joist hangers may be required depending on joist size and manufacturer.

3. Hangers for the floor joist are installed over the sheathing (gypsum, plywood or OSB) and must be rated/approved for this installation (e.g., Technical Bulletin from joist hanger manufacturer listing reduced allowable hanger loads).

4. This detail uses a 4x4 top plate. Use of double 2x plates (not depicted) is also common.

Total shrinkage per floor level with the 4x4 top plate and 2x4 sole plate:

$$S = 0.049 + 0.021 = 0.07 \text{ inch}$$
**Figure 6A. Typical Platform Floor Framing at Wall Using Sawn Joists**

**EXAMPLE CALCULATION**

**DETERMINE SHRINKAGE OF SAWN JOISTS WITH PLATFORM FRAMING (Figure 6A):**

\[ S = CD_i(M_F - M_i) = 0.002 \times 11.25 \times 12 - 19 = -0.158 \text{ inch} \]

Total shrinkage per floor level with the 4x4 top plate, 2x12 sawn joists and 2x4 sole plate:

\[ S = 0.049 + 0.021 + 0.158 = 0.228 \text{ inch} \]

**SETTLEMENT UNDER CONSTRUCTION GAPS (Consolidation):**

Small gaps can occur between plates and studs, caused by (among other things) mis-cuts (short studs) and the lack of square-cut ends. These gaps can account for up to 1/8 inch per story, where “perfect” workmanship would be 0 inches and a more “sloppy” workmanship would be 1/8 inch. This case study factors in gaps of 1/10 inch.

**DEFORMATION UNDER SUSTAINED LOADING:**

Wood beams that support walls can creep from the sustained loading. The “rate” of creep can be higher for beams that are loaded while “drying” under load, because the modulus of elasticity is lower for higher moisture contents. Appendix F of the NDS provides commentary related to creep in wood and recommends a (creep) deflection amplification factor of between 1.5 and 2.0 for computing deflections under sustained loads.
Table 5. Vertical Displacements

<table>
<thead>
<tr>
<th>Level</th>
<th>Vertical Displacement</th>
<th>Design Displacement (in.)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Per Floor</td>
<td>Cumulative</td>
</tr>
<tr>
<td>5th Floor</td>
<td>0.170</td>
<td>0.68</td>
</tr>
<tr>
<td>4th Floor</td>
<td>0.170</td>
<td>0.51</td>
</tr>
<tr>
<td>3rd Floor</td>
<td>0.170</td>
<td>0.34</td>
</tr>
<tr>
<td>2nd Floor</td>
<td>0.170</td>
<td>0.17</td>
</tr>
</tbody>
</table>

Where: Shrinkage of 0.07 inch + settlement of 0.10 inch = 0.170 inch

METHODS TO REDUCE VERTICAL DISPLACEMENT:

1. Use kiln-dried plates (MC < 19%) or even MC15 (MC < 15%) lumber or engineered lumber for plates.
2. Consider a single top plate instead of double top plate.
3. Consider balloon framing or a modified balloon framing.
4. Place floor joists in metal hangers bearing on beams or top plates instead of bearing on the top plates.
5. The site storage of the material stock can negate all design and planning when the material is not properly stored on the site. Lumber should be kept away from moisture sources and rain.

METHODS TO ACCOUNT FOR VERTICAL DISPLACEMENT:

1. Use continuous tie-down systems with shrinkage compensating devices in shear walls.
2. Architectural finish details near the floor lines need to account for vertical displacement.
3. Provide a 1/8-inch gap between window and door tops to the framing lumber.

6. Shear Wall Design Example

This design example features a four-story “segmented shear wall” with an out-to-out length of 29.0 feet and floor-to-floor heights of 10.0 feet. NDS-05 SDPWS §4.3.5.1 categorizes this wall type as having full-height wall segments with aspect ratio limitations of NDS-05 SDPWS §4.3.4 applying to each full height segment.

CHECK H/W RATIO FOR SHEAR WALL SEGMENTS:

Segment height = 10.0 feet
Segment width = 29.0 feet

\[
h/w = \frac{10.0}{29.0} = 0.34 < 2.0 \Rightarrow \text{okay}
\]

6a. Determination of Lateral Loads to Shear Wall

The structure used in this design example has interior shear walls located at every other wall between hotel guest units. The walls are spaced at 13 feet o.c., with the depth of the building equal to 65 feet.

Based on an “envelope” design using flexible diaphragm assumptions and a rigid diaphragm analysis, the critical forces to the interior shear wall (Figure 7) are shown in Table 6.
Figure 7. Typical Interior Shear Wall Elevation

Table 6. Distribution of seismic forces for both shear walls

<table>
<thead>
<tr>
<th>Level</th>
<th>Designation</th>
<th>$F_{Total}$ (lb)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Roof</td>
<td>$F_4$</td>
<td>13,935</td>
</tr>
<tr>
<td>5th Floor</td>
<td>$F_3$</td>
<td>23,415</td>
</tr>
<tr>
<td>4th Floor</td>
<td>$F_2$</td>
<td>29,820</td>
</tr>
<tr>
<td>3rd Floor</td>
<td>$F_1$</td>
<td>33,045</td>
</tr>
</tbody>
</table>
6b. Determination of Shear Wall Sheathing and Nailing

The shear wall to be designed will use 15/32-inch Structural I rated sheathing using 10d common nails with a minimum penetration of 1-1/2 inches into the framing members.

A 2x4 sole plate (sill plate) will be used at the base of the shear wall. There is a discrepancy between the IBC and the SDPWS on 3x nominal framing requirements:

Footnote e in IBC Table 2306.4.1 reads:

Framing at adjoining panel edges shall be 3 inches nominal or wider, and nails shall be staggered where nails are 2 inches o.c.

SDPWS section 4.3.7.1, item 3c, states that:

3x nominal framing is required when the required nominal shear capacity exceeds 700 plf in Seismic Design Category (SDC) D, E or F.

### Table 7. Determination of shear wall nailing

<table>
<thead>
<tr>
<th>Designation</th>
<th>$F_{Total}$ (lb)</th>
<th>Wall Length $l$ (ft)</th>
<th>ASD Design $V = \frac{F_{Total}(0.7)}{l}$, Wall Sheathed 1 or 2 sides (plf)</th>
<th>Allowable Shear $a$ (plf)</th>
<th>Fastener Edge Spacing $b$ $c$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$F_4$</td>
<td>13,935</td>
<td>29.0</td>
<td>340</td>
<td>1</td>
<td>340</td>
</tr>
<tr>
<td>$F_3$</td>
<td>23,415</td>
<td>29.0</td>
<td>565</td>
<td>1</td>
<td>665</td>
</tr>
<tr>
<td>$F_2$</td>
<td>29,820</td>
<td>29.0</td>
<td>720</td>
<td>1</td>
<td>870</td>
</tr>
<tr>
<td>$F_1$</td>
<td>33,045</td>
<td>29.0</td>
<td>800</td>
<td>1</td>
<td>870</td>
</tr>
</tbody>
</table>

a. Allowable shear values are obtained by taking the nominal unit shear capacities in NDS-05 SDPWS Table 4.3A and dividing by the ASD reduction factor of 2.0.

b. A 2x4 sole plate (sill plate) will be used at the base of walls (see Figure 6) with the exception of the bottom wall (on the podium slab) which requires a 2x sill plate. For 10d common nails spaced at 2 inches o.c., the nails are staggered. From a constructability standpoint (framer bent over to install nails) and for improved structural performance (larger edge distance), the use of a 3x sole plate is recommended.

c. Where fastener spacing is 2 inches o.c., some engineers may use sheathing on both sides of the wall with fasteners spaced at 4 inches o.c. for better performance and less drift.

6c. Shear Transfer at Top of Wall

The shear transfer at the top of the fifth floor wall is achieved with framing clips located at the bottom of the roof truss chord (see Figure 8). The collector truss is specified based on the vertical and lateral loading combinations including lateral collector loads.
Figure 8. Shear Transfer at Top of Wall

NOTES FOR FIGURE 8:

1. Diaphragm shear at collector truss:

\[ v = \frac{27,870 \text{ lb} \times 0.7}{65.0 \text{ ft}} = 300 \text{ plf} \]

where 27,870 lb is from Table 6.

2. Diaphragm nailing needs to accommodate one row of fasteners (boundary nailing). Using 8d common nails with 15/32-inch rated sheathing spaced at 4 inches o.c. with 2x nominal framing members, the allowable shear is 360 plf (IBC Table 2306.3.1).

3. The collector truss should be looked at for possible uplift forces and straping from truss to shear wall ends may be necessary.

4. Area separation walls may need a special truss with “flat members” or a doubled truss.
6d. Shearwall Cumulative Overturning Forces

When designing overturning forces in multi-level structures, shear and the respective overturning forces due to seismic (or wind) must be carried down to the foundation, or in this design example the podium slab, by the boundary studs and continuous tie-down system. These forces are cumulative over the height of the building, and shear forces applied at the upper levels will generate much larger base overturning moments than if the same shear forces were applied at the lower story.

The overturning forces for the shear wall (Figure 7) can be obtained by summing forces about the base of the wall for the level being designed.

Cumulative overturning force for the fifth floor level:
\[ M_{ot} = F_4 (H_4) \]

Cumulative overturning force for the fourth floor level:
\[ M_{ot} = F_4 (H_4 + H_3) + F_3 (H_3) \]

Cumulative overturning force for the third floor level:
\[ M_{ot} = F_4 (H_4 + H_3 + H_2) + F_3 (H_3 + H_2) + F_2 (H_2) \]

Cumulative overturning force for the second floor level:
\[ M_{ot} = F_4 (H_4 + H_3 + H_2 + H_1) + F_3 (H_3 + H_2 + H_1) + F_2 (H_2) + F_1 (H_1) \]

In shear walls with continuous tie-down systems, the overturning resistance in the shear wall is resisted by the posts and/or end studs resisting the compression forces and the tension rods resisting the tension forces.

In shear walls with conventional holdown systems, the overturning resistance in the shear wall is resisted by the posts and/or end studs resisting the compression forces and the tension forces.

6e. Load Combinations using 2006 IBC

IBC Section 1605.3.2 has alternative basic load combinations to ASCE 7-05. For allowable stress design, the earthquake load combinations are:

\[ D + L + S + \frac{E}{1.4} \quad \text{IBC Eq.16-20} \]

Since \( S \) is not present, the simplified load combination is:

\[ D + L + \frac{E}{1.4} \]

Where \( E \) = the horizontal seismic force (F):

\[ 0.9D + \frac{E}{1.4} \quad \text{IBC Eq.16-21} \]

6f. Load Combinations using ASCE 7-05

§12.4.2.3 Per Section 12.4.2.3, the following load combinations shall be used for basic combinations for allowable stress design:

\[ (1.0 + 0.14SDS)D + H + F + 0.7pQ_E \quad \text{ASCE 7-05 Eq. 5} \]

\[ (1.0 + 0.105SDS)D + H + F + 0.525pQ_E + 0.75L + 0.75(L_f \text{ or } S \text{ or } R) \quad \text{ASCE 7-05 Eq. 6} \]

\[ (0.6 - 0.14SDS)D + 0.7pQ_E + H \quad \text{ASCE 7-05 Eq. 8} \]
Where the dead load $D$ is increased (or decreased) for vertical accelerations by the $S_{DS}$ coefficient.

Since $H$, $F$, $S$ and $R$ are not present, the simplified load combinations are:

$$\begin{align*}
(1.0 + 0.14S_{DS})D + 0.7pQ_E & \quad \text{ASCE 7-05 Eq. 5} \\
(1.0 + 0.105S_{DS})D + 0.525pQ_E + 0.75L + 0.75L_r & \quad \text{ASCE 7-05 Eq. 6} \\
(0.6 + 0.14S_{DS})D + 0.7pQ_E & \quad \text{ASCE 7-05 Eq. 8}
\end{align*}$$

Where $Q_E$ = the horizontal seismic force $F$.

$$\begin{align*}
0.105S_{DS} &= 0.105 \times (1.206) = 0.13 \\
0.14S_{DS} &= 0.14 \times (1.206) = 0.17
\end{align*}$$

6g. Shearwall Chord (Boundary) Members

The vertical members at the end of the shear walls are the walls’ chords (boundary members). As in a diaphragm, the chords resist flexure and the sheathing (web) resist the shear. The overturning moment is resolved into a T-C couple creating axial tension and compression forces. When considering only the horizontal component of the seismic forces, the tension and compression forces are equal and opposite. The overturning compressive force is determined by dividing the overturning moment by the distance “d” between the center of the tension rod and the center of the compression posts (Figure 9). However, in most designs, the size and number of chords (boundary members) change from story to story as shown in Figures 10 and 11, which can necessitate iterations to derive the actual distance “d.” Many engineers will take a “conservative average” distance “d” and use the same value for all cases to minimize iterations.

Figure 9 illustrates multiple boundary members that are common to multi-level wood-framed shear walls.

The axial loads to the bearing wall and boundary members are determined from the following loads:

Dead loads:

$$\begin{align*}
W_{Roof} &= (28.0 \text{ psf})(2.0 \text{ ft}) = 56.0 \text{ plf} \\
W_{Roof} &= (30.0 \text{ psf})(13.0 \text{ ft}) = 390 \text{ plf} \\
W_{Wall} &= (10.0 \text{ psf})(10.0 \text{ ft}) = 100.0 \text{ plf}
\end{align*}$$

Live loads:

$$\begin{align*}
W_{Roof} &= (20.0 \text{ psf})(2.0 \text{ ft}) = 40.0 \text{ plf} \\
W_{Floor} &= (40.0 \text{ psf})(13.0 \text{ ft}) = 520 \text{ plf}
\end{align*}$$

Dead + live loads:

$$\begin{align*}
W_{Roof} &= (28.0 \text{ psf} + 20.0 \text{ psf})(2.0 \text{ ft}) = 96.0 \text{ plf} \\
W_{Floor} &= (30.0 \text{ psf} + 40.0 \text{ psf})(13.0 \text{ ft}) = 910 \text{ plf} \\
W_{Wall} &= 10.0 \text{ psf}(10.0 \text{ ft}) = 100.0 \text{ plf}
\end{align*}$$

$(1.2 + 0.2S_{DS})$ dead + live loads:

Per section 12.4.2.3 of ASCE 7-05, the load factor on $L$ is permitted to be 0.5 since the live load is equal to or less than 100 psf and not of public assembly. The 0.5 factor will be used in the live load determinations below:

$$\begin{align*}
W_{Roof} &= ((1.4 \times 28.0 \text{ psf}) + (0.5 \times 20.0 \text{ psf}))(2.0 \text{ ft}) = 98.5 \text{ plf} \\
W_{Floor} &= ((1.4 \times 30.0 \text{ psf}) + (0.5 \times 40.0 \text{ psf}))(13.0 \text{ ft}) = 806 \text{ plf} \\
W_{Wall} &= 1.4 \times 10.0 \text{ psf}(10.0 \text{ ft}) = 140.0 \text{ plf}
\end{align*}$$
NOTES FOR FIGURES 10 AND 11:
1. Some continuous rod systems favor centering the rod between symmetrical amounts of posts (concentric with the tension rod), while other continuous rod systems favor an asymmetrical orientation of posts (shown in Figures 10 and 11).
2. See Figures 13, 14 and 15 for comments on blocking at the floor framing.

Figure 9. Shear Wall Elevation with Distance D

Figure 10. Example Elevation of Shear Wall Boundary Members
For ASD compression on the chord members, the alternate basic load combination is used.

\[ D + L + \frac{E}{1.4} \quad \textit{IBC Eq. 16-20} \]

For strength compression on the chord members, the ASCE 7-05 seismic load combination will be used. The strength compression loads are used later in this example to determine the shear wall deflection at strength loads (sill plate crushing). Per ASCE 7-05 sections 12.8.6 and 12.12.1, strength level forces are required for the determination of shear wall deflections.

\[(1.2 + 0.2SD_S)D + \rho Q_E + L + 0.2S\]

Where:

\[ \rho Q_E = E \]

Since \( S \) is not present, the simplified load combination is:

\[(1.2 + 0.2SD_S)D + L + E\]

Where:

\[(1.2 + 0.2SD_S) = (1.2 + 0.2 \times 1.206) = 1.4\]

\[ E = \frac{M_{OT}}{d} \]
Table 8. Determination of shear wall chord member forces

<table>
<thead>
<tr>
<th>Level</th>
<th>(M_{OT})</th>
<th>ASD</th>
<th>(d')</th>
<th>(d)</th>
<th>ASD Demand Compression</th>
<th>Strength Demand Compression</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>(ft-k)</td>
<td>(k)</td>
<td>(ft)</td>
<td>(ft)</td>
<td>(k)</td>
<td>(k)</td>
</tr>
<tr>
<td>Roof</td>
<td>139.35</td>
<td>0.38</td>
<td>0.98</td>
<td>27.04</td>
<td>4.06</td>
<td>5.62</td>
</tr>
<tr>
<td>5th Floor</td>
<td>373.50</td>
<td>2.36</td>
<td>0.98</td>
<td>27.04</td>
<td>12.23</td>
<td>16.13</td>
</tr>
<tr>
<td>4th Floor</td>
<td>671.70</td>
<td>7.00</td>
<td>1.58</td>
<td>26.44</td>
<td>25.15</td>
<td>32.13</td>
</tr>
<tr>
<td>3rd Floor</td>
<td>1,002.1</td>
<td>10.19</td>
<td>1.58</td>
<td>26.44</td>
<td>37.26</td>
<td>47.62</td>
</tr>
</tbody>
</table>

Where: \(P_{D+L} = w(d')^2\)

FOR ASD DEMAND (see section 6g):

\(P_{D+L\,\text{Roof}} = (96 \text{ plf} + 100 \text{ plf})(0.98 \times 2) = 0.384 \text{ k}\)

\(P_{D+L\,\text{5thFloor}} = (910 \text{ plf} + 100 \text{ plf})(0.98 \times 2) + P_{\text{Roof}} = 2.36 \text{ k}\)

\(P_{D+L\,\text{4thFloor}} = ((910 \text{ plf} + 100 \text{ plf})^2 + (96 + 100))(1.58 \times 2) = 7.00 \text{ k}\)

\(P_{D+L\,\text{3rdFloor}} = ((910 \text{ plf} + 100 \text{ plf})^3 + (96 + 100))(1.58 \times 2) = 10.19 \text{ k}\)

FOR STRENGTH DEMAND (see section 6g):

\((1.2 + 0.02SDSD)D + L = 1.4D + L\)

\(P_{D+L\,\text{Roof}} = (98.5 \text{ plf} + 140 \text{ plf})(0.98 \times 2) = 0.467 \text{ k}\)

\(P_{D+L\,\text{5thFloor}} = (806 \text{ plf} + 140 \text{ plf})(0.98 \times 2) + P_{\text{Roof}} = 2.32 \text{ k}\)

\(P_{D+L\,\text{4thFloor}} = ((806 \text{ plf} + 140 \text{ plf})^2 + (98.5 + 140))(1.58 \times 2) = 6.73 \text{ k}\)

\(P_{D+L\,\text{3rdFloor}} = ((806 \text{ plf} + 140 \text{ plf})^3 + (98.5 + 140))(1.58 \times 2) = 9.72 \text{ k}\)

Table 9. Determination of shear wall chord members

<table>
<thead>
<tr>
<th>Level</th>
<th>Chord Posts</th>
<th>Total Area</th>
<th>(l_e) (ft)</th>
<th>(C_f)</th>
<th>(C_p)</th>
<th>Bearing Cap. (kips)</th>
<th>ASD Demand (kips)</th>
<th>Stability Capacity (kips)</th>
<th>D/C Ratio</th>
</tr>
</thead>
<tbody>
<tr>
<td>Roof</td>
<td>4-3x4</td>
<td>35.0</td>
<td>9.625</td>
<td>1.15</td>
<td>0.163</td>
<td>21.88</td>
<td>4.06</td>
<td>15.79</td>
<td>0.26</td>
</tr>
<tr>
<td>5th Floor</td>
<td>4-3x4</td>
<td>35.0</td>
<td>9.625</td>
<td>1.15</td>
<td>0.163</td>
<td>21.88</td>
<td>12.23</td>
<td>15.79</td>
<td>0.77</td>
</tr>
<tr>
<td>4th Floor</td>
<td>4-4x8</td>
<td>101.5</td>
<td>9.625</td>
<td>1.05</td>
<td>0.187</td>
<td>63.44</td>
<td>25.15</td>
<td>46.48</td>
<td>0.54</td>
</tr>
<tr>
<td>3rd Floor</td>
<td>4-4x8</td>
<td>101.5</td>
<td>9.625</td>
<td>1.05</td>
<td>0.187</td>
<td>63.44</td>
<td>37.26</td>
<td>46.48</td>
<td>0.80</td>
</tr>
</tbody>
</table>
Notes:
1. \( C_d = 1.6 \)
2. Bearing capacity (on sole plate) = \( F'_{c\perp} AC_b \)
3. Column bearing factor \( C_b = 1.0 \)
4. Column stability factor
   \[
   C_p = \frac{1 + (F_{ce}E/F_{c*})}{2c} \cdot \sqrt{\left[\frac{1 + (F_{ce}E/F_{c*})}{2c}\right]^2 - \frac{F_{ce}E/F_{c*}}{c}}
   \]
5. Column stability capacity = \( F_{CC}C_D C_{f} C_{P} A \)

Example for four 4x8 posts: 4x 11.62 = 46.48 kips

6. The typical interior stud wall is framed with 4-inch nominal framing studs.
7. Interior bearing walls for this design example are non-rated and, as such, would not require the reduction in allowable loads.

**6h. Example Compression Member Capacity Determination**

**4X8 POST – DOUGLAS FIR-LARCH NO. 1:**

Where:
- \( A = 25.375 \text{ in}^2 \)
- \( C_D = 1.6 \)
- \( E_{min} = 620,000 \text{ psi} \)
- \( d_1 = 3.5 \text{ in.} \)

The following coefficients for \( C_m \) and \( C_t \) are not referenced in the NDS formulas (for simplicity).
- \( C_m = 1.0 \)
- \( C_t = 1.0 \)
- \( K_e = 1.0 \)

The members’ span between the top of the 2x4 sill plate and the underside of the 4x4 top plate (see Figure 5).
- \( l = 9.52 \text{ feet} \)
- \( l_{e1} = 9.52 \times 12 = 114 \text{ inches} \)
- \( l_{e1}/d_1 = 114/3.5 = 32.64 \)

Slenderness is controlled by the minor axis and is thus used in the \( F_{CE} \) calculation.

**Compression parallel to grain:**

- \( F'_{c} = F_{c} C_D C_F C_P \)
- \( F_{c*} = F_{ce} C_D C_F = 1,500 \times 1.6 \times 1.05 = 2,520 \text{ psi} \)

\[
C_p = \frac{1 + (F_{ce}E/F_{c*})}{2c} \cdot \sqrt{\left[\frac{1 + (F_{ce}E/F_{c*})}{2c}\right]^2 - \frac{F_{ce}E/F_{c*}}{c}} = 0.1817 \quad \text{NDS Eq. 3.7-1}
\]
Where:

\[ c = 0.8 \]

\[ F_{cE} = \frac{0.822E_{min}}{(l_e/d)^2} = \frac{0.822 \times 620,000}{32.64^2} = 478.4 \text{ psi} \]

\[ \frac{F_{cE}}{F_c^*} = \frac{478.4}{2,520} = 0.1898 \]

\[ F_c' = F_{C_D}C_FC_p = 1,500 \times 1.6 \times 1.05 \times 0.1817 = 458 \text{ psi} \]

FOR A 4X8 POST:

\[ P_{allow} = A \times F_c' = 25.375 \times 458 = 11,620 \text{ lbs} \]

Compression perpendicular to grain:

\[ F_{c\perp} = 625 \text{ psi} \]

FOR A 4X8 POST:

\[ P_{allow} = A \times F_{c\perp} = 25.375 \times 625 = 15,860 \text{ lbs} \]

6i. Determine Resisting Moments and Uplift Forces

The resisting moment \( M_R \) is determined from the following dead loads:

\[
W_{Roof} = 28.0 \text{ psf (2.0 ft)} = 56.0 \text{ plf}
\]

\[
W_{Floor} = 30.0 \text{ psf (13.0 ft)} = 390.0 \text{ plf}
\]

\[
W_{Wall} = 10.0 \text{ psf (10.0 ft)} = 100.0 \text{ plf}
\]

Tables 10 and 10A illustrate the differences in ASD uplift values that can be calculated from using the ASCE 7-05 formula and the alternate IBC formula. For this case study, the ASCE 7-05 equation in Table 11 is used.

**Table 10. Determine shear wall uplift forces using ASCE 7-05 load combinations**

<table>
<thead>
<tr>
<th>Level</th>
<th>( M_R ) (ft-lb)</th>
<th>( d ) (ft)</th>
<th>Strength</th>
<th>ASD Uplift</th>
<th>Differential Load Per Floor</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>( M_{OT} ) (ft)</td>
<td>( (M_{OT} \times 0.7) - (0.6 - 0.14S_{DS})M_R ) d (lb)</td>
<td>( (M_{OT} \times 0.7) - (0.6 - 0.14S_{DS})M_R ) d (lb)</td>
<td>( (M_{OT} \times 0.7) - (0.6 - 0.14S_{DS})M_R ) d (lb)</td>
<td></td>
</tr>
<tr>
<td>Roof</td>
<td>65,600</td>
<td>27.04</td>
<td>139,350</td>
<td>28,210</td>
<td>2,565</td>
</tr>
<tr>
<td>5th Floor</td>
<td>271,645</td>
<td>27.04</td>
<td>373,500</td>
<td>116,805</td>
<td>5,350</td>
</tr>
<tr>
<td>4th Floor</td>
<td>477,690</td>
<td>26.44</td>
<td>671,700</td>
<td>205,405</td>
<td>10,015</td>
</tr>
<tr>
<td>3rd Floor</td>
<td>683,735</td>
<td>26.44</td>
<td>1,002,100</td>
<td>294,005</td>
<td>15,410</td>
</tr>
</tbody>
</table>

\(^1\) Where \((0.6 - 0.14S_{DS}) = (0.6 - 0.14 \times 1.206) = 0.43\)
Table 10A. Determine shear wall uplift forces using IBC alternate load combinations

<table>
<thead>
<tr>
<th>Level</th>
<th>$MR$ (ft-lb)</th>
<th>$d$ (ft)</th>
<th>Strength</th>
<th>ASD Uplift</th>
<th>Differential Load Per Floor</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
<td>$M_{OT}$</td>
<td>($M_{OT} / 1.4 - 0.9MR$)</td>
<td>$d$ (lb)</td>
</tr>
<tr>
<td>Roof</td>
<td>65,600</td>
<td>27.04</td>
<td>139,350</td>
<td>1,500</td>
<td>0</td>
</tr>
<tr>
<td>5th Floor</td>
<td>271,645</td>
<td>27.04</td>
<td>373,500</td>
<td>825</td>
<td>-675</td>
</tr>
<tr>
<td>4th Floor</td>
<td>477,690</td>
<td>26.44</td>
<td>671,700</td>
<td>1,885</td>
<td>2,560</td>
</tr>
<tr>
<td>3rd Floor</td>
<td>683,735</td>
<td>26.44</td>
<td>1,002,100</td>
<td>3,800</td>
<td>1,915</td>
</tr>
</tbody>
</table>

Notes for Table 10A: A “negative” differential load is a result of a higher resisting moment and occurs at a lower level than above.

6j. Shearwall Tie-down System Components

TIE-DOWN RODS
Tie-down rods are usually made from A36/A307 steel. This is called standard rod strength. Unless marked, rods should be considered standard rod strength. High-strength rods are A449 or A193-B7 and are usually marked on the end with an embossed stamp, though some rod manufacturers stamp the rod grade on the side. If the rod is stamped at the end and is cut, it needs to be re-marked. High-strength rods should have special inspection to confirm the rod type since the ends of these rods may be embedded into a coupler where the marks cannot be seen after installation. It should be noted that high-strength rods are not weldable. Proprietary systems have special rod colors and markings on the sides. The rods and tie-down systems are not proprietary, but the manufactured components are.

TIE-DOWN ELONGATION
Tie-down rod elongation is computed between bearing plates (restraints). This design example has bearing plates located at each floor. Table 11 computes the rod capacities and elongations (per floor) between the bearing plates.

Table 11. Determine rod sizes, capacities and elongations

<table>
<thead>
<tr>
<th>Level</th>
<th>Plate Height (ft)</th>
<th>Tension Demand (kips)</th>
<th>Rod Dia. $d$ (in)</th>
<th>Eff. Dia. $d_e$ (in)</th>
<th>$Ag$ $(in^2)$</th>
<th>$Ae$ $(in^2)$</th>
<th>$F_u$ (ksi)</th>
<th>$F_y$ (ksi)</th>
<th>Allow Rod Capacity $(.75F_u *Ag/2)$ (kips)</th>
<th>Rod Elong. (in)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Roof</td>
<td>10.0</td>
<td>2.56</td>
<td>0.625</td>
<td>0.560</td>
<td>0.307</td>
<td>0.226</td>
<td>60</td>
<td>43</td>
<td>6.91</td>
<td>0.047</td>
</tr>
<tr>
<td>5th Floor</td>
<td>10.0</td>
<td>5.35</td>
<td>0.625</td>
<td>0.560</td>
<td>0.307</td>
<td>0.226</td>
<td>60</td>
<td>43</td>
<td>6.91</td>
<td>0.098</td>
</tr>
<tr>
<td>4th Floor</td>
<td>10.0</td>
<td>10.0</td>
<td>0.625</td>
<td>0.560</td>
<td>0.307</td>
<td>0.226</td>
<td>120</td>
<td>92</td>
<td>13.82</td>
<td>0.183</td>
</tr>
<tr>
<td>3rd Floor</td>
<td>10.0</td>
<td>15.4</td>
<td>0.875</td>
<td>0.796</td>
<td>0.601</td>
<td>0.462</td>
<td>120</td>
<td>92</td>
<td>27.05</td>
<td>0.138</td>
</tr>
</tbody>
</table>
Notes:
1. Tension demand (ASD uplift) values are computed in Table 10.

2. Rod area: 
\[ Ag = \frac{3.14d^2}{4} \]

3. Net tensile area \( A_e \) is from AISC Table 7-18.

4. Standard rod is ASTM A36 rod with minimum \( F_u = 58 \text{ ksi} \), \( F_y = 36 \text{ ksi} \).
   High-strength rod is ASTM A193 rod with minimum \( F_u = 125 \text{ ksi} \), \( F_y = 105 \text{ ksi} \) for rods up to 2-1/2 inches in diameter and A449 rod with minimum \( F_u = 120 \text{ ksi} \), \( F_y = 105 \text{ ksi} \) for rods up to 1 inch in diameter then drops to \( F_y = 105 \text{ ksi} \) for larger rods.

5. Allowable rod capacity for the *AISC Steel Construction Manual Thirteenth Edition* is:
\[ \frac{0.75F_u A_g}{2} \]

6. Rod elongation:
\[ \Delta = \frac{P_L}{A_e E} \]

Where:
- \( \Delta \) = the elongation of the rod in inches
- \( P \) = the accumulated uplift tension force on the rod in kips (tension demand)
- \( L \) = length of rod in inches from bearing restraint to bearing restraint, with the bearing restraint being where the load is transferred to the rod
- \( E = 29,000 \text{ ksi} \)
- \( A_e \) = the effective area of the rod in square inches

When smooth rods are used, the area is equal to the gross area \((A_g)\). When threaded (all-thread) rods are used, the area is equal to the tension area \((A_e)\) of the threaded rod. Since many of the proprietary systems that have smooth rods have long portions threaded at the ends, it is recommended that \( A_e \) be used when calculating rod elongation.

7. Rod elongation is based on using the effective area \((A_e)\) and the following lengths:
   a. For the first level, the anchor bolt is projecting 4 inches above the foundation (height of coupler nut to anchor bolt at podium slab).
   b. For the framed floors, the rod from below is projecting 6 inches above the sole plate.

**ROD COUPLERS**
Coupplers are used to connect the rods. Couplers can either be straight or reducing and can be supplied in different strengths or grades. Couplers for high-strength rods need to be of high-strength steel and are marked with notches or marks on the coupler. For a rod to develop its full strength, the rod must be a set amount (usually the depth of a standard nut). It is recommended that, when couplers are used, they have “pilot” or “witness” holes in the side so the threads of the rods can be witnessed in the holes to ensure proper embedment.

Reducing couplers are used when the rod size is changed. In reducing couplers, the size of the threading changes at the middle of the coupler device. It is intended that the rods be embedded until they bottom out at the center of the coupler. If the rods are installed in this fashion, “witness” holes will not be necessary; however, it is recommended that couplers with witness holes be used so that proper installation can be confirmed by an inspector. Reducing couplers should have the same notches and identifying marks as straight couplers when used with high-strength rods.
BEARING PLATES

Bearing plates transfer the tension load from the structure, the sole plate or the top plates into the rod (see Figure 14). Premanufactured bearing plates are usually identified by paint color or by a number marked on the plate. However, paint colors or unpainted plates vary among different rod system manufacturers.

Table 12. Determine bearing plate sizes and capacities

<table>
<thead>
<tr>
<th>Level</th>
<th>Bearing Plate</th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Width</td>
<td>Length</td>
<td>Thickness</td>
<td>Hole dia.</td>
<td>$A_{Brg}$</td>
<td>Bearing Factor</td>
<td>Bearing Load</td>
</tr>
<tr>
<td>Roof</td>
<td>3.0</td>
<td>5.5</td>
<td>0.6</td>
<td>0.6875</td>
<td>15.788</td>
<td>1.07</td>
<td>2.565</td>
</tr>
<tr>
<td>5th Floor</td>
<td>3.0</td>
<td>3.5</td>
<td>0.4</td>
<td>0.6875</td>
<td>9.788</td>
<td>1.11</td>
<td>2.785</td>
</tr>
<tr>
<td>4th Floor</td>
<td>3.0</td>
<td>3.5</td>
<td>0.4</td>
<td>0.6875</td>
<td>9.788</td>
<td>1.11</td>
<td>4.665</td>
</tr>
<tr>
<td>3rd Floor</td>
<td>3.0</td>
<td>5.5</td>
<td>0.6</td>
<td>0.9375</td>
<td>15.396</td>
<td>1.07</td>
<td>5.395</td>
</tr>
</tbody>
</table>

Notes for Table 12:

1. Bearing plate is based on ASTM A36 steel with $F_y = 36$ ksi.
2. Bearing area factor for $l_b < 6$ inches:
   \[ C_b = \frac{I_b + 0.375}{I_b} \]

   Bearing area factor for $l_b \geq 6$ inches: $C_b = 1.0$
3. Bearing plate thicknesses shall be checked for bending using lengths governed by the area satisfaction check and the associated hole in the plate.
   Example bending check of bearing plate at third floor:
   Bearing plate size = 3.0 inches x 5.5 inches x 0.6 inches thick
   Bearing load = 5,395 lbs (Table 12)
   Bearing area for wood: subtracting for 3/16-inch oversized hold in wood plate
   \[ (16.5 - 1.104) = 15.396 \text{ sq in} \]
   \[ f_{cL} = \frac{5,395}{15.396} = 350 \text{ psi} \]
   \[ F'_{C} = F_c C_b = 625 \times 1.07 = 669 \text{ psi} > 350 \text{ psi okay} \]

Steel plate bending check:

\[ (350 \times 3.0) \times \left( \frac{5.5}{2} \right)^2 = 3,970 \text{ in/lb} \]
\[ Z_{plate} = \frac{bd^2}{4} = \frac{(3.0 - 0.9375) \times 0.6^2}{4} = 0.1856 \text{ in}^3 \]
\[ M = \frac{3,970}{0.1856} = 21.4 \text{ ksi okay} \]
4. Allowable capacity: $F'_{cL}A_{BrC}gCb$

Where: $F'_{cL} = 0.625 \text{ ksi}$

5. The bearing area is based upon the sill plate hole diameter being 1/4-inch larger than the rod diameter.

6. Bearing load = differential load from Table 10.

**BOLTED TIE-DOWN DEVICE ELEMENTS**

Another type of tie-down device, illustrated in Figure 15, utilizes bolts instead of bearing plates to transfer the overturning forces to the continuous rods. In this system, posts need to transfer tension forces. Although this type of system is still available, most framing contractors prefer the bearing plate devices due to quicker/easier installation in the field.

**TAKE-UP DEVICES**

Most continuous rod systems have methods of compensating for shrinkage with proprietary expanding or contracting devices.

The purpose of these devices is to minimize the clearance created between the holdown, tension tie connector, or plate washer and the anchor bolt/nut due to building settlement or wood shrinkage. They keep rotating the nut down (or use a compression spring) on the rod so the holdown, tension tie or bearing plate remains tight to the wood surface.

ICC Evaluation Service has acceptance criteria (AC 316) for shrinkage compensating (take-up) devices. The design engineer should check to see that the proprietary devices conform to these criteria.

The use of take-up devices is highly desirable in multi-level wood-framed construction. Since the total shrinkage of the building has to be accounted for in the tie-down displacement ($d_y$), it is very difficult to meet the code drift requirements for most shear walls without take-up devices, especially for short-length shear walls.

Take-up devices deflect under load just like the conventional holdown. Most manufacturers publish this information either in their brochures or Evaluation Service approvals. The deformation or initial slack of these devices needs to be considered in the overall tie-down displacement ($d_y$).

Take-up devices have moving parts and may jam if not properly installed. Jamming typically occurs as a result of excessive continuous tie rod angle (out-of-plumb). See the manufacturer’s instructions for proper installation.

**7. Considerations with Continuous and Discontinuous Anchor Tie-downs**

Continuous tie-downs have several advantages over conventional tie-downs—such as ease of installation and the achievement of higher uplift capacities. Most conventional tie-downs (hold downs) do not offer the capacities needed for multi-level construction, or the shrinkage compensating devices that are available in continuous tie-down systems.

**SKIPPING OF FLOORS FOR BEARING RESTRAINTS**

To reduce costs, some manufacturers “skip” floors with the bearing restraint devices. In this design example, bearing devices may be omitted at the third and fifth floors with restraints at the fourth floor and roof locations. When floors are skipped, the magnitude of tie-down assembly displacement is accumulative between the bearing restraints and hence significantly increases the shear wall deflection(s). Skipping floors is not recommended.
BEARING ZONE THROUGH FRAMING

Compression loads to the boundary members (posts) are achieved by nailing the shear wall sheathing to each boundary member, thus transferring the overturning (compression) forces, and are accumulative to the stories below. As the shear wall transfers the overturning (tension) forces to the boundary members, these forces collect at each level (between restrain devices) and transfer the differential loads (see Table 10) to the bearing plates at the level above (see Figure 14). The engineer should consider how the differential uplift forces are transferred from the boundary members to the bearing plate. As a general rule, when the differential uplift forces can be transferred within a bearing area located within a 45 degree plane from the bearing plate, no further investigation is necessary (see Figure 14A). When the transfer of forces requires an area larger than the 45 degree plane, some sort of further investigation is necessary (e.g., bending and shear checks of top plates etc.).

Example bearing check (See Figure 14A):
- Differential load at third floor = 5,395 lb (from Table 10)
- Bearing plate width = 5.5 inches (from Table 12)
- Bearing width at bottom of 4x4 top plate = (5.5 + 5.7 + 5.7) = 16.9 inches
- Net bearing area = (16.9 – 6.0) x 3.5 = 38.1 square inches
- Bearing stress = 5,395/38.1 = 142 psi < 625 psi okay
- Posts at plate = 5,395/(2 x 3.5 x 3.5) = 220 psi < 625 psi okay

8. Shear Wall Deflection, Tie-Down and Take-up Devices

8a. Continuous Tie-down Assembly Displacement

The continuous tie-down assembly displacement ($d_a$) is a collective accumulation of the deformation of tie-down elements. Each of these elements deforms, elongates and/or shrinks.

2006 IBC now has a revised definition of $d_a$ stated as follows:

“Vertical elongation of overturning anchorage (including fastener slip, device deflection, anchor rod elongation, etc.) at the design shear load ($\nu$).”

The net effect of the tie-down assembly displacement is a rotation of the shear wall, as a rigid body, with the displacement at the top of the wall ($\Delta$) equal to the aspect ratio times the tie-down assembly displacement ($d_a$).

**Figure 12. Effect of $d_a$ on drift**

NOTES FOR FIGURE 12:
Where:  
$h$ = floor-to-floor height  
b = the out-to-out dimension of the shear wall
ROD ELONGATION
Some jurisdictions have limits on the amount of rod elongation that can occur between restraints, and some require that the “allowable stress area” ($A_e$ vs. $A_g$) be used in rod elongation calculations. As such, local building department requirements should always be checked. This design example uses $A_e$ for rod elongation and $A_g$ or $A_n$ for rod capacity. Many manufactures will vary the yield strength of the tension rods. It should be noted that the use of a higher strength rod can actually increase the drift of the shear wall, due to increased elongation from higher loads that can be placed on the same size rod diameters and the modulus of elasticity of the steel, which does not change.

For further discussion on rod elongation see section 6j.

SILL PLATE CRUSHING
Per NDS-05 § 4.2.6, when compression perpendicular to grain $f_c \perp$ is less than $0.73 F_c \perp$, crushing will be approximately 0.02 inch. When $f_c \perp = F_c \perp$, crushing is approximately 0.04 inch. The effect of sill plate crushing is the downward effect at the opposite end of the wall (resulting from the boundary chords) and has the same rotational effect as the tie-down displacement ($d_{ty}$). Short walls that have no (net) uplift forces will still have a crushing effect at wall boundaries and contribute to rotation of the wall.

Table 13. Determine sill plate crushing

<table>
<thead>
<tr>
<th>Level</th>
<th>Chord Posts</th>
<th>ASD Demand (kips)</th>
<th>Strength Demand (kips)</th>
<th>Total Area ($in^2$)</th>
<th>$f_c \perp$ (ksi)</th>
<th>0.73$F_c \perp$ (ksi)</th>
<th>Crush (in)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Roof</td>
<td>4-3x4</td>
<td>4.06</td>
<td>5.62</td>
<td>35.0</td>
<td>0.160</td>
<td>0.456</td>
<td>0.007</td>
</tr>
<tr>
<td>5th Floor</td>
<td>4-3x4</td>
<td>11.53</td>
<td>16.13</td>
<td>35.0</td>
<td>0.461</td>
<td>0.456</td>
<td>0.023</td>
</tr>
<tr>
<td>4th Floor</td>
<td>4-4x8</td>
<td>22.88</td>
<td>32.13</td>
<td>101.5</td>
<td>0.317</td>
<td>0.456</td>
<td>0.015</td>
</tr>
<tr>
<td>3rd Floor</td>
<td>4-4x8</td>
<td>33.85</td>
<td>47.62</td>
<td>101.5</td>
<td>0.469</td>
<td>0.456</td>
<td>0.025</td>
</tr>
</tbody>
</table>

Where:
1. ASD demand and strength demand values are obtained from Table 8.
2. Crushing value ranges from 0.00 to 0.02 inch when $f_c \perp$ ranges from 0.0 psi to $0.73 F_c \perp$, and ranges from 0.02 to 0.04 inch when $f_c \perp$ ranges from $0.73 F_c \perp$ to $F_c \perp$. Values are interpolated to obtain the crushing values listed (crush).

Table 14. Determine bearing plate crushing

<table>
<thead>
<tr>
<th>Level</th>
<th>ASD Bearing Load (kips)</th>
<th>Strength Bearing Load (kips)</th>
<th>Bearing Plate $A_{bg}$ ($in^2$)</th>
<th>$f_c \perp$ (ksi)</th>
<th>0.73$F_c \perp$ (ksi)</th>
<th>Crush (in)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Roof</td>
<td>2.565</td>
<td>3.664</td>
<td>15.788</td>
<td>0.232</td>
<td>0.456</td>
<td>0.010</td>
</tr>
<tr>
<td>5th Floor</td>
<td>2.785</td>
<td>3.979</td>
<td>9.788</td>
<td>0.406</td>
<td>0.456</td>
<td>0.018</td>
</tr>
<tr>
<td>4th Floor</td>
<td>4.665</td>
<td>6.664</td>
<td>9.788</td>
<td>0.681</td>
<td>0.456</td>
<td>0.047</td>
</tr>
<tr>
<td>3rd Floor</td>
<td>5.395</td>
<td>7.707</td>
<td>15.396</td>
<td>0.501</td>
<td>0.456</td>
<td>0.025</td>
</tr>
</tbody>
</table>
Where:

1. ASD bearing load values are obtained from the differential loads of Table 11.
2. Strength bearing loads are obtained by dividing ASD bearing loads by the conversion factor of 0.7.
3. Note that the “allowable” $F_{cL}$ has been exceeded at the fourth floor; however, this design example uses “strength” (LRFD) loads where the bearing resistance is:

$$F_{cL} = \phi F_c K_p C_{f} C_b = 1.0 \times 0.9 \left(\frac{1.875}{0.9}\right) 625 \times 1.11 = 1,300 \text{ psi} > 681 \text{ psi okay}$$

Also see ASD bearing plate capacities and bearing factors from Table 12.

<p>| Table 15. Determine tie-down assembly displacement (with shrinkage compensators) |
|---------------------------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|</p>
<table>
<thead>
<tr>
<th>Level</th>
<th>Rod Elong. (in)</th>
<th>Shrinkage (Vertical Displacement) (in)</th>
<th>Chord Crushing (in)</th>
<th>Bearing Plate Crushing (in)</th>
<th>Take-up Deflection Elongation (in)</th>
<th>Total Displacement $d_a$ (in)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Roof</td>
<td>0.047</td>
<td>0.03</td>
<td>0.007</td>
<td>0.010</td>
<td>0.03</td>
<td>0.124</td>
</tr>
<tr>
<td>5th Floor</td>
<td>0.098</td>
<td>0.03</td>
<td>0.023</td>
<td>0.018</td>
<td>0.03</td>
<td>0.199</td>
</tr>
<tr>
<td>4th Floor</td>
<td>0.183</td>
<td>0.03</td>
<td>0.015</td>
<td>0.047</td>
<td>0.03</td>
<td>0.305</td>
</tr>
<tr>
<td>3rd Floor</td>
<td>0.138</td>
<td>0.03</td>
<td>0.025</td>
<td>0.025</td>
<td>0.03</td>
<td>0.248</td>
</tr>
</tbody>
</table>

<p>| Table 15A. Determine tie-down assembly displacement (without shrinkage compensators) |
|---------------------------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|</p>
<table>
<thead>
<tr>
<th>Level</th>
<th>Rod Elong. (in)</th>
<th>Shrinkage (Vertical Displacement) (in)</th>
<th>Chord Crushing (in)</th>
<th>Bearing Plate Crushing (in)</th>
<th>Total Displacement $d_a$ (in)</th>
<th>Accumulative Displacement $d_a$ (in)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Roof</td>
<td>0.047</td>
<td>0.170</td>
<td>0.007</td>
<td>0.010</td>
<td>0.234</td>
<td>1.311</td>
</tr>
<tr>
<td>5th Floor</td>
<td>0.098</td>
<td>0.170</td>
<td>0.023</td>
<td>0.018</td>
<td>0.309</td>
<td>1.077</td>
</tr>
<tr>
<td>4th Floor</td>
<td>0.183</td>
<td>0.170</td>
<td>0.015</td>
<td>0.042</td>
<td>0.410</td>
<td>0.768</td>
</tr>
<tr>
<td>3rd Floor</td>
<td>0.138</td>
<td>0.170</td>
<td>0.025</td>
<td>0.025</td>
<td>0.358</td>
<td>0.358</td>
</tr>
</tbody>
</table>

Notes for Tables 15 and 15A:

Where:

1. Rod Elongation values are obtained from Table 11.
2. Shrinkage values (vertical displacement) are obtained from Table 5; where shrinkage compensating devices are used, a value of 1/32 inch is used, recognizing that most devices have to travel a distance before they get to the next “groove” in the device to re-adjust.
3. Chord crushing (crush) values are obtained from Table 13.
4. Bearing plate (crush) values are obtained from Table 14.
5. Take-up deflection elongation in Table 15A is 0.00 inches because the device has been omitted.
6. Without shrinkage compensators (Table 15A), the tie-down assembly displacements are accumulative from floor-to-floor level.
8b. Shear Wall Deflection

DEFLECTION EQUATION:
The IBC lists the following well-known four-term equation to determine the shear wall deflection:

\[
\delta = \frac{8vh^3}{EA_b} + \frac{vh}{G_t} + 0.75 \frac{h e_n}{b} + \frac{h}{b} d_{a}
\]

**IBC Eq. 23-2**

Where:
- \( E \) = Modulus of Elasticity of diaphragm chords
  - \( E = 1,700,000 \) psi
- \( A_b \) = area of chord cross-section (3x4 posts or 4x8 posts in this design example)
- \( G_t \) = sheathing shear stiffness from nail slip and panel shear deformation (from IBC Table 2305.2.2(2)).
  - \( G_t = 44,500 \) lb/in for 15/32" Structural I, 5-ply plywood and 83,500 lb/in for OSB
- \( b \) = shear wall length
- \( h \) = height of the wall in feet
- \( v \) = incurred unit shear in diaphragm
- \( d_{a} \) = continuous tie-down assembly displacement (see section 8a for discussion)
- \( e_n \) = nail deformation

The NDS-05 SDPWS lists the following three-term equation to determine the shear wall deflection:

\[
\delta = \frac{8vh^3}{EA_b} + \frac{vh}{1,000 G_a} + \frac{h}{b} d_{a}
\]

**SDPWS Eq. C4.3.2-2**

Where:
- \( E \) = Modulus of elasticity of diaphragm chords
  - \( E = 1,700,000 \) psi
- \( A_b \) = area of chord cross-section (3x4 posts or 4x8 posts in this design example)
- \( G_a \) = apparent diaphragm shear stiffness from nail slip and panel shear deformation (from Column A – Table 4.2A); for 6-inch nailing in a blocked diaphragm:
  - \( G_a = 17.0 \) kips/in
  - Note: \( G_a \) values are to be multiplied by 0.5 if the moisture content is 19% at time of installation of nails/fasteners.
- \( b \) = shear wall length
- \( v \) = incurred unit shear in diaphragm
- \( h \) = height of the wall in feet
- \( d_{a} \) = continuous tie-down assembly displacement (see section 8b for discussion)

The new simplified three-term equation combines the second and third terms (of the four-term equation) into one term. The computed deflections by using either the four-term equation or the three-term equation produce nearly identical results.

This design example uses the SDPWS three-term equation.
### Table 16. Determine shear wall deflection (using shrinkage compensating devices)

<table>
<thead>
<tr>
<th>Level</th>
<th>ASD Shear (plf)</th>
<th>Strength Shear (plf)</th>
<th>h (ft)</th>
<th>A (in$^2$)</th>
<th>b (ft)</th>
<th>$G_a$ (k/in)</th>
<th>Nail Spacing (in)</th>
<th>Total Displacement $d_a$ (in)</th>
<th>Deflection $\delta_{xe}$ (in)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Roof</td>
<td>340</td>
<td>485</td>
<td>10.0</td>
<td>35.0</td>
<td>29.0</td>
<td>22.0</td>
<td>6</td>
<td>0.124</td>
<td>0.27</td>
</tr>
<tr>
<td>5th Floor</td>
<td>565</td>
<td>807</td>
<td>10.0</td>
<td>35.0</td>
<td>29.0</td>
<td>36.0</td>
<td>3</td>
<td>0.199</td>
<td>0.30</td>
</tr>
<tr>
<td>4th Floor</td>
<td>720</td>
<td>1,028</td>
<td>10.0</td>
<td>101.5</td>
<td>29.0</td>
<td>51.0</td>
<td>2</td>
<td>0.305</td>
<td>0.31</td>
</tr>
<tr>
<td>3rd Floor</td>
<td>800</td>
<td>1,142</td>
<td>10.0</td>
<td>101.5</td>
<td>29.0</td>
<td>51.0</td>
<td>2</td>
<td>0.248</td>
<td>0.31</td>
</tr>
</tbody>
</table>

### Table 16A. Determine shear wall deflection (without shrinkage compensating devices)

<table>
<thead>
<tr>
<th>Level</th>
<th>ASD Shear (plf)</th>
<th>Strength Shear (plf)</th>
<th>h (ft)</th>
<th>A (in$^2$)</th>
<th>b (ft)</th>
<th>$G_a$ (k/in)</th>
<th>Nail Spacing (in)</th>
<th>Total Displacement $d_a$ (in)</th>
<th>Deflection $\delta_{xe}$ (in)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Roof</td>
<td>340</td>
<td>485</td>
<td>10.0</td>
<td>35.0</td>
<td>29.0</td>
<td>22.0</td>
<td>6</td>
<td>1.311</td>
<td>0.68</td>
</tr>
<tr>
<td>5th Floor</td>
<td>565</td>
<td>807</td>
<td>10.0</td>
<td>35.0</td>
<td>29.0</td>
<td>36.0</td>
<td>3</td>
<td>1.077</td>
<td>0.60</td>
</tr>
<tr>
<td>4th Floor</td>
<td>720</td>
<td>1,028</td>
<td>10.0</td>
<td>101.5</td>
<td>29.0</td>
<td>51.0</td>
<td>2</td>
<td>0.768</td>
<td>0.47</td>
</tr>
<tr>
<td>3rd Floor</td>
<td>800</td>
<td>1,142</td>
<td>10.0</td>
<td>101.5</td>
<td>29.0</td>
<td>51.0</td>
<td>2</td>
<td>0.358</td>
<td>0.35</td>
</tr>
</tbody>
</table>

Where:

$$\delta = \frac{8vh^2}{EA} + \frac{vh}{1000G_a} + \frac{d_a}{b}$$

Comparing shear wall deflections, the shear walls without shrinkage compensating devices were found to deflect 2½ times more at the roof level than those with these devices. Further, the magnitude of the increased deflection increases significantly as the length of the shear wall decreases and the ratio of $h/b$ becomes larger.

Note that some jurisdictions require the calculated drifts to be increased by 1.25 to account for dynamic cyclic effects on the wall that could reduce its stiffness.

### 8c. Story Drift Determination

ASCE 7-05 §12.8.6

The code states that when allowable stress design is used, the computed story drift $\delta_{xe}$ shall be computed using strength-level seismic forces specified in ASCE 7-05 §12.8 without the reduction for allowable stress design.

For light-frame walls sheathed with wood structural panels rated for shear resistance, the design story drift is computed as follows:

$$\delta_x = \frac{C_d \delta_{xe}}{l}$$
Where:

\( \delta \) = design story drift

\( C_d \) = deflection amplification factor from ASCE 7-05 Table 12.2-1

\( C_d = 4.0 \)

\( I \) = occupancy factor

\( I = 1.0 \)

\( \delta_{xe} \) = calculated deflection at the top of the wall

\[ \delta_x = \frac{4.0 \delta_{xe}}{1.0} = 4.0 \delta_{xe} \]

The calculated story drift using \( \delta_x \) shall not exceed the maximum allowable which is 0.025 times the story height \( h \) for structures four stories or less in height. The calculated story drift shall not exceed 0.020 times the story height \( h \) for structures five stories or more in height. Since the overall building is five stories, the drift limit is 0.020 \( h \).

### DETERMINATION OF MAXIMUM DRIFTS

ASCE 7-05 Table 12.12-1

**Table 17. Determine shear wall drift vs. allowable drifts (with shrinkage compensators)**

<table>
<thead>
<tr>
<th>Level</th>
<th>Deflection ( \delta_{xe} ) (in)</th>
<th>( h ) (ft)</th>
<th>Story Design Drift ( 4.0\delta_{xe} ) (in)</th>
<th>Code Max. Allowable (in)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Roof</td>
<td>0.27</td>
<td>10.0</td>
<td>1.08</td>
<td>2.40</td>
</tr>
<tr>
<td>5th Floor</td>
<td>0.30</td>
<td>10.0</td>
<td>1.20</td>
<td>2.40</td>
</tr>
<tr>
<td>4th Floor</td>
<td>0.31</td>
<td>10.0</td>
<td>1.24</td>
<td>2.40</td>
</tr>
<tr>
<td>3rd Floor</td>
<td>0.31</td>
<td>10.0</td>
<td>1.24</td>
<td>2.40</td>
</tr>
</tbody>
</table>

**Table 17A. Determine shear wall drift vs. allowable drifts (without shrinkage compensators)**

<table>
<thead>
<tr>
<th>Level</th>
<th>Deflection ( \delta_{xe} ) (in)</th>
<th>( h ) (ft)</th>
<th>Story Design Drift ( 4.0\delta_{xe} ) (in)</th>
<th>Code Max. Allowable (in)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Roof</td>
<td>0.68</td>
<td>10.0</td>
<td>2.72</td>
<td>2.40</td>
</tr>
<tr>
<td>5th Floor</td>
<td>0.60</td>
<td>10.0</td>
<td>2.40</td>
<td>2.40</td>
</tr>
<tr>
<td>4th Floor</td>
<td>0.47</td>
<td>10.0</td>
<td>1.88</td>
<td>2.40</td>
</tr>
<tr>
<td>3rd Floor</td>
<td>0.35</td>
<td>10.0</td>
<td>1.40</td>
<td>2.40</td>
</tr>
</tbody>
</table>

Notes for Tables 17 and 17A:

Shear wall drifts do not include the diaphragm deflections between the shear walls but are considered negligible for this design example.

For the 29-foot-long wall used in this design study, the shear wall with the shrinkage compensating devices meets the drift requirements but the shear wall without the shrinkage compensating devices exceeds the drift requirements at roof level.
8d. Load Path for Rod Systems

**COMPRESSION MEMBERS**
When the shear wall end is in compression, the end chord members create a compression bearing path from the posts through blocking at the floor levels and then to the next set of posts below (Figure 13).

**TENSION RODS**
When the shear wall end is in tension, the end chord members lift up and bear in compression on the floor (or roof) above. The bearing plate (load transfer device) resists the individual story overturning by restraining the posts below from uplifting (Figure 14). The bearing plates transfer the uplifting forces from the posts to the tension rod.

![Figure 13. Load Transfer from Compression Posts to Compression Posts](image)

**NOTES FOR FIGURE 13:**
Detail A (at platform framed) may have a single block with a drilled hole for the tie-down rod (see Figure 15).
**Figure 14. Load Transfer from Uplifting Posts to Bearing Device**

NOTES:
Detail A (at platform framed) may have a single block with a drilled hole for the tie-down rod (see Figure 15).

**Figure 14A. Bearing Zone Through Framing from Uplifting Posts to Bearing Device**
8e. Proprietary Software for Continuous Tie-down Systems

Several continuous tie-down system manufacturers offer design software to aid the design engineer in the proper selection of their products as well as the proper selection of the compression chord members. The use of these software programs can be a big time saver for the engineer.

9. Discontinuous System Considerations and the Over Strength (Ω) Factor

9a. Anchor Forces to Podium Slab

For over 20 years, the building codes have had requirements for amplified forces to elements supporting discontinuous systems. Earlier editions of the codes used the term $3R_w/8$, while current codes use the term $Ω$. Previous editions of the IBC and the 97 UBC exempted concrete slabs supporting light-framed construction from these requirements. However, ASCE 7-05 has added “slabs” to the list of elements needing the design strength to resist the maximum axial force that can be delivered per the load combinations with the overstrength factor (Ω) in §12.4.3.2.

This means that the shear wall boundary overturning forces (axial uplift and axial compression) need to have the $Ω$ factor of 3.0 applied to the supporting slab design. Footnote g of ASCE 7-05 Table 12.2-1 states that, for structures with flexible diaphragms, this value may be 2.5. However, ASCE 7-05 has added commentary to the requirements in §12.4.3.2:

Section C12.4.3 of the ASCE 7-05 commentary states that:

This standard permits the special seismic loads to be taken as less than the amount computed by the $Ω_0$ coefficient … when it can be shown that yielding of other elements in the structure will limit the amount of load that can be delivered to the element.
In Addition, § C12.3.3.3 of the ASCE 7-05 commentary states that:

*Connection between shear wall and supporting member need only be designed to transmit the loads associated with the shear wall and not the special seismic loads.*

What the ASCE 7-05 commentary is stating is that the $\Omega$ factor of 3.0 need not be applied when it can be shown that yielding of other elements (diaphragm, collector, collector tie, etc.) will occur below the $\Omega$ level forces. In addition, the commentary is also stating that the “tie-down” to the slab need not be designed for the special seismic loads. The provision of §12.3.3.3 only requires that the connection be adequate to “transmit” the forces for which the discontinuous elements were required to be designed. The ability to “transmit” such forces addresses the need for the “strength” of the connection to be adequate (rather than ensuring elastic type of response in the connection—e.g., Omega factor increase).

Different jurisdictions interpret the application of the $\Omega$ factor to podium slabs differently and it is recommended that the engineer discuss the requirements with local building officials prior to starting the podium slab design.

It is common to have an anchor bolt (to the podium slab) not meet the requirements of ACI 318 Appendix D because of edge distances or embedment lengths available. Other means of bolt anchorage commonly used include “through bolting” or “sleeves” for a post installed through bolt, embed plates with welded studs, bearing plate washers at the bolt nut, or special steel reinforcing bars used in conjunction with the anchor bolts/bearing plates.

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**Suggestions for Improvement**

Comments and suggestions for improvement are welcome and should be e-mailed to WoodWorks at info@woodworks.org.
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